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Abstract- Supply chain management (SCM) is concerned with a complex business relations network that contains interrelationships between various entities, such as suppliers, manufacturers, distribution centers and customers. SCM integrates these entities and manages their interrelationships through the use of information technology to meet customer expectation effectively along the entire value chain. Thus, one of the vital issues in supply chain management is the design of the value chain network. In this paper, a multi objective fuzzy mathematical programming model is developed to optimize the supply chain networking under inherent uncertainty of input data. The proposed model is able to optimize the environmental impacts beside the traditional cost minimization objective to make a fair balance between them. The model determines the fuzzy capacities of the facilities and the design of the network configuration with a minimum total cost. A real case is used to demonstrate the significance and applicability of the developed fuzzy optimization model as well as the usefulness of the proposed solution approach. The developed model is solved by a professional software package (LINDO), and the computational results are discussed.

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1. INTRODUCTION

A well-structured supply chain is an important strategic competency that enables firms to be competitive in today's marketplace. Along this important issue, the concern about environmental impact of business activities results in governmental legislations and environmentally conscious consumers. Environmental or green supply chain management can be defined as integrating environmental aspects into supply chain management covering both forward and reverse supply chains from product design to end-of-life management of used products. The ultimate goal is to consider environment in every decision making process across supply chain, especially the strategic level decisions. Supply chain optimization can help define, recommend, and set flexible supply chain strategies based on organization's operations, resources, and other capabilities. Optimization of supply chain network design, as the most important strategic decision in supply chain management, plays an important role in overall environmental and economic performance of the

supply chain. In general, supply chain network design includes determining the locations, numbers and capacities of network facilities and the aggregate material flow between them. Since the end-of-life (EOL) products have significant impact on environment, a considerable part of literature is dedicated to EOL product management. This has created a need to develop models for reverse supply chain (logistics) network design. Reverse supply chain network design problem addresses the number of collection, recovery, recycling and disposal centers needed, their location and capacities and material flows between them.

In the last several years, many studies have been proposed and much research has been performed on the design and optimization of supply chain networks. In one study, Pirkul and Jayaraman [1] studied a multi-commodity, multi-plant, capacitated facility location problem and proposed an efficient heuristic solution to the problem. In the capacitated plant and warehouse location model, customers typically demand multiple units of different products that are distributed to customer outlets from open warehouses that receive these products from several manufacturing plants. The objective function of the model minimizes the sum of the fixed cost of establishing and operating the plants and the warehouses plus the variable cost of transporting units of products from the plants to the warehouses and distributing the products from the warehouses to the customer, to satisfy the multiple demands of the customers. Recently Ilgin and Gupta et al. [2] present a comprehensive review on environmentally conscious manufacturing and product recovery; below we have surveyed some relevant papers on environmental supply chain network design. Timpe and Kallrath [3] considered a multi-site, multi-product production network and presented a general mixed integer linear programming model that combines aspects related to production, distribution and marketing and involves production sites (plants) and sales points. Cakra vastia et al. [4] developed an analytical model of the supplier selection process in designing a supply chain network. The constraints on the capacity of each potential supplier are considered in the process. The objective of the supply chain is to minimize the level of customer dissatisfaction, which is evaluated by two performance

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criteria: (i) price and (ii) delivery lead time. The overall model operates at two levels of decision making: the operational level and the chain level. The operational level concerns decisions related to optimizing the manufacturing and logistical activities of each potential supplier, to meet the customer's requirements. At the chain level, all of the bids from potential suppliers are evaluated, and the final configuration of the supply chain is determined. The structure of the chain depends on the product specifications and on the customer's order size. An optimal solution in terms of the models for the two levels can be obtained using a mixed-integer programming technique [4, 5] presented a multi-phase mathematical programming approach for effective supply chain design. Syarif et al. [6] considered the logistic chain network problem formulated by the 0-1 mixed integer linear programming problem. The design of the problem involves the choice of the facilities (plants and distribution centers) to be opened and the distribution network design, with the goal of satisfying the demand with minimum cost. For the solution method, the spanning tree-based genetic algorithm using Prüfer number representation is proposed. Sanayeia et al. [7] proposed an integrated approach of multi-attribute utility theory (MAUT) and linear programming (LP) for rating and choosing the best suppliers and defining the optimum order quantities among selected ones in order to maximize total additive utility. Javadi et al. [8] developed a fuzzy multi-objective linear programming (FMOLP) model for solving the multi-objective no-wait flow shop scheduling problem in a fuzzy environment. The proposed model attempted to simultaneously minimize the weighted mean completion time and the weighted mean earliness. A numerical example demonstrated the feasibility of applying the proposed model to no-wait flow shop scheduling problem. The proposed model yielded a compromised solution and the decision maker's overall levels of satisfaction.

To overcome the literature gap, this paper proposes a practical, but tractable, multi-objective fuzzy mathematical programming model for optimization of supply chain networking perspective environmental impact problem that is able to (1) consider both economic and environmental objectives in the design of the supply chain network, (2) integrate the design of reverse and forward supply chain networks to avoid the sub-optimality's results from separated design of forward and reverse supply chains, (3) The model allows decision-makers to design the network configuration with the minimum total cost. (4) Handle the epistemic uncertainty in parameters in real cases results from unavailability or incompleteness and imprecise nature of input data. Also, this paper proposes an efficient solution approach that is able to generate both balanced and unbalanced solutions through making a

reasonable tradeoff between environmental and economic objectives.

This paper is organized into eight sections. After the introduction, in which some supply chain models are described, the remainder of the paper is structured as follows. In Section 2, problem statement of the proposed supply chain network is introduced. This model is formulated in section 3 and developed an equivalent auxiliary crisp model in section 5. Implementation and evaluation of this proposed model is described in section 6, and section 7 represents the results and discussion. Conclusions are presented in Section 8. As well as finally appendix and references are attached.

