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On $(LCS)_n$ -Manifolds Satisfying Certain Conditions on D-Conformal Curvature Tensor

By Sunil Yadav & Praduman Kumar Dwivedi

Alwar Institute of Engineering & Technology, India

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Keywords : (LCS)_n - Manifold, D - conformal curvature tensor, Projective curvature tensor, Concircular curvature tensor.

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DN LCSN -MANIFOLDS SATISFYING CERTAIN CONDITIONS ON D-CONFORMAL CURVATURE TENSOR

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On (*LCS*)_n - Manifolds Satisfying Certain Conditions on D-Conformal Curvature Tensor

Sunil Yadav^a & Praduman Kumar Dwivedi^o

Abstract - In this paper we have characterized $(LCS)_n$ -manifolds with D -Conformal curvature tensor, concircular curvature tensor and projective curvature tensor.

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I. INTRODUCTION

An *n*-dimensional Lorentzian manifold *M* is smooth connected para contact Hausdorff manifold with Lorentzian metric *g*, i.e., *M* admits a smooth symmetric tensor field *g* of type (0,2) such that for each point $p \in M$, the tensor $g_p : T_pM \times T_pM \to \Re$ is a non degenerate inner product of signature (-,+,...,+) where T_pM denotes the tangent space of *M* at *p* and \Re is the real number space. A non-zero vector $v \in (T_pM)$ is said to be time like (res., non-space like, null, space like) if it satisfies $g_p(v,v) < 0$ (resp., $\leq 0, = 0, > 0$) (see [2]).

Definition1.1. In a Lorentzian manifold (M, g) a vector field *P* defined by

$$g(X, P) = A(X)$$

for any vector field $X \in \chi(M)$ is said to be concircular vector field if

$$(\nabla_X A)(Y) = \alpha \big[g(X,Y) + \omega(X) A(Y) \big]$$

where α is a non zero scalar function, A is a 1-form and ω is a closed 1-form.

Let M^n be a Lorentzian manifold admitting a unit time like concircular vector field ξ , called the characteristic vector field of the manifold. Then we have

$$g(\xi,\xi) = -1$$

Author a : Department of Applied Science & Humanities, Faculty of Mathematics, Alwar Institute of Engineering & Technology, M.I.A. Alwar -301030, Rajasthan India. E-mail : prof sky16@yahoo.com

Author o : Department of Applied Science & Humanities, Faculty of Mathematics, Institute of Engineering & Technology, M.I.A. Alwar - 301030, Rajasthan India. E-mal : drpkdwivedi@yahoo.co.in

Since ξ is the unit concircular vector field, there exist a non zero 1-form η such that

(1.2)
$$g(X,\xi) = \eta(X)$$

the equation (1.2) of the following form holds

(1.3)
$$(\nabla_X \eta)(Y) = \alpha [g(X,Y) + \eta(X)\eta(Y)] \ (\alpha \neq 0)$$

for all vector field X, Y, where ∇ denotes the operator of covariant differentiation with respect to Lorentzian metric g and α is a non zero scalar function satisfying

(1.4)
$$(\nabla_X \alpha) = (X \alpha) = \rho \eta(X),$$

where ρ being a scalar function. If we put

(1.5)
$$\phi X = \frac{1}{\alpha} \nabla_X \xi$$

then from (1.3) and (1.5), we have

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(1.6)
$$\phi^2 X = X + \eta(X)\xi,$$

from which it follows that ϕ is a symmetric (1,1) -tensor. Thus the Lorentzian manifold M^n together with unit time like concircular vector field ξ , its associate 1-form η and (1,1) -tensor field ϕ is said to be (*LCS*)*n* -manifold. Especially, if we take $\alpha = 1$, then the manifold becomes LP-Sasakian structure of Matsumoto (see [3]).

The *D*-conformal curvature tensor *B* (see [4]), projective curvature tensor *P*, concircular curvature tensor *C* (see [5]) on a Riemannian manifold (M^n, g) , (n > 4) are defined as

$$B(X,Y)Z = R(X,Y)Z + \frac{1}{n-3} \begin{bmatrix} S(X,Z)Y - S(Y,Z)X + g(X,Z)QY - g(Y,Z)QX - S(X,Z)\eta(Y)\xi \\ + S(Y,Z)\eta(X)\xi - \eta(X)\eta(Z)QY + \eta(Y)\eta(Z)QX \end{bmatrix}$$

(1.7)
$$-\frac{(k-2)}{(n-3)}\left\{g(X,Z)Y - g(Y,Z)X\right\} + \frac{k}{(n-3)}\left\{\begin{array}{l}g(X,Z)\eta(Y)\xi - g(Y,Z)\eta(X)\xi\\ +\eta(X)\eta(Z)Y - \eta(Y)\eta(Z)X\end{array}\right\}$$

