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Neotheory of Continuous Mediums Thermomechanics

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The required field functions are reduced fundamental substances: mass, amount of movement, increment of internal energy, moment of the local momentum - all for absolute of motion in inertial systems of counting.

The practical significance of the theory under development is underlined.

Some easy accesses examples of calculations in simplified formulation are given.

The theme and content of the work are such that it should be considered in the discussion plan.

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I. INTRODUCTION

Multifunctional servers, impressive levels of speed and RAM of modern computer equipment, as well as prospects for their further development, along with the continuous improvement of methods, tools and technologies for precision physical experiments, contributing to the formation of moderate but sustained optimism with the statement of the possibilities in the not too distant future, to solve scientific and technical problems of almost any degree of complexity.

This class of tasks includes, in particular, creative design solutions and in-depth studies of thermomechanical processes in different artifact and natural systems in all their diversity. The expected initial measures, including both ensuring the highest qualities with dynamic stability of their creation, and the achievement of guaranteed extreme thermomechanical indicators of the executive bodies of power devices corresponding to objects in a wide range of deviations from the nominal condition.

A rational way of possible satisfaction of the marked majorant estimates of the effective qualities of

the research is to attract the most perfect spatialtemporal, i.e. four-dimensional *3Dt* (or *4D*), statements in the description of movements and transformations of working fluids that are in different aggregative states.

We believe that the 3Dt physical and mathematical model of non-equilibrium thermomechanics of solid, liquid and gaseous continuous media presented below and developed from unified installations will prove to be directly demanded over time in a phased advance to the previously noted objectives.

An additional application of the following concept, which is quite significant at the current time, consists of the following. The desired, most competitive results in the subject area of research considered here can, to a certain extent and, of course, at the level of predictions, be achieved by attracting / borrowing readymade software products of simulation computer reproduction of the discussed phenomena based on traditional physical and mathematical models of their description. This approach, widely used today, implies the ability of the user to *competently* form preferences when comparing different versions of such computer services. In this regard, one of the determining reasons, which led the author to this publication, was also a opinion that familiarization with reinforced the foundations of the proposed alternative theory would help the developer of innovative objects and systems of various applications, which is a consumer of existing thermomechanical calculation programs, find it easier to navigate in the ever-increasing list relevant proposals and implement the most favorable of them.

An extended understanding of the essence of the developed scientific product and the details of individual transformations, including designations, are presented in the author's previous works on this topic (see references). We hope that the interested specialist, taking into account the singular complexity of the subject of study, will condescendingly refer to individual points of our previous works, which subsequently required a certain clarifying correction and a demanded generalization of the initially obtained relations.

The undertaken research, the main results of which in a compact form are set forth below, seems to be consistent, but at the same time it essentially goes beyond the framework of well-established ideas about the physical and mathematical description of continuous dynamics, including fluids, media (C-mediums and F-

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mediums enumeration). Further concretization of the present unified, abstractly independent of the type of aggregative state of the environment, the formalism requires large-scale and, as a rule, precision field experiments to verify the group of additional *physical* coefficients included in the proposed paradigm.

The statements of the corresponding initialboundary-value problems turn out to be fundamentally incorrect, especially for F-mediums under turbulent flow regimes, and involving the introduction of certain agreements in the concept of a generalized solution of such problems using, inter alia, and possibly the *ergodic hypothesis* of statistical physics [1, 4].

Note that thermomechanical processes are considered primarily in the framework of the installations adopted in [1], which is assumed *to be known*.

Direct numerical implementation of the developed model, without truncations, filtering and subgrid approximations, even for the simplest canonical areas of medium movement, will be possible only with the help of hyper computer engineering.

These difficulties are significant, but the intellectual and material costs required to overcome them are justified by the undeniable imperative to further improve the methods of analysis and synthesis of the super-complex, but ubiquitous systems considered here.

Let us dwell on the following preliminary, but fundamentally significant circumstances.