II. PROBLEM STATEMENT

The concerned integrated supply chain network in this paper is motivated by a real industrial case. The case is a supply chain network of Coca-Cola drinks in Bangladesh that supplies about 80% of domestic demand. The manufacturer has one production plant with about 600 thousand production capacity per one year. In transportation system of supply chain networking consists of environmental impact like, carbon dioxide (CO_2) that is responsible for the environmental disasters. To overcome this problem proposed a multi-echelon supply chain network that includes both forward and reverse networks is illustrated in Fig. 1. Through forward network the new products manufactured by plants (production centers) are distributed among customer zones. In the reverse network, the used products are shipped to recycling centers through collection/disassembly centers. All demands of customers must be satisfied and all of the returned products from customers must be collected. Also, a predefined percent of demand from each customer is assumed as returned products from corresponding customer. Unavailability or incompleteness of data in real world network optimization problems is an important challenge that imposes a high degree of uncertainty in such problem. The problem is concerned with the uncertain parameters are presented by fuzzy numbers described by their possibility distribution. The possibility distributions are estimated based on current insufficient data and the decision makers' knowledge. The main objective of this integrated supply chain under uncertain condition includes the material flow quantities between different facilities with respect to two conflicting objective functions: (1) minimization of total cost and (2) minimization of total environmental impact.

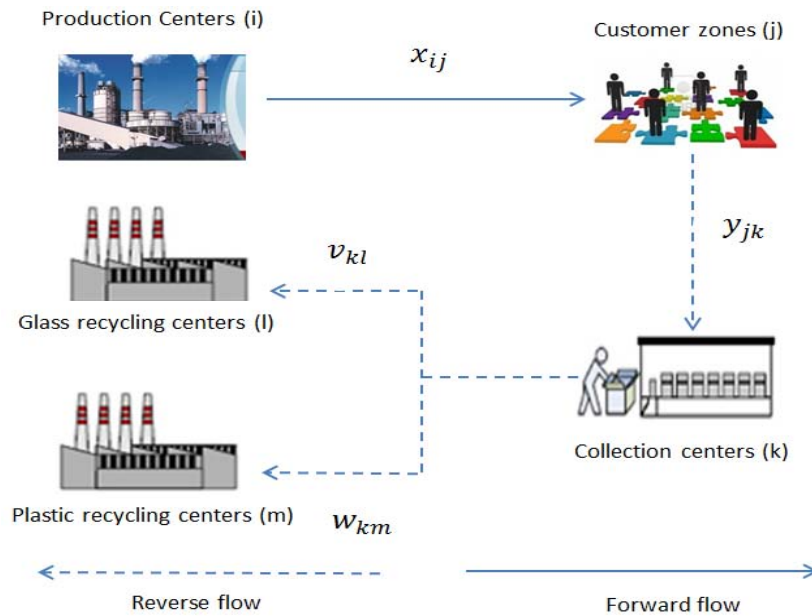


Fig. 1 : Concerned integrated supply chain network

III. MODEL FORMULATION

The indices, parameter and variables used to formulate the concerned environmental supply chain network design problem.

a) Indices

i = index of candidate location for production centers, $i = 1, 2, 3, 4, \dots, i$

j = index of fixed location of customer zones, $j = 1, 2, 3, 4, \dots, j$

k = index of candidate location for collection centers, $k = 1, 2, 3, 4, \dots, k$

l = index of existing glass recycling centers, $l = 1, 2, 3, 4, \dots, l$

m = index of existing plastic recycling centers, $m = 1, 2, 3, 4, \dots, m$

b) Parameters

d_j = demand of customer zone, j

w_j = rate of return percentage from customer zones, j

f_i = fixed cost of opening production centers, i

g_k = fixed cost of opening collection centers, k

c_{ij} = transportation cost per product unit from plant, i to customer zones, j

a_{jk} = transportation cost of per used product unit from customer zone, j to collection center, k

b_{kl} = transportation cost of per glass part of used product unit from collection center, k to glass recycling center, l

h_{km} = transportation cost of per plastic part of used product unit from collection center, k to plastic recycling center, m

ρ_i = manufacturing cost per unit of product at production center, i

ϕ_k = processing cost for per unit of used product at collection center, k

β_l = processing cost for per glass part of used product unit at glass recycling center, l

α_m = processing cost for per plastic part of used product unit at plastic recycling center, m

π_i = maximum capacity of production center, i

η_k = maximum capacity of collection center, k

δ_l = maximum capacity of glass recycling center, l

θ_m = maximum capacity of plastic recycling center, m

e_i^{pro} = Environmental impact per production of one unit of product

e_{ij}^{tpc} = environmental impact of shipping one unit of product from plant, i to customer zone, j

e_{jk}^{tcc} = environmental impact of shipping one unit of used product from customer zone, j to collection center, k

e_{kl}^{tcs} = environmental impact of shipping glass part of used product unit from collection center, k to glass recycling center, l

e_{km}^{tcp} = environmental impact of shipping plastic part of used product unit from collection center, k to plastic recycling center, m

e_i^{col} = environmental impact per handling one unit of collected used product at collection centers

e_i^{src} = environmental impact of recycling the glass part of one unit of used product

e_i^{prc} = environmental impact of recycling the plastic part of one unit of used product

c) Variables

x_{ij} = quantity of product shipped from plant, i to customer zone, j

y_{jk} = quantity of used product shipped customer zone, j to collection center, k

v_{kl} = quantity of glass part of used product shipped from collection center, k to glass recycling center, l

w_{km} = quantity of plastic part of used product shipped from collection center, k to plastic recycling center, m

$$u_i = \begin{cases} 1, & \text{if a production center opened at location, } i \\ 0, & \text{otherwise} \end{cases}$$

$$q_k = \begin{cases} 1, & \text{if a collection center opened at location, } k \\ 0, & \text{otherwise} \end{cases}$$

d) Objective Function

There are two objective functions are considered:

- i. Minimization of total cost
- ii. Minimization of total environmental impact

First objective Function: minimization of total cost

$$\text{Min } w_1 = \sum_i f_i u_i + \sum_k g_k q_k + \sum_i \sum_j (\rho_i + c_{ij}) x_{ij} + \sum_j \sum_k (\phi_k + a_{jk}) y_{jk} + \sum_j \sum_k (\phi_k + a_{jk}) y_{jk} + \sum_k \sum_l (\beta_l + b_{kl}) v_{kl} + \sum_k \sum_m (\alpha_m + h_{km}) w_{km}$$

Here transportation costs between facilities are calculated by multiplying the transportation cost of one unit shipping per unit of distance.

For the second objective: minimizing the total environmental impact

The purpose of this supply chain network is to fulfill the customer demand by producing and distributing the product at forward network and the safe management of product by reverse network.

The purpose of using ECO-indicator is to estimate the environmental impact of different supply chain network configurations. Following ECO-indicators are considered for this supply chain network design.

