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By Noboru Hokkyo

Senjikan Institute, Japan

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I. INTRODUCTION

Since the advent of quantum mechanics in the mid-1920s there have been continued interpretational controversies surrounding its counter-intuitive nature such as the wave-particle duality and the instantaneous collapse of the particle wave function at the detection point. But the paradox of nonlocal EPR¹ correlation between distant events without nonlocal interactions has been more problematic in recent times by Bell's experimental non locality test^{2,3} proposed in 1964, though the paradox was first noticed by Schrödinger⁴ and discussed in the dialogue between Einstein and Bohr⁵ at 1935 Solvay Council. In emphasis of the signal transmission in EPR correlation Cavalcanti and Wiseman⁶ asked: "What Bohr could have told Einstein at Solvay had he known about Bell experiments?" In his recollection in 1990 Bell⁷ wrote: "Suppose quantum mechanics were found to resist precise formulation. Suppose that when formulation beyond FAPP (For All Practical Purposes)⁸ is attempted, we find an unmovable finger obstinately pointing outside the subject...to the Mind of the Observer..., or only Gravitation?" We here show that the solution of quantum paradoxes can be found outside the EPR's reality criterion of local causality⁹ but within the framework of time-symmetric quantum electrodynamics for finite spacetime.¹⁰ A cosmological implication of the bi-directional signal transmission $P \leftrightarrow Q$ without common source S in the inflationary cosmology and a possible origin of dark energy are also discussed.

Author: Senjikan Institute, Niigata, Japan.
e-mail: noboruhok@yahoo.co.jp

II. EPR CORRELATION IN EPR LOOPHOLE

At the Solvay council EPR asked: "Are there spooky actions at a distance in quantum mechanics?" Recently, Yin et al.¹¹ led by Q. Zhang measured a superluminal speed of spooky actions between counter-propagating pair of photons emitted from an optically pumped atom in spin 0 state. During the measurement the locality and the freedom-of-choice loopholes of previous experiments were maximally closed by observing a 12-hour continuous violation of Bell's numerical expression (inequality) to EPR's reality criterion of local causality and separability of distant events. Let the spacetime positions of the photon source and the detection points be $S(x_S, t_S)$, $P(x_P, t_P)$ and $Q(x_Q, t_Q)$. Then the lower bound of the speed c_s of the spooky actions

$$c_s = |x_Q - x_P| / |t_Q - t_P| \quad (1)$$

can be superluminal as $|t_Q - t_P| \rightarrow 0$. Here we can see a local and causal link $P \leftarrow S \rightarrow Q$ ($t_S < t_P \approx t_Q$) and the nonlocal and a causal (spooky) link $P \rightarrow Q$ ($t_P < t_Q$). Let ϵ_P and ϵ_Q be the unit polarization vectors of photons measured at P and Q. The experiments verified the quantum expectations of the correlation function $C_{QM}(\epsilon_P, \epsilon_Q) = \epsilon_P \cdot \epsilon_Q = \cos \theta$, where θ is the Hilbert space angle between ϵ_P and ϵ_Q , and showed a clear rejection of classical theories obeying Bell's inequalities. The experiments also confirmed the insensitivity of C_{QM} to observer's delayed decision as to which direction to measure each photon's polarization at P and Q after the photon left the source at S—too late for a message to reach the opposite photon,⁸ making the causal link $P \leftarrow S \rightarrow Q$ improbable and the bi-directional link $P \leftrightarrow S \leftrightarrow Q$ probable in the loophole of EPR's reality criterion of local causality between P and Q.