- The prevailing part of the limitations specified in the main section of the article, or the complementarity violations in the usual models of C- mediums dynamics, for many years seemed to the author as an unnatural reality. Almost three centuries of invaluable scientific and practical experience in the study of C- mediums thermomechanics predetermined the manifestation of a kind of "*inhibition syndrome*" in the final decision to popularize the concept presented below.
- The outlined paradigm, eliminating (to put it mildly

 in many ways) existing antinomies, in relation to
 modeling the functions of external surface action
 (see the left parts of equations (I) (IV) in the
 second column of the table) remains
 fundamentally phenomenological. Therefore, its
 further and thorough theoretical and experimental
 approbation is required.
- The text should strictly distinguish between the subtle designations of the coordinates $x_k(t), k = \overline{1,3}$ and the *only* absolute argument, namely, time *t*, the motion of the *labeled* elementary medium particle (*e.m.p.*) for the tracking / trajectory / Lagrangian frame of reference: *L-systems*, in the *right-hand* sides of

equations (I) - (IV) and denoted in the *left-hand* parts of these equations (see lower) by *thickened* font of the notation for the coordinates \mathbf{x}_k and time t of the rigid / Eulerian reference system, then the *E-system*, for establishing *3Dt* distributions of action functions with *four* independent arguments. Thus, in the *L-system* $\vec{x}(t)$ there is the current position of the point belonging to the labeled particle of the medium, and in the *E-system* the radius vector $\vec{\mathbf{x}}$ - is the point marker of the timeless *3D* space. Prototypes of labeled *e.m.p.* are passing relatively of such points discretely distributed on the regular net of *E-system* of space. It is clear that at each *fixed* point in time these vectors coincide $\vec{x}|_t = \vec{\mathbf{x}}$.

- Coordinate systems $(t, \vec{x}(t))$ and (t, \vec{x}) are considered as absolute, inertial and with the united chiefly fixed origin of the counting.
- It is easy to see that the classical foundations of the C-mediums science sections "Continuous kinematics" and "Basic equations of the dynamics of an ideal incompressible fluid" (Euler, Bernoulli) are naturally preserved if for the first section the corresponding distributions of field functions are considered in the *E*-system \vec{x} each "frozen" time point *t*, or at each *abstract* point \vec{x} with variable *t*, and for the second section in $L\Lambda E$ reference systems.
- The desired functions of the substance-field are substances $\rho, \vec{v}, \varepsilon, \vec{\Lambda}$ (see explanations below).

II. Main Part

For a clearer justification of the dependencies described below, in Fig.1a,b the topological properties of the $L \wedge E$ - systems are shown conditionally and separately, and in Fig.1c, when they are combined.



Fig. 1: Schematic representations of $L \wedge E$ - systems: a, b– separate; c - combined

The shaded arrows in Fig.1a, departing from the arrow of time *t* and ending on the axes of the tracking / Lagrangian frame of reference, emphasize figuratively the dependence of the Cartesian coordinates of each physical point (PP, see below) of the medium on this absolute argument. As before [1], PP means the smallest material formation, for which the *continuity* hypotheses and *non-equilibrium* thermodynamics processes is still valid.

Externally similar coordinate system in Fig.1b is timeless in space with four, as previously indicated, independent arguments. It also shows a simply connected, otherwise *arbitrary*, but fixed in 3D small macrovolume $\overline{\mathbf{v}}$ with boundary \mathbf{s} and orth of the external normal to it \vec{n} , filled with a single-phase moving medium. At the same time $\overline{\mathbf{v}} \in \overline{\mathbf{V}}$, with the norm $\|\overline{\mathbf{v}}\| << \|\overline{\mathbf{V}}\|$, where $\overline{\mathbf{V}}$ - is the closed calculated macro-region of studying the motion of the C-medium. Inside \mathbf{v} for a given time instant t, the instantaneous position of a labeled elementary particle with a focus c and a some virtual point in it $\mathbf{b} \in \overline{\mathbf{v}}$ is highlighted. Two darkened silhouette arrows show and identify external volumetric and surface actions on $\overline{\mathbf{v}} = \mathbf{v} \cup \mathbf{s}$ of different physical nature.