- The production (*pro*)
- Transportation from production centers to customer zone (*tpc*)
- Transportation from customer zone to collection centers (*tcc*)
- Handling the used product at collection centers (*col*)
- Transportation from collection to glass recycling centers (*tcs*)
- Glass recycling center (*src*)
- Transportation from collection centers to plastic recycling centers (*tcp*)
- Plastic recycling centers (*src*)

Second objective function: minimization of total environmental impact

$$\text{Min } w_2 = \sum_i \sum_j (e_i^{pro} + e_{ij}^{tpc}) x_{ij} + \sum_j \sum_k (e_j^{col} + e_{jk}^{tcc}) y_{jk} + \sum_k \sum_l (e_l^{src} + e_{kl}^{tcs}) v_{kl} + \sum_k \sum_m (e_k^{tcp} + e_{km}^{src}) w_{km}$$

IV. CONSTRAINTS

Demand and return satisfaction constraints

Here following constraints (3) and (4) ensure the demands of all customers are satisfied and the entire used products are collected from the customer zones.

$$\sum_i x_{ij} \geq d_j \tag{3}$$

$$\sum_k y_{jk} \geq d_j w_j \tag{4}$$

a) Flow Balance Constraints

Here constraints (5) and (6) ensure the flow balance at collection centers. Two EOL options are considered in the proposed model, the collected used product should be sent to glass and plastic recycling centers. Therefore the total number of plastic and glass parts should be equal to recycling centers because they are disassembled from one used product.

$$\sum_j y_{jk} \geq \sum_m w_{km} \tag{5}$$

$$\sum_m w_{km} \geq \sum_l v_{kl} \tag{6}$$

b) Capacity Constraint

$$\sum_j x_{ij} \geq u_i \pi_i \tag{7}$$

$$\sum_j y_{jk} \geq q_k \eta_k \tag{8}$$

$$\sum_l v_{kl} \leq \delta_l \tag{9}$$

$$\sum_m w_{km} \leq \theta_m \tag{10}$$

Here constraints (8) to (10) are capacity constraints on production, collection and glass recycling and plastic recycling centers respectively. Also constraints (7) and (8) prohibit the units of new and used products from being transferred to production and collection centers which are not opened respectively.

Decision variables constraints

The following constraints are related to the binary and non-negatively restrictions on the corresponding decision variables.

$$u_i, q_k \in \{0, 1\} \tag{11}$$

$$x_{ij}, y_{jk}, v_{kl}, w_{km} \geq 0 \tag{12}$$

V. PROPOSED METHOD

This is a multi-objective probabilistic mixed integer programming model. To solve this model a two phase approach is proposed one is the method of Jimenez to convert the proposed model and the second

phase proposed a modified version of ϵ -constraint method to find the final preferred compromise solution.

VI. EQUIVALENT AUXILIARY CRISP MODEL

Jimenez et al. [9] method is selected to develop this equivalent auxiliary crisp model as well as this model is based on mathematical concepts that is expected interval and expected value of fuzzy numbers and also explain a ranking method which can support

different kind of membership functions such as triangular, trapezoidal and nonlinear ones in both symmetric and asymmetric functions. This method also computational efficient to solve fuzzy linear problems as it can preserve its linearity and do not increase the number of objective functions and inequality constraints. The detail of this method is given in Appendix.

Equivalent auxiliary crisp model can be formulated as follows:

$$\begin{aligned} \min w_1 = & \sum_i \left(\frac{f_i^{pes} + 2f_i^{mos} + f_i^{opt}}{4} \right) u_i + \sum_k \left(\frac{g_k^{pes} + 2g_k^{mos} + g_k^{opt}}{4} \right) q_k + \sum_i \sum_j \left(\frac{\rho_i^{pes} + 2\rho_i^{mos} + \rho_i^{opt} + c_{ij}^{pes} + 2c_{ij}^{mos} + c_{ij}^{opt}}{4} \right) x_{ij} + \\ & \sum_j \sum_k \left(\frac{\phi_k^{pes} + 2\phi_k^{mos} + \phi_k^{opt} + c_{jk}^{pes} + 2c_{jk}^{mos} + c_{jk}^{opt}}{4} \right) y_{jk} + \sum_k \sum_l \left(\frac{\beta_l^{pes} + 2\beta_l^{mos} + \beta_l^{opt} + b_{kl}^{pes} + 2b_{kl}^{mos} + b_{kl}^{opt}}{4} \right) v_{kl} + \\ & \sum_k \sum_m \left(\frac{\alpha_m^{pes} + 2\alpha_m^{mos} + \alpha_m^{opt} + h_{km}^{pes} + 2h_{km}^{mos} + h_{km}^{opt}}{4} \right) w_{km} \end{aligned}$$

$$\min w_2 = \sum_i \sum_j (ei^{pro} + ei^{tpc}) x_{ij} + \sum_j \sum_k (ei^{col} + ei^{tcc}) y_{jk} + \sum_k \sum_l (ei^{src} + ei^{tcs}) v_{kl} + \sum_k \sum_m (ei^{prc} + ei^{tcp}) w_{km}$$

Subject to,

$$\sum_i x_{ij} \geq \alpha \left(\frac{d_j^{mos} + d_j^{opt}}{2} \right) + (1-\alpha) \left(\frac{d_j^{pes} + d_j^{mos}}{2} \right)$$

$$\sum_k y_{jk} \leq \left[\alpha \left(\frac{d_j^{mos} + d_j^{opt}}{2} \right) + (1-\alpha) \left(\frac{d_j^{pes} + d_j^{mos}}{2} \right) \right] \left[\alpha \left(\frac{w_j^{mos} + w_j^{opt}}{2} \right) + (1-\alpha) \left(\frac{w_j^{pes} + w_j^{mos}}{2} \right) \right]$$

$$\sum_j q_{jk} = \sum_m w_{km}$$

$$\sum_m w_{km} = \sum_l v_{kl}$$

$$\sum_j x_{ij} \leq u_i \left[\alpha \left(\frac{\pi_i^{pes} + \pi_i^{mos}}{2} \right) + (1-\alpha) \left(\frac{\pi_i^{mos} + \pi_i^{opt}}{2} \right) \right]$$

$$\sum_j y_{jk} \leq q_k \left[\alpha \left(\frac{\eta_k^{pes} + \eta_k^{mos}}{2} \right) + (1-\alpha) \left(\frac{\eta_k^{mos} + \eta_k^{opt}}{2} \right) \right]$$

$$\sum_k v_{kl} \leq \left[\alpha \left(\frac{\delta_l^{pes} + \delta_l^{mos}}{2} \right) + (1-\alpha) \left(\frac{\delta_l^{mos} + \delta_l^{opt}}{2} \right) \right]$$