III. EPR CORRELATION ON DOUBLE-LIGHT CONE

Dirac¹² defined the two-point correlation function or propagator $\Delta(x,t)$ between $S(0,0)$ and $P(x,t)$, and visualized the signal transmission $S \leftrightarrow P$ on the light cone with the origin S as vertex:

$$\begin{aligned} (\partial^2/c^2 \partial t^2 - \partial^2/\partial x^2) \Delta(x,t) &= 0, \\ \Delta(x,t) &= \alpha(t) \delta(c^2 t^2 - x^2) \\ &= [\delta(ct - x) - \delta(ct + x)] \end{aligned} \quad (2)$$

$$= \Delta_{\text{future}} - \Delta_{\text{past}} = \Delta_{\text{ret}} - \Delta_{\text{adv}}, \quad (3)$$

where $\alpha(t) = t/|t| = 1$ ($t > 0$); $= -1$ ($t < 0$). There an electron at $S(0, 0)$ moves under the retarded (causal) action Δ_{ret} of a charged particle at P on the past light cone $\delta(ct + x)$ of S as well as the advanced (retrocausal) action Δ_{adv} of a charged particle at Q on the future light cone $\delta(ct - x)$ of S , giving a divergence-free radiation damping of the electron at S . The bi-directional EPR link, $P(x_P, t_P) \leftrightarrow S(x_S, t_S) \leftrightarrow Q(x_Q, t_Q)$, can be visualized on the future light cone of the optically pumped metastable atom at $S(0, 0)$ by replacing the step function $\alpha(t)$ by the square (step-up and down) function $\beta(t) = 0$ ($t < t_S$); $= 1$ ($t_S < t < t_{P/Q}$); $= 1$ ($t > t_{P/Q}$)

$$\begin{aligned} & \Delta(|x_{P/Q} - x_S|, |t_{P/Q} - t_S|) \\ &= [\delta(c|t_{P/Q} - t_S| - |x_{P/Q} - x_S|) \\ & - \delta[(c|t_{P/Q} - t_S| - |x_{P/Q} - x_S|)/|x_{P/Q} - x_S|]]. \end{aligned} \quad (4)$$

The double-light cone¹³ [$\delta_{\text{ret}} - \delta_{\text{adv}}$] in Eq.(5) tells that the detection point P/Q on the left/right arms of the future light cone of S is reached by retarded wave $\exp(i\omega t - kt)$ from S while advanced wave $\exp(i\omega t + kx)$ from P/Q reaches S on the right/left arms of the past light cone of P/Q , forming a bi-directional sinusoidal wave, $\exp(i\omega t \pm kx)$, standing in phase between S and P/Q with nodes fixed in space at $x = n\pi/k$ ($n = \text{integer}$).

IV. BI-DIRECTIONAL MICROSCOPE

"Is the star (moon) there when nobody looks" asked Tetrode (Mermin).¹⁴ At the 1947 Solvay Council Heisenberg proposed a thought experiment measuring the electron position on microscope's object plane. There the photon wave collapsing at S in the retina of the observer entails the retrocollapse (appearance) of an electron at P scattering the photon to be observed at S . That is, the electron is not at P when nobody looks. at S . This point was emphasized by Weizsäcker¹⁵ in his delayed-choice thought experiment measuring the transverse photon momentum on the focal plane of Heisenberg's microscope. If the microscope is very long, the observer at S can make choice as to which property of the electron, position or momentum, to measure after the scattering process has taken place at P . To see the bi-directional signal transmission $S \leftrightarrow P$ in microscope we write Eq.(4) in momentum space¹⁴

$$\begin{aligned} & \Delta_{\omega,k}(|x_P - x_S|, |t_P - t_S|) \\ &= [\exp(ik|t_P - t_S|) \text{sink}|x_P - x_S|/|k|], \end{aligned} \quad (5)$$

getting an uncertainty relation between photon momentum $p = \hbar k$ and the microscope length

$$p|x_P - x_S| = nh/2, \quad (6)$$

where n is the number of nodes of the sinusoidal wave standing between S and P .

V. COSMOLOGICAL EPR CORRELATION

In an attempt to resolve EPR problem Dirac^{17,18} revived early ideas of aether transmitting light signal between distant points separated by spacelike distance, but was rejected by Einstein as it could not be fitted in his 4-dimensional formulation of relativity. Dirac¹⁸ further proposed a bi-directional EPR connection between points P and Q located on the 4-dimensional hyperboloid $(ct)^2 - r^2 = l_{\text{pl}}^2$ crossing the light cone at $ct = l_{\text{pl}}$ at $r = 0$ with spacelike velocity:

$$dr/dt = ct/r = c(1 + l_{\text{pl}}^2/r^2)^{1/2}, \quad (7)$$

defining 3-dimensional Lorenz sphere $r^2 = l_{\text{pl}}^2$. We can likewise embed the Lorenz sphere into the radial line element ds of de Sitter universe in Reissner-Nordstroem form:²⁰

$$\begin{aligned} ds^2 &= c^2 g_{tt} dt^2 - g_{rr} dr^2, \\ g_{tt} &= g_{rr}^{-1} = (1 - \Lambda c^2/r^2 + l_{\text{pl}}^2/r^2)^{-1/2}, \end{aligned} \quad (8)$$

where Λ is the cosmological constant. Putting $ds^2 = 0$, we get light velocity:

$$dr/dt = cg_{tt}/g_{rr} = c(1 - \Lambda r^2/c^2 + l_{\text{pl}}^2/r^2). \quad (9)$$

We find that dr/dt is space like at $r \sim l_{\text{pl}}$ but decreases towards $dr/dt = c$ at $r = (cl_{\text{pl}})^{1/2} \Lambda^{1/4} \sim 10^{12} \Lambda^{1/4}$ cm. From there dr/dt continues to decrease towards $dr/dt = c$, but rises again to space like velocity at the cosmological horizon $r = c\Lambda^{-1/2}$ after a brief interlude of subluminal period.

Hawking¹⁹ proposed a cyclic Lorenz-de Sitter model where an expanding and contracting universe starts and ends on the 4-dimensional Lorenz sphere $\tau^2 + r^2 = l_{\text{pl}}^2$ with imaginary time $\tau = it$. There the Hubble expansion $\sim \exp Ht$ is replaced by a cosmological wave function of radius $\sim \exp iH\tau \sim \exp i\Lambda\tau$, determining the temperature $T \sim H$, entropy $S \sim \Lambda^{-2}$ and the energy of radiation $E \sim \hbar c/R$ created by the de Sitter black hole capturing negative energy components of Zittering electrons²⁰ at temperature T .

In high dimensional string theory,²¹ the parallel orbifold branes collide periodically in cycle, expanding and contracting with dark energy Λ .

VI. MASS DEFECT OF SEMICLOSED FRIEDMAN UNIVERSE

The idea of semiclosed Friedman universe was proposed by Zel'dovich and others²¹ in 1970s as a possible model of quasistellar radio sources evolving from and joined-on to preexisting asymptotically flat space. The expansion history of the semiclosed universe is dictated by the Hubble constant $H = 8\pi G/\rho_\Lambda$ and the dimensionless density parameter $\Omega_\Lambda = \rho_\Lambda/\rho_{c\Lambda}$ where ρ_Λ is the energy density and $\rho_{c\Lambda}$ the critical density.

For $0 < \Omega_\Lambda < 0.5$ the expanding universe in lower hemisphere is joined onto asymptotically flat outer space through Schwarzschild throat; for $0.5 < \Omega_\Lambda < 1$ the contracting upper hemisphere is joined onto outer space through double-valued Schwarzschild bottleneck; for $\Omega_\Lambda \sim 1$ the almost closed universe is joined onto asymptotically flat space extending to infinity through Planck scale throat. For an observer comoving with cosmological expansion and contraction history of semiclosed Friedman universe can be described by the radial line element ds of the universe in Reissner-Nordstrom form:

$$ds^2 = c^2 g_{tt} dt^2 - g_{rr} dr^2, \\ g_{tt} = g_{rr}^{-1} = (1 - r^2/r_g^2 + l_{pl}^2/r^2)^{1/2}, \quad (10)$$

where $r_g = 3c^2/8\pi G\rho_\Lambda$. The light velocity $dr/dt = c(1 - \Lambda r^2/c^2 + l_{pl}^2/r^2)$ is space like at $r \sim l_{pl}$. As r increases from $r = l_{pl}$, dr/dt decreases towards c at $r = (r_g l_{pl})^{1/2} \sim 10^{28} \text{cm}$ for $r_g \sim 10^{28} \text{cm}$, to be compared with the radius of causally related small region $\sim 10 \text{cm}$ in inflationary model. With further increase of r towards horizon $r = r_g$, dr/dt reaches spacelike velocity $r = r_g$ after a long interlude of subluminal period: $l_{pl} \ll r \ll r_g$. In this period a detailed description of the semiclosed Friedman universe can be given by using the integral $\int dx (1 - r^2/r_g^2)^{1/2} = \sin^{-1} x$ to calculate the proper mass M_p and volume V_p of the universe:

$$M_p = \rho_\Lambda V_p = 2\pi\rho_\Lambda \int_0^{r_g} r^2 g_{rr} dr = (3/2)(R/r_g)^3 [\sin^{-1}(R/r_g) - (R/r_g)(1 - (R^2/r_g^2)^{1/2})] M, \quad (11)$$

where $M = (4\pi R^3/3)\rho_\Lambda = \rho_\Lambda V$ is the Newtonian mass and volume V . Eq.(11) tells that the proper radius $R_p = \int_0^R g_{rr} r dr$ and volume $V_p = (4\pi R_p^3/3)$ increases with the increase of the world radius from $r \sim 0$, where $\sin^{-1}(R/r_g) \sim 0$, until V_p fills the half of the closed universe (lower hemisphere) of the closed Friedman universe, where $\sin^{-1}(l_{pl}/r_g) = \pi/2$. With further increase of r , R_p decreases towards $R_p \sim l_{pl}$, where $\sin^{-1}(l_{pl}/r_g) \sim \pi$, forming a gravitational semiclosure with $V_p \sim M_p \sim 0$ (with upper hemisphere) having Planck surface l_{pl}^2 and mass m_{pl} , creating Planck scale black holes liberating dark energy $E \sim \hbar c/l_{pl}$ or recreating a black Lorenz sphere outside the gravitational radius $R = r_g$, liberating dark energy $E \sim \hbar c/R$ with information content $(R/l_{pl})^2$ in asymptotically flat outer space.²²

VII. SOURCE OF DARK ENERGY

We note that the negative equation of state $\rho_\Lambda + p_\Lambda c^2 < 0$ required by the dark energy is satisfied in the upper hemisphere of the semiclosed Friedman universe. There the density of gravitationally bound pairs of quantized metric fluctuations, or gravitational Bohr atoms, dominate by creating negative attractive potential $Gm_{pl}^2/l_{pl} = \hbar c/l_{pl} = m_{pl}c^2$ capturing positive rest mass energy $m_{pl}c^2$ of single metric fluctuation, or Planckeons. In the lower hemisphere, where the

positive equation of state $\rho_\Lambda + p c^2 > 0$ is satisfied, the free Planckeons prevails. The evolutionarily earlier upper hemisphere is characterized by the density parameter $0.5 < \Omega_\Lambda = (R/r_g)^2 = 1$ and the less earlier lower hemisphere by $0 < \Omega_m < 0.5$. The recently updated density parameters²³ fall into these ranges: $\Omega_\Lambda \sim 0.685$ and $\Omega_m \sim 0.266$. Adding the evolutionarily recent atomic matter $\Omega_{\text{atom}} \sim 0.049$, we have $\Omega_{\text{tot}} = \Omega_\Lambda + \Omega_m + \Omega_{\text{atom}} = 0.965 \sim 1$ indicating the asymptotic flatness of the extragalactic space required for the asymptotic solutions of Einstein equations to be found useful.

VIII. CONCLUSION

We have shown that the quantum paradox of EPR correlation between distant points P and Q sharing a common source S arises outside EPR's reality criterion of local causality, and can be solved within the framework of time-symmetric and relativistic quantum electrodynamics for finite spacetime¹⁰ with singular boundary conditions allowing the bi-directional signal transmission $P \leftrightarrow S \leftrightarrow Q$ on the double-light cone where the future and the past cones share a common light path connecting S and P/Q. A cosmological implication of the bi-directional and superluminal signal transmission $P \leftrightarrow Q$ without a common source S in explaining the observed homogeneity of the universe and the possible Planckeon origin of dark energy in the upper hemisphere of the semiclosed Friedman universe, joined onto an asymptotically flat space, are also discussed to explain the asymptotic flatness of the extragalactic space. In conclusion Planckeon origin of dark energy in the upper hemisphere of the semiclosed Friedman universe is proposed.

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