In Fig.1c additionally depicts a fragment of the trajectory of the focus c of the *pre-images* of the past (the upper part of the trajectory) and the future (lower part of the trajectory) of the labeled particle. Strictly speaking, the point b introduced here are possible / virtual PP of the selected medium particle and in the final dynamic equations, with the exception of the right side of equation (IV) (see below), their specific positions are *leveled*. We shall indicate also that under consideration systems of counting *are inertial, homogeneous and isotropy* by space and time and, as it follows from Fig. 1, with *common and fixed* the origin of coordinates. In addition studied C-mediums in general are *dissipated* and *inhomogeneous* as well as *non-isotropy* by space and time.

Now, giving preference to the compressed style of presentation of the material, we proceed as follows. We introduce a table consisting of two columns. In the left column we place the well-known and characteristic closed system of equations of the dynamics of the Cmedium (It) - (IVt), (1t) - (3t), which, in particular, for Fmediums is described in [5]. At the bottom of this column we list the undeniable antinomies and limitations of this system.

In the second - right column we place the innovative system of fundamental equations of C – mediums (I) - (IV) with extremely concise detail (1) - (6), (A), (B), (C) of separate fragments of the fundamental equations indicated by Roman in numbers. Next will follow the necessary explanations, comments and conclusions from the range of issues under consideration. The descriptions of random / pseudo-random exposures and, in general, aspects of setting initial-boundary conditions are omitted here. Variants of the formalization of these factors are described in our works [3, 7], mainly in the aspect of pro-domains.

So, taking into account the presence in the future text of an explanation of the notation (see also the list of notation in the forerunner work [1]), we have the following.

Table: Fundamental and private laws/equations of the continuous mediums of thermomechanics (without regard of random perturbations and boundary conditions on the whole).