$$\sum_k w_{km} \leq \left[\alpha \left(\frac{\theta_m^{pes} + \theta_m^{mos}}{2} \right) + (1-\alpha) \left(\frac{\theta_m^{mos} + \theta_m^{opt}}{2} \right) \right]$$

$$u_i, q_k \in \{0, 1\}$$

$$x_{ij}, y_{jk}, v_{kl}, w_{km} \geq 0$$

VII. IMPLEMENTATION AND EVALUATION

The validity of the developed model as well as the usefulness of the proposed solution method is investigated via the data withdrawn from the case study. The manufacturer firm has nine customer zones. The firm is responsible to collect the used product from domestic customers therefore the return rate from the foreign customer is considered equal to zero. To estimate the possibility of distribution parameters first objective data is gathered and the firm managers

determined three prominent values (most likely, most pessimistic and most optimistic) of triangular fuzzy numbers according to available data. The fuzzy data for demand and rate of return each customer is represented in table: 1 for the over three years. The firm managers considered eight candidate locations to open new production centers. At reverse network, candidate locations are considered as the collections centers as well as the corresponding capacity are represented in table: 2 and 3.

Table 1 : Demand (d_j) and rate of return (w_j)

Customer zone (j)	Demand, d_j (Thousand)			Rate of Return (w_j)		
	pes	mos	opt	pes	mos	opt
Khulna	234	254	292	0.65	0.75	0.85
Rajshahi	295	330	390	0.65	0.75	0.85
Chitagong	112	124	138	0.65	0.75	0.85
Dhaka	98	110	127	0.55	0.65	0.75
Narayongonj	84	93	110	0.70	0.80	0.90
Rangpur	100	118	131	0.65	0.75	0.85
Savar	198	211	228	0.65	0.75	0.85
Barisal	215	240	270	0.70	0.80	0.90
India	320	344	360	0	0	0

Table 2 : Data for fixed cost (f_i) and capacity (π_i) for production centers

Location(i)	Fixed Cost, f_i (Thousand)			Capacity, π_i (Thousand)		
	pes	mos	opt	pes	mos	opt
Khulna	13300	14500	15300	190	200	210
Rajshahi	13500	14700	15400	190	200	210
Narayongonj	13600	14800	15500	200	210	220
Chitagong	13500	14700	15400	165	180	195
Dhaka	13000	14000	15000	190	200	210
Rangpur	13600	14700	15400	190	200	210
Barisal	13400	14200	15200	165	180	195
Joshor	0	0	0	170	190	210

Table 3 : Fixed cost (g_k) and capacity (η_k) for collection centers

Location, i	Fixed cost, g_k (Thousand)			Capacity, η_k (Thousand)		
	pes	mos	opt	pes	mos	opt
Khulna	1700	1740	1780	240	245	250
Rajshahi	1750	1790	1830	240	245	250
Chitagong	1700	1740	1780	250	255	260
Dhaka	1680	1720	1740	220	225	230
Narayongonj	1780	1830	1880	230	235	240
Rangpur	1760	1810	1860	220	205	210
Savar	1740	1780	1820	200	205	210
Barisal	1720	1750	1780	210	215	220
Joshor	1730	1770	1810	225	230	235

VIII. RESULTS AND DISCUSSION

Firm supplies products from different production centers to customer's zone as well as shipped using transportation by trucks. Products manufactured in production centers are directly dispatched to customer zone, and the manufacturer has to pay transportation costs. The firm assigns trucks with respect to the capacities of truck options and transports the products from the production center to the customer zone.

Table 4. presents the transportation cost from production center to customer zone; here trucks are used to transport the products.

Table 4 : Data for Transportation cost of production center, i to customer zone, j

Production Center, i Customer Zone, j		1	2	3	4	5	6	7	8
		1	pes	900	1000	900	1000	1100	1100
	mos	1000	1200	1200	1200	1300	1250	1400	1250
	opt	800	1100	800	1100	1200	1000	1200	1200
2	pes	1100	1100	1000	1100	1000	1200	1000	1200
	mos	1200	1350	1100	1250	1400	1250	1300	1400
	opt	1150	1200	1200	1300	1200	1300	1200	1100
3	pes	1200	1200	1100	1100	1200	1400	1000	1500
	mos	1400	1400	1150	1300	1450	1100	1350	1600
	opt	1100	1100	1200	1200	1000	1200	1200	1400
4	pes	1400	1200	1000	1100	1200	1200	1300	1300
	mos	1500	1500	1200	1350	1500	1150	1400	1500
	opt	1300	1300	900	1200	1400	1000	1200	1200
5	pes	1200	1200	1000	1200	1300	1000	1000	1100
	mos	1350	1550	1300	1400	1500	1200	1500	1700
	opt	1100	1100	1200	1100	1400	1100	1300	1200
6	pes	1200	1400	1300	1200	1400	1200	1200	1300
	mos	1500	1600	1350	1450	1600	1250	1550	1750
	opt	1100	1350	1200	1100	1300	1300	1200	1200
7	pes	1400	1200	1500	1200	1400	1200	1100	1400
	mos	1600	1700	1400	1500	1250	1300	1600	1600
	opt	1300	1300	1300	1100	1500	1000	1200	1300
8	pes	1500	1400	1400	1300	1000	1000	1000	1200
	mos	1700	1750	1450	1600	1300	1350	1650	1550
	opt	1600	1500	1200	1400	1200	1200	1100	1300
9	pes	1500	1300	1000	1000	1200	1000	1200	1000
	mos	1650	1400	1500	1250	1350	1400	1400	1600
	opt	1400	1200	900	1200	1100	1200	1000	1200

Table 5. Presents the manufacturing cost of products in production center by triangular fuzzy method.

Table 5 : Manufacturing cost (ρ_i) at production center

Production centers, i	pes	mos	opt
1	10000	10500	11000
2	10500	12000	12500
3	11000	11500	10000
4	10000	12000	11000
5	11500	12500	13000
6	12000	11000	14000
7	11000	10000	15000
8	10500	11500	12000

Table 6. Represents the transportation cost of product from customer zone to collection center by using trucks.