(1.8)
$$P(X,Y)Z = R(X,Y)Z - \frac{1}{(n-1)} \left\{ S(Y,Z)X - S(X,Z)Y \right\}$$

(1.9)
$$C(X,Y)Z = R(X,Y)Z - \frac{r}{n(n-1)} \{g(Y,Z)X - g(X,Z)Y\}$$

respectively, where r is the scalar curvature, Q is the Ricci tensor and $k = \frac{(r+2)(n-1)}{(n-2)}$

Ref

 $[\mathbf{\omega}]$

Univ.Natur.Soci.12(1989),151-156.

II. Preliminaries

A differentiable manifold *M* of dimension *n* is called (*LCS*)*n*-manifold if it admits a (1,1) – tensor ϕ , a contravarient vector field ξ , a covariant vector field η and a Lorentzian metric *g* which satisfy the following.

(2.1) $\eta(\xi) = -1$ (2.2) $\phi^2 = I + \eta \otimes \xi$ (2.3) $g(\phi X, \phi Y) = g(X, Y) + \eta(X) \eta(Y)$ (2.4) $g(X, \xi) = \eta(X)$ (2.5) $\phi^{\xi} = 0, \quad \eta(\phi X) = 0$

for all $X, Y \in TM$. Also in a (LCS)*n* –manifold the following relations are satisfied (see[4]).

(2.6)
$$\eta(R(X,Y)Z) = (\alpha^2 - \rho)[g(Y,Z)\eta(X) - g(X,Z)\eta(Y)]$$

(2.7)
$$R(X,Y)\xi = (\alpha^2 - \rho)[\eta(Y)X - \eta(X)Y]$$

(2.8)
$$R(\xi, X)Y = (\alpha^2 - \rho)[g(X,Y)\xi - \eta(Y)X]$$

(2.9)
$$R(\xi, X)\xi = (\alpha^2 - \rho)[\eta(X)\xi + X]$$

(2.10)
$$(\nabla_X \phi)(Y) = \alpha \Big[g(X,Y)\xi + 2\eta(X)\eta(Y)\xi + \eta(Y)X \Big]$$

(2.11)
$$S(X,\xi) = (n-1)(\alpha^2 - \rho)\eta(X)$$

(2.12)
$$S(\phi X, \phi Y) = S(X, Y) + (n-1)(\alpha^2 - \rho)\eta(X)\eta(Y)$$

(2.13)
$$(X\rho) = d\rho(X) = \beta\eta(X)$$

Definition.2.1. A Lorentzian concircular structure manifold is said to be η -Einstein if the Ricci operator Q satisfies

$$Q = aId + b\eta \otimes \xi,$$

where a and b are smooth functions on the manifolds, In particular if b=0, then M is an Einstein manifold.

III. MAIN RESULTS

Theorem 3.1. There is no $(LCS)_n$ - manifold that satisfying B(X,Y)Z = 0. **Proof.** Assume that in a $(LCS)_n$ -manifold

$$B(X,Y)Z = 0.$$

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Then it is follows from (1.7) and (3.1) that

(3.2)

$$R(X,Y)Z = -\frac{1}{(n-3)} \begin{bmatrix} S(X,Z)Y - S(Y,Z)X + g(X,Z)QY - g(Y,Z)QX \\ -S(X,Z)\eta(Y)\xi + S(Y,Z)\eta(X)\xi - \eta(X)\eta(Z)QY \\ +\eta(Y)\eta(Z)QX \end{bmatrix} \\ +\frac{(k-2)}{(n-3)} \left\{ g(X,Z)Y - g(Y,Z)X \right\} - \frac{k}{(n-3)} \left\{ \begin{array}{l} g(X,Z)\eta(Y)\xi - g(Y,Z)\eta(X)\xi \\ +\eta(X)\eta(Z)Y - \eta(Y)\eta(Z)X \end{array} \right\}$$

It can also written as

(3.3)

$$g(R(X,Y)Z,U) = -\frac{1}{(n-3)} \begin{cases} S(X,Z)g(Y,U) - S(Y,Z)g(X,U) + g(X,Z)S(Y,U) \\ -g(Y,Z)S(X,U) - S(X,Z)\eta(Y)\eta(U) + S(Y,Z)\eta(X)\eta(U) \\ -\eta(X)\eta(Z)S(Y,U) + \eta(Y)\eta(Z)S(X,U) \\ +\frac{(k-2)}{(n-3)} \left\{ g(X,Z)g(Y,U) - g(Y,Z)g(X,U) \right\} \end{cases}$$