Traditional	Alternative
\leftarrow <i>E</i> -system \rightarrow	<i>E</i> - system $\leftarrow \mid \rightarrow L$ - system : $\begin{bmatrix} cause \\ action \end{bmatrix} \xrightarrow{<} \begin{bmatrix} effect \\ consequencee \end{bmatrix}$
$-\rho \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \vec{v} = \frac{d\rho}{d t} (\text{It})$	$-\vec{\nabla}_{\vec{\mathbf{x}}}\cdot\vec{v} = \frac{d\ln\rho}{dt} $ (I)
$\rho \vec{F} + \vec{\nabla}_{\vec{x}} \cdot \mathbf{P} = \rho \frac{d\vec{v}}{d t} (\text{IIt})$	$\rho \vec{F} + \vec{\nabla}_{\vec{x}} \cdot \Pi = \frac{d\rho \vec{v}}{dt}, (II)$ ubi $\Pi = \mathbf{P}^{(s)} + \mathbf{P}^{(a)}, \mathbf{P}^{(s)} = \mathbf{P}_s + \mathbf{P}_d \text{ et } \Pi_d = \mathbf{P}_d + \mathbf{P}^{(a)}$
$\mathbf{P} \cdot \cdot \dot{\mathbf{S}} + \rho q_{cd} = \rho \frac{d\varepsilon}{d \mathbf{t}} $ (IIIt)	$\Pi \cdot \left(\vec{\nabla}_{\vec{\mathbf{x}}} \vec{v}\right) + \mathfrak{M}_{p} + \rho q_{cd} + \rho q_{r} = \frac{d\rho\varepsilon}{dt} \qquad (III)$ $\mathfrak{M}_{p} = \left(\left(\vec{\nabla}_{\vec{\mathbf{x}}} \vec{u}_{d}\right)^{*} \times \Pi\right) \cdot \vec{\Lambda} + \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \left(M^{(a)} \cdot \vec{\Lambda}\right)$
$\mathbf{P} = \mathbf{P}^* = -p\mathbf{I} + (IVt) + (2\mu\dot{\mathbf{S}}_d \lor 2G\mathbf{S}_d)$	$(\vec{\nabla}_{\vec{\mathbf{x}}}\vec{u}_{d})^{*} \times \Pi + \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{M}^{(a)} = \frac{d\vec{J} \cdot \vec{\Lambda}}{dt}, (IV)$ $\boldsymbol{J} = c_{J} \approx \int_{J}^{-2} \rho, c_{J} \text{ and } \approx_{J} \text{see below notations }.$
Joule: $\varepsilon = \varepsilon_0 + \int_{T_0}^T c_V(T) dT^{(1t)}$	Inversions (1 t) (see also [2]): $T = T_0 + \int_{\varepsilon_0}^{\varepsilon} \beta_{\rho}(\rho, \varepsilon; \mu_{\beta}) d\varepsilon, T_0 \ge T_{\text{inf}}, \beta_{\rho} = c_V^{-1} (1)$ $\mu_{\beta} : \frac{\partial}{\partial \rho} \left(\mu_{\beta} \frac{\partial \beta_{\rho} _e}{\partial \varepsilon} \right) = \frac{\partial}{\partial \varepsilon} \left(\mu_{\beta} \frac{\partial \beta_{\rho} _e}{\partial \rho} \right),$ $ _e - \text{obtained under } e\text{-conditions}$
Clapeyron: $\mathbf{F}(ho,p,T)=0$ (2t)	Strong form of Generalization (2 t) (see also [2]): $\mathbf{P}_{s} = -\left\{p_{0} + \int_{\overset{L}{L}\rho_{0},\overset{L}{L}\varepsilon_{0}}^{\overset{L}{L}\rho} \mu_{b}\left[\mathbf{\overline{\kappa(t)}}\overline{B}\right]_{\varepsilon} d\overset{t}{L}\rho + \mathbf{\overline{\kappa(t)}}\overline{B}\right]_{\rho} d\overset{t}{L}\varepsilon\right\} \mathbf{I}, (2)$ $L = \ln, \dot{L} = \partial \ln/\partial t. \ddot{L} = \partial^{2} \ln/\partial t^{2} \ni t = \emptyset, \bullet, \bullet \bullet$
Fourier: $ \rho q_{cd} = -\rho \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \vec{q}_{cd}, $	Stress deviator \mathbf{P}_{d} approximation $\mathbf{P}_{d} = \mathbf{P}_{d0} + 2 \overset{i}{G}(\rho, \varepsilon) \int_{\mathbf{S}_{d0}}^{\mathbf{S}_{d}} \overline{\mathbf{K}(t) \cdot d\mathbf{S}}_{d}, \qquad (3)$ $\overset{i}{G} = \overset{i}{G}_{0} + \int_{\dot{D}\rho_{0}, \dot{D}\varepsilon_{0}}^{\dot{D}\rho} \overset{i}{\mu}_{g} \left[\frac{\partial G}{\partial D\rho} dD\rho + \frac{\partial G}{\partial D\varepsilon} dD\varepsilon \right],$ $D = 1, \dot{D} = \partial/\partial \mathbf{t}, \ddot{D} = \partial^{2}/\partial \mathbf{t}^{2}, \text{see also [2]}$



CRITERION OF THE COLLAPSE-PASSAGE

$$\vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{U}_{d} = \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{U} = \int_{0}^{t} (\int_{0}^{\leftarrow t} \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{a} \partial \tau) \partial \tau$$

$$I = \vec{u}_{d} \cdot |\vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{U}|$$

$$I^{*} = (|\vec{u}_{d} \cdot | \approx_{s.sup})^{*}, \quad si \quad I > I^{*} \quad eo \quad \mathbf{K}^{2} < 3, \quad \mathbf{K}^{t} < 1$$
(C)