Table 6 : Transportation cost from customer zone, j to collection center, k

Collection Center, k / Customer Zone, j		Collection Center, k								
		1	2	3	4	5	6	7	8	9
1	pes	650	800	900	650	700	650	600	700	800
	mos	800	900	1000	700	600	700	800	900	1000
	opt	700	700	800	600	800	600	700	600	900
2	pes	500	700	700	600	600	700	700	800	650
	mos	750	800	600	650	750	800	850	900	700
	opt	600	750	800	700	700	750	800	700	600
3	pes	700	700	600	700	600	700	600	750	750
	mos	800	600	700	900	1000	800	700	800	900
	opt	850	750	500	750	900	900	650	700	800
4	pes	900	1000	400	800	800	800	800	700	700
	mos	1000	1200	800	900	700	600	1000	800	900
	opt	800	900	500	850	850	900	900	600	800
5	pes	700	800	600	900	900	800	700	850	1000
	mos	800	900	700	650	600	700	800	900	950
	opt	600	750	750	950	800	900	900	950	800
6	pes	800	800	850	700	900	700	800	700	550
	mos	850	950	750	900	700	600	550	500	600
	opt	700	900	800	800	800	950	900	600	700
7	pes	750	800	900	700	900	700	800	700	550
	mos	800	900	950	900	700	600	550	500	600
	opt	700	700	800	800	800	950	900	600	700
8	pes	800	900	700	1000	750	1000	500	600	600
	mos	900	950	800	850	800	700	600	650	550
	opt	700	800	750	900	700	900	700	700	700
9	pes	600	700	1100	700	750	700	500	850	650
	mos	900	800	1000	800	800	800	600	900	700
	opt	500	600	900	600	650	600	550	800	600

Table 7. Represents the processing cost of per unit of used product at collection center in reverse supply chain networking.

Table 7 : Processing cost per unit of used product, ϕ_k

Collection center, k	pes	mos	opt
1	1000	1200	1100
2	800	700	1000
3	900	800	1200
4	1100	1000	900
5	800	700	1000
6	1100	800	1000
7	1000	900	1200
8	1100	800	1000
9	1000	900	1200

Table 8. Represents the transportation cost of product from collection center to glass recycling center by using trucks in reverse supply chain networking.

Table 8 : Transportation cost (b_{kl}) from collection center, k to glass recycling center, l

Glass recycling center, l collection center, k		1	2	3	4
		1	pes	500	300
1	mos	600	400	500	300
	opt	400	200	600	500
	2	pes	600	400	600
2	mos	700	750	650	600
	opt	650	500	700	300
	3	pes	450	600	700
3	mos	500	550	600	700
	opt	550	700	750	600
	4	pes	700	800	600
4	mos	650	700	800	700
	opt	600	900	700	600
	5	pes	500	800	700
5	mos	600	500	450	300
	opt	400	700	600	800
	6	pes	400	400	500
6	mos	450	550	650	750
	opt	300	500	550	600
	7	pes	500	600	900
7	mos	800	750	700	850
	opt	600	700	800	300
	8	pes	700	650	500
8	mos	900	600	300	400
	opt	800	700	600	300
	9	pes	400	700	500
9	mos	300	450	400	500
	opt	500	800	600	600

Table 9. Represents the production cost of per unit of used product at glass recycling center in reverse supply chain networking.

Table 9 : Production cost (β_l)

Glass recycling center, l	pes	mos	opt
1	500	600	900
2	800	900	700
3	700	450	400
4	600	650	500

Table 10. Represents the transportation cost of product from collection center to plastic recycling center by using trucks in reverse supply chain networking.

Table 10 : Transportation (h_{km}) from collection center, k to plastic recycling center, m

Plastic recycling center, m Collection Center, k		1	2	3	4
		1	pes	300	400
1	mos	400	300	450	500
	opt	500	500	500	300

2	pes	400	700	700	500
	mos	500	600	650	550
	opt	300	650	800	400
3	pes	350	700	900	500
	mos	700	650	700	600
	opt	500	800	800	400
4	pes	600	700	650	700
	mos	550	600	700	800
	opt	700	750	600	900
5	pes	600	500	500	600
	mos	400	300	450	550
	opt	550	600	550	700
6	pes	600	400	650	700
	mos	700	600	700	650
	opt	650	500	600	600
7	pes	750	450	700	500
	mos	700	650	500	450
	opt	800	700	650	400
8	pes	500	700	700	500
	mos	300	400	500	600
	opt	400	800	650	550
9	pes	500	700	600	600
	mos	700	800	750	650
	opt	600	650	700	700

Table 11. Represents the processing cost of per unit of used product at plastic recycling center in reverse supply chain networking.

Table 11 : Processing cost of plastic part (α_m)

<i>m</i>	pes	mos	opt
1	500	600	700
2	600	650	550
3	500	400	450
4	500	650	700

Table 12. Represents the environmental impact of shipping product from production center to customer zone, here environmental impact means the amount of carbon di oxide (CO₂) obtained from the trucks during transportation.

Table 12 : Environmental impact (e_{ij}^{tpc}) of shipping product from production center, *i* to customer zone, *j*

<i>i</i> \ <i>j</i>	1	2	3	4	5	6	7	8
1	30	32	34	30	32	36	38	40
2	42	35	36	38	39	40	42	45
3	46	47	48	39	40	46	47	48
4	50	52	42	46	47	48	49	50
5	52	53	54	55	46	48	50	52
6	54	32	34	36	38	40	42	45
7	46	48	50	52	54	46	48	50
8	42	46	40	38	35	45	46	48
9	44	48	38	36	32	40	48	46

Environmental impact per production of one unit of product, $ei^{pro} = 42$

$$\sum_i \sum_j (ei^{pro} + e_{ij}^{tpc}) = 6155$$

Table 13. Represents the environmental impact of shipping one unit of product from customer zone to collection center, here environmental impact means the amount of carbon di oxide (CO₂) obtained from the trucks during transportation.

Table 13 : Environmental impact of shipping one unit of product from customer zone, j to collection center, k

J \ k	1	2	3	4	5	6	7	8	9
1	24	26	28	30	39	32	36	38	40
2	26	28	30	32	34	36	38	40	38
3	32	36	38	44	32	24	28	30	32
4	34	34	40	42	34	32	30	28	34
5	30	28	32	36	34	35	28	30	32
6	36	32	38	40	36	26	32	48	38
7	38	34	36	38	38	32	36	46	36
8	36	36	34	36	36	44	38	44	32
9	40	38	32	36	40	42	40	42	34

Environmental impact of handling one unit of collected used product at collection center, $ei^{col} = 32$

$$\sum_j \sum_k (ei^{col} + e_{ij}^{tcc}) = 5416$$

Table 14. Represents the environmental impact of shipping glass part from collection center to glass recycling center, here environmental impact means the amount of carbon di oxide (CO₂) obtained from the trucks during transportation.