Notes

$$-\frac{k}{(n-3)} \begin{cases} g(X,Z)\eta(Y)\eta(U) - g(Y,Z)\eta(X)\eta(U) \\ +\eta(X)\eta(Z)g(Y,U) - \eta(Y)\eta(Z)g(X,U) \end{cases}$$

Taking $X = U = \xi$ in (3.3) and using (2.1) (2.4) and (2.11), it becomes

(3.4)
$$\left[\frac{(\rho - \alpha^2)(5n+3) + 2(k-1)}{(n-3)}\right] \left\{ g(Y,Z) + \eta(Y)\eta(Z) \right\} = 0$$

Then (3.4) implies that

(3.5)
$$g(Y,Z) + \eta(Y)\eta(Z) = 0.$$

From (3.5) and (2.3) it is seen that $g(\phi Y, \phi Z) = 0$, however, as this is not possible.

This proves the theorem 3.1.

Theorem3.2. A Ricci *D* -conformal semi-symmetric $(LCS)_n$ -manifold is an Einstein manifold with scalar curvature $r = 2n^2(\alpha^2 - \rho)$.

Proof. From (1.7) by virtue of (2.6) and (2.11), we obtain

(3.6)
$$\eta (B(X,Y)Z = \left[(\alpha^2 - \rho) + \frac{(k-2)}{(n-3)} \right] \{ g(Y,Z) \ \eta(X) - g(X,Z) \ \eta(Y) \}$$

From (3.6), it follows that

(3.7)
$$\eta(R(X,Y)\xi) = 0.$$

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and

Notes

(3.8)
$$\eta(B(\xi,Y)Z = \left[(\alpha^2 - \rho) + \frac{(k-2)}{(n-3)} \right] \left\{ -g(Y,Z) - \eta(Y) \ \eta(Z) \right\}$$

Assume that M^n is a Lorentzian concircular manifold satisfies the condition

(3.9) B(X,Y)S(Z,W) = 0.

From (3.9), it is obtained that

(3.10)
$$S(B(X,Y)Z,W) + S(Z,B(X,Y)W) = 0$$

Taking $X = W = \xi$ in (3.10) and using (3.6) (3.7) (3.8) and (2.11), we get

(3.11)
$$S(Y,Z) = 2n(\alpha^2 - \rho)g(Y,Z)$$

This proves the theorem 3.2.

Definition 3.1.A Riemannian manifold (M^n, g) is termed as Ricci *D* -conformal semi-symmetric if B(X,Y)S = 0.

Theorem3.3. There is no $(LCS)_n$ -manifold that satisfying R(X,Y)B = 0.

Proof. Assume that in a $(LCS)_n$ -manifold satisfies the conditions $R(\xi, Y)B = 0$, then it is expressed as

(3.12) R(X,Y) B(Z,V)W - B(R(X,Y)Z,V)W - B(Z,R(X,Y)V)W - B(Z,V)R(X,Y)W = 0

for all vector field X, Y, Z, V and W on M^n .

For $X = \xi$, it is follows from (2.8) and (3.12) that

$$(3.13) \qquad (\alpha^2 - \rho) \begin{bmatrix} B(Z,V,W,Y) - \eta(B(Z,V)W)\eta(Y) - g(Y,Z)\eta(B(\xi,V)W) + \eta(Z)\eta(B(Y,V)W) \\ -g(Y,V)\eta(B(Z,\xi)W) + \eta(V)\eta(B(Z,Y)W) - g(Y,W)\eta(B(Z,V)\xi) + \eta(W)\eta(B(Z,V)Y) \end{bmatrix} = 0$$

In fact Y = Z in (3.13) and by use of (3.6) (3.7) and (3.8) we have

(3.14)
$$(\alpha^2 - \rho) \left[B(Z,V,W,Y) - g(Z,Z) \eta(B(\xi,V)W) - g(Z,W)\eta(B(Z,V)\xi)W) + \eta(W)\eta(B(Z,V)Z) \right] = 0$$

From (3.14), by contracting we get

$$\left[\frac{-2(n-3)(\rho-\alpha^2)^2 - 2(\alpha^2 - \rho)(k-1)}{(n-3)}\right] \left\{g(V,W) + \eta(V)\eta(W)\right\} = 0$$

This implies that $g(V,W) = -\eta(V)\eta(W)$. Then from (2.3) we get $g(\phi V,\phi W) = 0$, however, as this is not possible. This proves the theorem 3.3.