For integrated expressions in formulas (2), (3),
 (A) the upper central index is summarized *ι*=Ø,●,●.
 Here are some comments to the information in

these two columns of the table. In the upper part of the left column of the table, the balance equations are written for specific mass ρ (lt), momentum \vec{V} (llt), increments of internal energy ε (llt). The balance equation of the moment of momentum (IVt) in the accepted here representation of the *radius vector* of the action of the moments of external forces and inertia forces in the *E-system*, namely in the form \vec{x} [5] (and not in the *L-system*, that is, in the form as $\vec{x}(t)$, since these moments are actually applied to the particle of the medium, and not to the abstract point of a rigid 3D space), it reduces to the condition of symmetry of the stress tensor **P** (see the first equality in the graph (IVm); the upper asterisk is a transposition sign).

The closure of the system (It) - (IVt) is carried out by invoking generalizations to the 3D case of Hooke's law for solid media and the Newton hypothesis for fluids given by Navier (see the last equality in (IVt)), as well as the private Joule thermodynamic laws (1t), Fourier (3t) and Clapeyron equations (or its known generalizations) (2t), but related to the conditions of globally equilibrium thermal processes.

The system (|t|) - ($|Vt\rangle$), (1t) - (3t) of the formalization of the fundamental and specific laws of thermomechanics includes, in aggregate, the entire list of inconsistencies and truncations formulated in the lower part of the left column: (A.1 - A.9).

We now turn to the content of the right-hand column of the table, focusing primarily on the successively considered (from A.1 to A.9) aspects of the *full* or possible phenomenological approach, eliminating the shortcomings expressed in relation to the already agreed model in the proposed concept.

A.1 The fundamental equations (I) - (IV) individual/substantial, i.e. for labeled PP, derivative in *t*, therefore in the *L*-system on quantum time $\partial \tau = \Delta t$ from the scalar function **f** or **f** as k-th component of the vector field function is determined by the limit

$$\frac{d\mathbf{f}}{dt} = \lim_{\substack{\Delta t \to 0\\ \Theta \in [t,t+\Delta t]}} \frac{\mathbf{f}(t + \Delta t, \vec{x}(t) + \vec{v}(\Theta)\Delta t) - \mathbf{f}(t, \vec{x}(t))}{\Delta t} , \quad (7)$$

where in the linear positing

$$\vec{v}(\Theta) = 0.5(\vec{v}(t + \Delta t) + \vec{v}(t)), \quad \vec{v}(t) = \vec{v}(t, \mathbf{x}), \quad \vec{x}(t) = \vec{\mathbf{x}}$$

(see too further indications (11), (12)).

It is important to keep in mind that dependence of the limit (7) from \vec{X} (t) and evidently from *t* is not additionally as in *L*-system does not defined as separate item partial derivation $\frac{\partial \mathbf{f}}{\partial t}$ in its classical meaning as far as to \vec{X} fixation simultaneouslymeans and fixation *t* with the exception a special cases of the fool braking of separate PP of medium.

For scalar functions **f** limit transitions are carried out directly, and for vector - for each of their components. In steady-state conditions the limit (7) adopts the repeating meanings. When the particles moves with constant field functions along a rectilinear coordinates of the inertial system of counting that

$$\frac{d\mathbf{f}}{dt} \equiv 0 \; .$$

Expression (7) is established changing **f** on time at motion of the marked *e.p.m.* along *their trajectory* on the specified step $\partial \tau$ and is differed on principle from the total derivative by **f** to **t**in the *E-system* of counting, which is written in the form

$$\frac{d\mathbf{f}}{dt} = \lim_{\Delta t \to 0, \bar{\mathbf{x}}} \frac{\mathbf{f}(t + \Delta t, \bar{\mathbf{x}}) - \mathbf{f}(t - \Delta t, \bar{\mathbf{x}})}{2\Delta t} + v_i \lim_{t \to \bar{\mathbf{x}} \to 0} \frac{\mathbf{f}(t, \mathbf{x}_i + \Delta \mathbf{x}_i) - \mathbf{f}(t, \mathbf{x}_i - \Delta \mathbf{x}_i)}{2\Delta \mathbf{x}_i}$$
(8)

Here the summation to $i = \overline{1,3}$, $d\mathbf{x} \neq \vec{v}(t)dt$ (t- thin).