Table 14 : Environmental impact of shipping glass part from collection center, k to glass recycling center, l

k \ l	1	2	3	4
1	50	48	50	52
2	52	46	54	54
3	48	44	56	55
4	46	42	58	42
5	44	44	42	44
6	50	46	44	46
7	52	48	46	48
8	54	50	48	50
9	50	52	50	52

Environmental impact of recycling one unit of glass part, $ei^{src} = 40$

$$\sum_k \sum_l (ei^{src} + e_{kl}^{tcs}) = 3197$$

Table 15. Represents the environmental impact of shipping plastic part from collection center to plastic recycling center, here environmental impact means the amount of carbon di oxide (CO₂) obtained from the trucks during transportation.

Table 15 : Environmental impact of shipping plastic part from collection center, k to plastic recycling center, m

$m \backslash k$	1	2	3	4
1	16	18	20	22
2	24	18	22	24
3	26	20	18	16
4	28	18	22	18
5	30	28	18	18
6	32	26	20	20
7	34	24	16	22
8	32	22	20	24
9	18	20	18	18

Environmental impact of recycling one unit of plastic product, $ei^{prc} = 20$

$$\sum_k \sum_m (ei^{prc} + e_{km}^{tcp}) = 1510$$

Table 16. Represents the maximum capacity of glass and plastic recycling center in reverse supply chain networking.

Table 16 : Maximum capacity of glass (θ_m) and plastic (δ_l) recycling center

l, m	θ_m			δ_l		
	pes	mos	opt	pes	mos	opt
1	100	150	200	180	150	200
2	200	150	180	180	200	250
3	190	200	250	220	180	250
4	230	250	180	240	250	180

Simplifications of the constraints are obtained by developing a program using Code blocks programming software:

$$\min w_1 = 10175u_i + 15925q_k + 918900x_{ij} + 138675y_{jk} + 43925v_{kl} + 41375w_{km}$$

$$\min w_2 = 6155x_{ij} + 5416y_{jk} + 3197v_{kl} + 1510w_{km}$$

Constraints,

$$x_{ij} \geq 15012$$

$$y_{jk} \geq 10730.61$$

$$x_{ij} \leq 13860 \text{ or } x_{ij} \leq 0$$

$$y_{jk} \leq 18639 \text{ or } y_{jk} \leq 0$$

$$v_{kl} \leq 7281$$

$$w_{km} \leq 6736.5$$

Optimize this problem using LINDO 12 for this purpose use some symbol to put this equation in LINDO 12 more easily represent in table 17.

Table 17: Symbol transformation

Symbol	Modified Symbol
u_i	X
q_k	Y
x_{ij}	Z
y_{jk}	W
v_{kl}	M
w_{km}	N

Optimal solution for minimizing total cost (w_1):

Global optimal solution found.

Objective value: 0.1394333E+11

Infeasibilities: 0.000000

Total solver iterations: 0

Model Class: LP

Total variables: 6

Nonlinear variables: 0

Integer variables: 0

Total constraints: 5

Nonlinear constraints: 0

Total nonzeros: 10

Nonlinear nonzeros: 0

Variable	Value	Reduced Cost
X	0.000000	10175.00
Y	0.000000	15925.00
Z	15012.00	0.000000
W	10730.61	0.000000
M	0.000000	43925.00
N	0.000000	41375.00

Row	Slack or Surplus	Dual Price
1	0.1394333E+11	-1.000000
2	0.000000	-918900.0
3	0.000000	-13867.00
4	7281.000	0.000000
5	6736.500	0.000000

The above solution represent the minimization of total cost is 0.1394333E+11; here no iteration is required to get the optimal solution. The optimal solution is obtained for the proposed supply chain networking contains of variables of production centers (X) is 10175.00 that shows that if a new production center is opened than cost will increase otherwise reduced amount is 10175.00. The variables (Y) represent the collection center that is obtained 15925.00, that presents if a collection center is opened than cost will increase amount of 15925.00 otherwise reduced.

Variables (Z) show the quantity of product shipped from production centers (i) to customer zone (j) that is obtained 15012.00 units for the minimization of cost. Variables (W) shows the quantity of product shipped from customer zone (j) to collection center (k) that is obtained 10730.61 for the minimization of total cost. For the reverse flow variables (m) & (n) presents the quantity of used product shipped from collection center (k) to glass recycling center (l) & quantity of plastic part of used product shipped from collection center (k) to plastic recycling center (m) those are 43925.00 and

41375.00 reduced cost. Inequality constraint to transform it to equality slack and surplus values for the row 1,2,4,5 are 0.1394333E+11, 7281.000, 6736.500

and row 2 & 3 presents the transportation cost of production center (i) to customer zone (j) & customer zone (j) to collection center (k).

Optimal solution for minimizing environmental impact (w_2):

Global optimal solution found.

Objective value: 0.9239886E+08

Infeasibilities: 0.000000

Total solver iterations: 0

Model Class: LP

Total variables: 5

Nonlinear variables: 0

Integer variables: 0

Total constraints: 5

Nonlinear constraints: 0

Total nonzeros: 8

Nonlinear nonzeros: 0

Variable	Value	Reduced Cost
Z	15012.00	0.000000
Y	0.000000	5416.000
M	0.000000	3197.000
N	0.000000	1510.000
W	10730.61	0.000000
Row	Slack or Surplus	Dual Price
1	0.9239886E+08	-1.000000
2	0.000000	-6155.000
3	0.000000	0.000000
4	7281.000	0.000000
5	6736.500	0.000000

The above solution represent the minimization of total environmental impact here environmental impact minimization means the reduction of carbon di oxide (CO_2) during the transportation of product from production center (i) to customer zone (j) and customer zone (j) to location centers (k) finally location centers (l) to glass or plastic recycle center (l or m) through trucks. Here for the proposed supply chain networking problem only carbon di oxide (CO_2) is considered as an environmental impact others are neglected. The 2nd objective function shows the minimization of environmental impact that is 0.9239886E+08 as well as no iteration is required to get the optimal solution. Variables (Z) show the quantity of product shipped from production centers (i) to customer zone (j) that is obtained 15012.00 units for the minimization of environmental impact. The variables (Y) represent the collection center that is obtained reduced 5416.000. A variable (M) is the quantity of glass part shipped from collection center (k) to glass recycling center (l) than the reduced amount of 3197.000. A variable (N) is the

quantity of plastic part shipped from collection center (k) to plastic recycling center (m) than the reduced amount of 1510.000. A variable (W) is the quantity of used product shipped from customer zone (j) to collection center (k) amount of 10730.61. Inequality constraint to transform it to equality slack and surplus values for the row 1,4,5 are 0.9239886E+08, 7281.000, 6736.500 and dual prices are showing in row 1 & 2.