Theorem3.4. A $(LCS)_n$ -manifold is projectively Ricci symmetric if and only if the manifold in an Einstein manifold.

Proof. Assume that in $(LCS)_n$ -manifold the condition $P(X,Y) \cdot S(Z,W) = 0$ are satisfies, and then it can be expressed as

Notes

(3.15)
$$S(P(X,Y)Z,W) + S(Z,P(X,Y)W = 0$$

From (1.8) and (2.11) we get

(3.16)
$$P(\xi, Y)Z = (\alpha^2 - \rho) \left[g(Y, Z)\xi - \eta(Z)Y \right] - \frac{1}{(n-1)} \left[S(Y, Z)\xi - (n-1)(\alpha^2 - \rho)\eta(Z)Y \right]$$

Taking $X = \xi$ in (3.15) by virtue of (2.11) and (3.16) we obtain

(3.17)
$$S(Y,Z) = (n-1)(\alpha^2 - \rho)g(Y,Z)$$

This proves the theorem 3.4.

Theorem3.5. A $(LCS)_n$ -manifold is concircurly Ricci symmetric if and only if either scalar curvature $r = n(n-1)(\alpha^2 - \rho)$ or the manifold in an Einstein manifold.

Proof. Assume that in $(LCS)_n$ -manifold satisfies the condition $C(X,Y) \cdot S(Z,W) = 0$, and then it can be expressed as

(3.18)
$$S(C(X,Y)Z,W) + S(Z,C(X,Y)W = 0$$

From (1.9) and (2.11), we have

(3.19)
$$C(\xi, Y)Z = \left[(\alpha^2 - \rho) - \frac{r}{n(n-1)} \right] \left\{ g(Y, Z)\xi - \eta(Z)Y \right\}$$

Taking $X = \xi$ in (3.18) by virtue of (3.19) and (2.11), we get

(3.20)
$$\left[(\alpha^2 - \rho) - \frac{r}{n(n-1)} \right] \{ S(Y, Z) - 2n(\alpha^2 - \rho)g(Y, Z) \} = 0$$

This implies that either $r = n(n-1)(\alpha^2 - \rho)$ or $S(Y, Z) = 2n(\alpha^2 - \rho)g(Y, Z)$

This proves the theorem 3.5

Theorem3.6.A $(LCS)_n$ -manifold satisfies the condition $P(\xi, X) \cdot S = 0$ if and only if the M^n is an Einstein manifold with scalar curvature $r = 2n^2 (\alpha^2 - \rho)$.

Proof. The condition $P(\xi, X) \cdot S = 0$ implies

(3.21)
$$S(P(\xi, X)Y, \xi) + S(Y, P(\xi, X)\xi = 0$$

By virtue of (2.8) and (2.11), equation (1.8) reduces that

(3.22)

$$S(P(\xi, X)Y, \xi) = -2n(\alpha^{2} - \rho)^{2} \{g(X,Y) + \eta(X)\eta(Y)\} + \frac{1}{(n-1)} 2n(\alpha^{2} - \rho) \{S(X,Y) + 2n(\alpha^{2} - \rho)\eta(X)\eta(Y)\}$$

and

 N_{ote}

(3.23)
$$S(P(\xi, X)\xi, \xi) = (\alpha^{2} - \rho)^{2} \left\{ S(X,Y) + 2n(\alpha^{2} - \rho)\eta(X)\eta(Y) \right\} - \frac{1}{(n-1)} 2n(\alpha^{2} - \rho) \left\{ S(X,Y) + 2n(\alpha^{2} - \rho)\eta(X)\eta(Y) \right\}$$

Using (3.22)(3.23) in (3.21), we get

$$S(X,Y) = 2n(\alpha^2 - \rho)g(X,Y)$$

This proves the theorem 3.6

Corollary1. In $(LCS)_n$ -manifold the *D*-conformal curvature tensor *B* satisfies

 $(3.24) \qquad \qquad B(X,Y)\xi = \lambda \{\eta(Y)X - \eta(X)Y\}$

where

$$\lambda = \frac{(n+1)(\rho - \alpha^2) + (k-1)}{(n-3)}$$

Proof. Using (2.7) and (2.11) in (1.7) we get (3.24).