Strictly speaking, its not exists a derivative concept of the same independent argument by other, for example, $d\mathbf{x}_i/dt$ without explanation of its differentials ratio meaning, namely and according to subject of consideration by way of establishment for current of time quantum unknown in advance of direction of PP trajectory fragment, e.i. really of the marked/labelled e.p.m. element of motion. Consequently, differentials dt and $d\vec{x}$ does not arbitrarily disappearing quantities but its ration must be equal to the desired velocity \vec{v} .

Differences between the limits (7) and (8) are obvious.

We would notice that in preparing on perspective of algorithm for computer realization of the present conception differential / scale on time $\partial \tau = \partial \tau$ is fixed over ability to be solved of the proper / actual discrete of a frequency spectrum. Further, by each rated τ moment of time $t + \partial \tau$ the *left* parts of the fundamental equations (I)-(IV) are determined on the *regular* net of *E*-system of counting for *preceding* rated moment *t* including, naturally, *given* initial distributions of action functions at $t = 0^+$ (see too before explanations for formalism (7)).

Effects of a operator $\frac{d}{dt}$ (*L*-system) application

to functions \mathbf{f} and its future transformation is considered in staging plan of concluding subjection of present work, noted by single asterisk * from the left.

A.2. In the original integral form of recording balance laws, an *arbitrarily* chosen macrovolume $\bar{\mathbf{v}} = \mathbf{vUs}$ is assumed to be fixed in the *E-frame* with a *certain* possibility of introducing a time differentiation operation under the sign of the integral over this volume for the corresponding field substance. As a result, we arrive at differential forms of laws (I) - (IV) with left and right sides that have a clear physical interpretation, but do not coincide with the similarly located terms in equations (It) - (IVt). Note that in equation (III), the expressions for the second arrival in the medium particle of conductive q_{cd} and radiant q_r types of energy are stored according to the traditional model of their description (see for example [1, 3, 6]).

AA.3-4. The extension of the model to the class of *asymmetric* mechanics of C-media is associated with two circumstances.

a) A natural idea that rotations / torsions — rotations of elementary (up to the PP scale) particles of the medium occur, as well as shear deformations, according to the laws of deformable / changing volume and shape, as well as heat-conducting bodies is taken.

b) Following the logic of the analysis, the moments from inertial and external forces (bulk, surface) are considered on the radius-vector $\vec{x}_b(t)$ of some virtual point **b** of the current e.m.p. (Fig. 2; see also Fig. 1 b, c). In fig. 2: indexes $c \wedge b$ in designations are related to center of mass / focusc and a virtual point of this particle **b** with a distance vector between them $\delta \vec{x}_{cb}$, which includes the component of *complete* deformation with velocity $\vec{v}_d(t, \vec{x}_b(t))$, i.e. from torsion and shear in absolute *L*-system coordinates.

Vector $\vec{\Lambda}(t)$ of inertial second rotation *e.m.p.* (see equation IV in the Table, and Fig.2) belongs to the class of vortices of the total strain rate, i.e. $\vec{\Lambda}(t) \in \{\vec{\Omega}\}$ (accordingly, $t=\bullet$), but with axis passing through center of inertia*c*.