IX. CONCLUSION

Effective supply chain network design and optimization of the network are tasks that provide a competitive advantage to firms and organizations in today's highly intractable global business environment. In this study, design and optimization supply chain networking based on multi-objective fuzzy mathematical programming model, this consists of minimizing the total cost and environmental impact and determining the optimal physical shipment of product from production center to customer zone in forward flow and collection center to recycling center in reverse flow. The proposed

fuzzy model includes the design of the network configuration with a minimum total cost and environmental impact under the fuzzy capacity constraints with triangular and trapezoidal membership functions. The total cost involves the following: the transportation costs between production center and customer zone; customer zone to collection center and collection center to recycling center. To solve the proposed optimization model, an interactive fuzzy solution approach is developed based on the e-constraint method and the possibility programming approach proposed by Jimenez et al. [9]. The proposed hybrid solution approach is able to generate both balanced and unbalanced solutions and making a reasonable tradeoff between environmental and economic objectives. The effectiveness of the developed fuzzy optimization model as well as the usefulness of the proposed solution approach is investigated through a real industrial case. Finally, a sensitivity analysis developed to show the correlation between the objective function value and the constraints using LINDO 12 optimization software.

APPENDIX

The Jimenez et al. [9] method is based on the definition of the “expected interval” and the “expected value” of a fuzzy number. Assume that \check{C} is a triangular fuzzy number. The following equation can be defined as the membership function of \check{C} .

$$\mu_{\check{C}}(x) = \begin{cases} f_c(x) = \frac{x - c^{pes}}{c^{mos} - c^{pes}} & \text{if } c^{pes} \leq x \leq c^{mos} \\ g_c(x) = \frac{c^{opt} - x}{c^{opt} - c^{mos}} & \text{if } c^{mos} \leq x \leq c^{opt} \end{cases}$$

$$\mu_{\check{C}}(x) = \begin{cases} 1; & \text{if } x = c^{mos} \\ 0; & \text{if } x \leq c^{pes} \text{ or } x \geq c^{opt} \end{cases}$$

Here c^{mos} , c^{pes} and c^{opt} are the three prominent points (the most likely, the most pessimistic and the most optimistic values), respectively. Eqs. (13) And (14) define the expected interval (EI) and the expected value (EV) of triangular fuzzy number \check{C} .

$$EI(\check{C}) = [E_1^c, E_2^c] = \left[\int_0^1 f_c^{-1}(x) dx, \int_0^1 g_c^{-1}(x) dx \right] = \left[\frac{1}{2}(c^{pes} + c^{mos}), \frac{1}{2}(c^{mos} + c^{opt}) \right] \quad (13)$$

$$EV(\check{C}) = \frac{E_1^c + E_2^c}{2} = \frac{c^{pes} + 2c^{mos} + c^{opt}}{4} \quad (14)$$

According to the ranking method of Jimenez [10], for any pair of fuzzy numbers ‘a and b’, the degree in which a is bigger than b can be defined as follows.

$$\mu_m(a,b) = \begin{cases} 0; & \text{if } E_2^a - E_1^b \leq 0 \\ \frac{E_2^a - E_1^b}{E_2^a - E_1^b - (E_1^a - E_2^b)}; & \text{if } 0 \in [E_1^a - E_2^b, E_2^a - E_1^b] \\ 1; & \text{if } E_1^a - E_2^b > 0 \end{cases} \quad (15)$$

When $\mu_m(a,b) \geq \alpha$ it will be said that a is bigger than, or equal to, b at least in degree of α and it will be represented as $a \geq_{\alpha} b$. Now, consider the following fuzzy mathematical programming model in which all parameters are defined as triangular or trapezoidal fuzzy numbers.

$$\text{Min } z = \check{C}x$$

$$ST,$$

$$a_i x \geq b_i, \quad i = 0, 1, 2, \dots, l; \quad (16)$$

$$x \geq 0$$

Based on Jimenez et al. [9], a decision vector $x \in R^n$ is feasible in degree of α if $\min_{i=1,2,\dots,l} \{\mu_m(a_i x, b_i)\} = \alpha$. According to (16), equation $a_i x \geq b_i$ is equivalent to the following equation.

$$\frac{E_2^{a_i x} - E_1^{b_i}}{E_2^{a_i x} - E_1^{a_i x} + E_2^{b_i} - E_1^{b_i}} \geq \alpha \quad \text{iff } i = 1, 2, 3, \dots, l; \quad (17)$$

Eq. (17) can be rewritten as follows.

$$[(1 - \alpha)E_2^{a_i} + \alpha E_1^{a_i}]x \geq xE_2^{b_i} + (1 - \alpha)E_1^{b_i}, \quad i = 1, 2, 3, \dots, l; \quad (18)$$

Also, Jimenez et al. [9] showed that a feasible solution like x^0 is an acceptable optimal solution of the model (18) if and only if for all feasible decision vectors say x such that $a_i x \geq b_i, i = 1, 2, 3, \dots, l$; and $x \geq 0$; the following equation holds.

$$c^t x \geq \frac{1}{2} c^t x^0 \quad (19)$$

Therefore, with the objective of minimizing, x^0 is a better choice at least in degree 1/2 as opposed to the other feasible vectors. The above equation can be rewritten as follows.

$$\frac{E_2^t x + E_1^t x}{2} \geq \frac{E_2^t x^0 + E_1^t x^0}{2} \quad (20)$$

Finally, by the aid of the definition of expected interval and expected value of a fuzzy number, the

$$\begin{aligned} & \min EI(\check{C})x \\ & ST, \\ & [(1 - \alpha)E_2^{a_i} + \alpha E_1^{a_i}]x \geq \alpha E_2^{b_i} + (1 - \alpha)E_1^{b_i}, \quad i=1, 2, 3, \dots, l; \\ & X \geq 0 \end{aligned} \quad (21)$$