Definition3.2. The rotational motion (curl) of D-conformal curvature tensor *B* on a Riemannian manifold is given by

(3.25)
$$Rot B = (\nabla_U B)(X, Y, Z) + (\nabla_X B)(U, Y, Z) + (\nabla_Y B)(U, X, Z) - (\nabla_Z B)(X, Y)U = 0$$

By virtue of second Bianchi identity

(3.26)
$$(\nabla_U B)(X,Y,Z) + (\nabla_X B)(Y,U,Z) + (\nabla_Y B)(U,X,Z) = 0$$

Equation (3.25) reduces to

Rot
$$B = -(\nabla_Z B)(X, Y)U$$

If the D-conformal curvature tensor is irrotational then $\operatorname{curl} B = 0$ and by (3.26), we have

$$(\nabla_Z B)(X,Y)U = 0$$

This implies that

(3.27)
$$\nabla_Z \{B(X,Y)U\} = B(\nabla_Z X,Y)U + B(X,\nabla_Z Y)U + B(X,Y)\nabla_Z U$$

In view of (3.27) with $U = \xi$ it is seen that

(3.28)
$$\nabla_Z \{ B(X,Y)\xi \} = B(\nabla_Z X,Y)\xi + B(X,\nabla_Z Y)\xi + B(X,Y)\nabla_Z \xi$$

Theorem.3.7. If the *D*- conformal curvature tensor in $(LCS)_n$ -manifold is irrotational then the *D* - conformal curvature tensor *B* is given by (3.30)

Notes

Proof. Using (3.24) and (1.5) in (3.28), we get

(3.29)
$$B(X,Y)\phi Z = \lambda \left[(\nabla_Z \eta)(Y) X - (\nabla_Z \eta)(X) Y \right]$$

Replacing Z by ϕZ in (3.29) by using (1.3) and (1.6) it is seen that

$$(3.30) \qquad B(X,Y)Z = \lambda \left\{ g(\phi Z,Y) X - g(\phi Z,X)Y - \eta(Y)\eta(Z)X + \eta(X)\eta(Z)Y \right\}$$

This proves the theorem 3.7.

Theorem3.8. If the *D* -conformal curvature tensor in $(LCS)_n$ -manifold is irrotational then the manifold is an η -Einstein manifold with scalar curvature

$$\tau = \left[\frac{n(n-3) + 2n\{(n-1)(\alpha^2 - \rho) - (k-2)\} - (n-1)(\alpha^2 - \rho)}{(n-1)}\right]$$

Proof. Using (3.21) in (1.7) the curvature tensor of B_{in} (LCS)_n -manifold is given by

$$R(X,Y)Z = \lambda \begin{bmatrix} g(Z,Y)X - g(Z,X)Y \\ -\eta(Y)\eta(Z)X + \eta(X)\eta(Z)Y \end{bmatrix} - \frac{1}{(n-3)} \begin{bmatrix} S(X,Z)Y - S(Y,Z)X + g(X,Z)QY \\ -g(Y,Z)QX - S(X,Z)\eta(Y)\xi \\ +S(Y,Z)\eta(X)\xi - \eta(X)\eta(Z)QY \\ +\eta(Y)\eta(Z)QX \end{bmatrix} \\ + \frac{(k-2)}{(n-3)} \left\{ g(X,Z)Y - g(Y,Z)X \right\} - \frac{k}{(n-3)} \left\{ g(X,Z)\eta(Y)\xi - g(Y,Z)\eta(X)\xi \\ +\eta(X)\eta(Z)Y - \eta(Y)\eta(Z)X \right\}$$

Let $X_{i, i} = 1, 2, 3, ..., n$ be an orthonormal basis of the tangent space at any point. Then the sum for $1 \le i \le n$ of the relation (3.31) with $Y = D = X_i$, yields

$$(3.32) \qquad \sum R(X,X_i)X_i = \lambda \Big[g(X_i,X_i)X - g(X,X_i)X_i \Big] - \frac{1}{(n-3)} \Big[\frac{S(X,X_i)X_i - S(X_i,X_i)X + g(X,X_i)QX_i}{-g(X_i,X_i)QX + S(X_i,X_i)\eta(X)\xi} + \frac{(k-2)}{(n-3)} \Big\{ g(X,X_i)X_i - g(X_i,X_i)X \Big\} + \frac{k}{(n-3)} \Big\{ g(X_i,X_i)(X)\xi \Big\}$$

The Ricci tensor *S* is given by

(3.33)
$$SX,Y) = \sum g(R(X,X_i)X_i,Y) + g(X,Y)$$

Taking inner product of (3.32) with Y and by virtue of (3.31) and (3.33), we get

$$(3.34) S(X,Y) = a g(X,Y) + b\eta(X)\eta(Y)$$

Notes

where

$$a = \left[\frac{(n-3)+2(n-1)(\alpha^2 - \rho) - 2(k-2)}{(n-1)}\right], \quad \text{and} \quad b = (\alpha^2 - \rho)$$

This implies that the manifold is an η -Einstein manifold.

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