Unit direction of the being used further vectors $\vec{\Lambda} \parallel \dot{\vec{\Lambda}}$ is precisely coincides with ort $i_{A.1}$ of the momentary *local* (trajectory) three-orthogonal (Cartesian) *bench-mark* $i_{A.k}$, $k = \overline{1,3}$ of the labeled *e.p.m.*torsionaly curl in absolute motion.



Fig. 2: The instantaneous position of the labeled/marked particles of the medium. Actual particle - darkened volume; distortions: shear - bar loop, torsion - bar-dotted momentary axis to the vector of the torsion velocity $\vec{\Lambda}$ of inertial turning of marked e.p.m. for the unit of time, in one radian and point c is center of inertia / mass. Designations $i_{A,k}$, $k = \overline{1,3}$ are the trajectory three-orthogonal *bench-mark* for the given *e.p.m*, moreover $i_{A,1}\dot{\Lambda} = \vec{\Lambda}$.

These factors have resulted in the introduction of the complete stress tensor Π and it deviator Π_d representation Π as the sum of symmetric $\mathbf{P}^{(s)}$ and antisymmetric $\mathbf{P}^{(a)}$ parts, followed by decomposition $\mathbf{P}^{(s)}$ into spherical \mathbf{P}_{s} and deviator \mathbf{P}_{d} terms. Tensors \mathbf{P}_{s} , \mathbf{P}_{d} and $\mathbf{P}^{(a)}$, in turn, based on the phenomenological assumptions linearly expressed in terms of the unit tensor I, as well as symmetric $\mathbf{S} / \mathbf{S}_d$ and antisymmetric \mathbf{A} tensors of proper deformations and turns, as well as the speed and "acceleration" of data movements (see (2), (3), (A)). Besides in equations (II) - (IV) it was required to introduce additionally antisymmetric tensors $\mathbf{\Lambda}$ of turn e.p.c. as single, but deformable, whole, Recall still that the upper index iota identifies the top signs $\iota = \emptyset, \bullet, \bullet \bullet =$, •, ••.

For C-mediums with heterogeneous and nonisotropy of the intrinsic physical properties modules $\overset{i}{B},\overset{i}{G},\overset{i}{R},\overset{i}{N},\overset{i}{R}_{\Lambda}$, $\overset{i}{N}_{\Lambda}$ are suggested in the form of tensors scalar/tensor multiplied on proper kinematic tensors I, $\overset{i}{\mathbf{S}}_{d},\overset{i}{\mathbf{A}} \wedge \overset{i}{\mathbf{\Lambda}}$. Let us remark absence in the equality (2), as consequence of notations simplification, of the terms

$$(2G'_{I_{s,1,0}}^{i'}\mathbf{x} dI_{s,1})\mathbf{I}$$
, summing up ι ,

where $I_{s,1}$ are first invariant of tensors $\mathbf{\hat{S}}$; G^{h} and $\mathbf{\hat{\kappa}}$ are modules of viscosity and collapse-functions. These terms are taken into account a viscous resistance to high-speed change of particle medium volume.

It proved also necessary to add the C-mediums in the capacity of additional function of the *action* of the components of the antisymmetric tensor moments $\mathbf{M}^{(a)} \begin{bmatrix} \mathbf{N} & \mathbf{m} \\ \mathbf{m}^2 \end{bmatrix}$ from volume action of the surface of couple forces, applied to these particles from the *outside* to the formalism of *asymmetrical* mechanics. This tensor is expressed linearly in terms of tensors $\mathbf{A} \wedge \mathbf{A}$ and consequently - the vortex vectors $\mathbf{\hat{\Omega}}$ and torsions $\mathbf{\hat{\Lambda}}$ of *e.p.m.* as a single but *deformable* whole, of its speedand «acceleration» in *E-system* of counting.