REFERENCES RÉFÉRENCES REFERENCIAS

1. H. Pirkul, V. Jayaraman, A multi-commodity, multi-plant, capacitated facility location problem: formulation and efficient heuristic solution, *Computers & Operations Research* 25 (10) (1998) 869–878.
2. M.A. Ilgin, M. Surendra, S.M. Gupta, Environmentally conscious manufacturing and product recovery (ECMPRO): a review of the state of the art, *J. Environ. Manage.* 91 (2010) 563–591.
3. C.H. Timpe, J. Kallrath, Optimal planning in large multi-site production networks, *European Journal of Operational Research* 126 (2) (2000) 422–435.
4. A. Cakravastia, I.S. Toha, N. Nakamura, A two-stage model for the design of supply chain networks, *International Journal of Production Economics* 80 (3) (2002) 231–248.
5. S. Talluri, R.C. Baker, A multi-phase mathematical programming approach for effective supply chain design, *European Journal of Operational Research* 141 (3) (2002) 544–558.
6. A. Syarif, Y.S. Yun, M.A. Gen, Study on multi-stage logistic chain network: a spanning tree-based genetic algorithm approach, *Computers & Industrial Engineering* 43 (2002) 299–314.
7. A. Sanayeia, S.F. Mousavib, M.R. Abdic, A. Mohagharb, An integrated group decision-making process for supplier selection and order allocation using multi-attribute utility theory and linear programming, *Journal of the Franklin Institute* 345 (2008) 731–747.
8. B. Javadi, M. Saidi-Mehrabad, A. Haji, I. Mahdavi, F. Jolai, N. Mahdavi-Amiri, No-wait flow shop scheduling using fuzzy multi-objective linear programming, *Journal of the Franklin Institute* 345 (2008) 452–467.
9. M. Jimenez, M. Arenas, A. Bilbao, M.V. Rodriguez, Linear programming with fuzzy parameters: An interactive method resolution, *Eur. J. Oper. Res.* 177 (2007) 1599–1609.
10. M. Jimenez, Ranking fuzzy numbers through the comparison of its expected intervals, *Int. J. Uncertain. Fuzziness Knowledge. Based Syst.* 4 (4) (1996) 379–388.
11. L. Meade, J. Sarkis, A. Presley, The theory and practice of reverse logistics, *Int. J. Logistics Syst. Manage.* 3 (2007) 56–84.
12. S.K. Srivastara, Green supply-chain management: a state-of-the-art literature review, *Int. J. Manage. Rev.* 9 (1) (2007) 53–80.
13. M.T. Melo, S. Nickel, F. Saldanha-da-Gama, Facility location and supply chain management – A review, *Eur. J. Oper. Res.* 196 (2009) 401–412.
14. A.I. Barros, R. Dekker, V. Scholten, A two-level network for recycling sand: A case study, *Eur. J. Oper. Res.* 110 (1998) 199–214.
15. V. Jayaraman, V.D.R. Guige Jr, R. Srivastava, A closed-loop logistics model for manufacturing, *J. Oper. Res. Soc.* 50 (1999) 497–508.
16. F. Du, G.W. Evans, A bi-objective reverse logistics network analysis for post-sale service, *Comput. Oper. Res.* 35 (2008) 2617–2634.
17. H.R. Krikke, A. Van Harten, P.C. Schuur, Reverse logistic network re-design for copiers, *OR Spektrum* 21 (1999) 381–409.
18. J.E. Lee, M. Gen, K.G. Rhee, Network model and optimization of reverse logistics by hybrid genetic algorithm, *Comput. Ind. Eng.* 56 (2009) 51–964.
19. N. Aras, D. Aksen, Locating collection centers for distance- and incentive-dependent returns, *Int. J. Prod. Econ.* 111 (2008) 316–333.
20. M.S. Pishvae, R.Z. Farahani, W. Dullaert, A memetic algorithm for bi-objective integrated forward/reverse logistics network design, *Comput. Oper. Res.* 37 (2010) 1100–1112.
21. H.J. Ko, G.W. Evans, A genetic-based heuristic for the dynamic integrated forward/reverse logistics network for 3PLs, *Comput. Oper. Res.* 34 (2007) 346–366.
22. M.S. Pishvae, F. Jolai, J. Razmi, A stochastic optimization model for integrated forward/reverse logistics network design, *J. Manufact. Syst.* 28 (2009) 107–114.
23. M. El-Sayed, N. Afia, A. El-Kharbotly, A stochastic model for forward_reverse logistics network design under risk, *Comput. Ind. Eng.* 58 (2010) 423–431.
24. M.S. Pishvae, S.A. Torabi, A possibilistic programming approach for closed-loop supply

- chain network design under uncertainty, *Fuzzy Sets Syst.* 161 (2010) 2668–2683.
25. H.F. Wang, H.W. Hsu, Resolution of an uncertain closed-loop logistics model: an application to fuzzy linear programs with risk analysis. *J. Environ.Manage.* (in press).
 26. Mir Saman Pishvaei, Jafar Razmi, Environmental supply chain network design using multi-objective fuzzy mathematical programming. *Applied Mathematical Modelling* 36 (2012) 3433–3446.
 27. S.A. Torabi, E. Hassini, An interactive possibilistic programming approach for multiple objective supply chain master planning, *Fuzzy Sets Syst.* 159 (2008) 193–214.
 28. C.L. Hwang, A. Masud, Multiple Objective Decision Making. Methods and Applications: A State of the Art Survey, *Lecture Notes in Economics and Mathematical Systems* 164, Springer-Verlag, Berlin (1979).
 29. G. Mavrotas, Effective implementation of the e-constraint method in multi-objective mathematical programming problems, *Appl. Math. Comput.* 213 (2009) 455–465.
 30. C.H. Timpe, J. Kallrath, Optimal planning in large multi-site production networks, *European Journal of Operational Research* 126 (2) (2000) 422–435.
 31. K.-M. Tsai, S.-Y. You, Y.-H. Lin, C.-H. Tsai, A fuzzy goal programming approach with priority for channel allocation problem in steel industry, *Expert Systems with Applications* 34 (2008) 1870–1876.
 32. J. Xu, Q. Liu, R. Wang, A class of multi-objective supply chain networks optimal model under random fuzzy environment and its application to the industry of Chinese liquor, *Information Sciences* 178 (2008) 2022–2043.
 33. H. Yan, Z. Yu, T.C.E. Cheng, A strategic model for supply chain design with logical constraints: formulation and solution, *Computers & Operations Research* 30 (14) (2003) 2135–2155.
 34. M. Kumar, P. Vrat, R. Shankar, A fuzzy programming approach for vendor selection problem in a supply chain, *International Journal of Production Economics* 101 (2) (2006) 273–285.

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