Noted in two previous item vector and tensor functions are, of course, in the right column of the table

and figured in left part of the fundamental equations (II) - (IV). Operations with tensors $\mathbf{A} \wedge \mathbf{A}$ and vectors $\mathbf{D} \wedge \mathbf{A}$ $\mathbf{A} \wedge \mathbf{A}$ are provided here in the form of (A) with the additional conditions (B). Modules $\mathbf{A} \wedge \mathbf{A}$ and $\mathbf{A} \wedge \mathbf{A}$ requires initial verification. Recall that a colon in the first term of the equation (III) to the left means the corresponding double scalar multiplication of tensor on dyad. This additive/member is action of power of the inner (by volume) forces on velocity of energy ε by change per unit time. The first term in the left side of the moment balance equation (IV), written as a vector multiplication of the vector deformation \mathbf{u}_d on the radius-

vector $\vec{\mathbf{x}}$, i. e. $\frac{d\vec{u}_d}{d\vec{\mathbf{x}}}$, on a full stress tensor $\mathbf{\Pi}$, there is

arises in torsional deformation moment of imbalance on the external surface forces $(\vec{n} \cdot \Pi)$ (cf. [5, p.p. 62 -. 63]).

A. 5 - 6. As in earlier publications [1, 3] in this paradigm is used a hypothesis only about local thermodynamic quasi-equilibrium (LTD QE, see e.g. [6]), i.e. on the 3D scale PP. Under this approach a functions of pressure p and temperature T, viewed in this concept as a manifestation, a kind indicators of status and changes in the fundamental substance ρ , ε , are deterministic (except for random fluctuations) measured (at least - for the F-mediums) givens. Therefore, experimentally determined physical coefficients / parameters / modules are usually dependent on p and T, but in conditions of generally global equilibrium thermomechanical processes. Expressed the situation in [2] called econditions. In connection with this there is realized in study [2] procedure inversion, i.e. the transfer of the indicated coefficients, established in e-conditions the performance of the experiments, and the themselves functions p and T to *current* dynamic conditions of their expression through ρ , ε in LTD QR. The starting point of this transition are: representation about the direct dependence of these parameters and functions only on the current values of ρ (especially for gas) and ε , as well as the concept of full differentials and curvilinear integrals with introduction of the integrator factors (see (1) - (3) and also [2]).

Note that in present work functions p and T essentially are considered as of *indicators* of the substances p and ε condition and change.

The main results of the made transformations are presented in the table relations (1) - (3), in which $\beta_{\rho}(\rho,\varepsilon)$ - the treatment function, and $\stackrel{'}{B}(\rho,\varepsilon) \wedge \stackrel{'}{G}(\rho,\varepsilon)$ - volume and shear-modules of elasticity, their velocities and "accelerations" with convert from *e-conditions* of own experimental identification in conditions of the LTD QR according [2]. By similar inversions are subjects to modules $\stackrel{'}{R} \wedge \stackrel{'}{R}_{\Lambda}$ and $\stackrel{'}{N} \wedge \stackrel{'}{N}_{\Lambda}$ in operations (A). Detail of

the further actions with indicated modules is considered also in article [2]. It is clear, that possibly furthers amplification of ideas for physical coefficients by the inlet of its dependence in addition from substance $|\vec{v}|$ Some more in the capacity of insight-hypothesis we point out that if it is granted physically in many possible judgement about equality of the modules G = R (see table of the right), then formalism of the law (II) will be, as clearly, contain the sum of kinematic tensors of full

deformations
$$\mathbf{T} = \frac{d \vec{w}_d}{d\mathbf{x}} = \mathbf{S} + \mathbf{A}$$
.

A. 7. Direct account rate of thermal deformation of the medium particles \vec{v}_q as additive addition to the velocity \vec{v}_f from the force fields, so that $\vec{v} = \vec{v}_f + \vec{v}_q$, is realized by the formula (5) where A - is coefficient velocity of thermal deformations (see also [1]) in the form of a product coefficients of conductivity of the temperature and linear thermal deformations.

A. 8. The author, as before, adheres to the opinion that for F-media, when critical parameters of a freely disturbed flow are reached, i.e. far from solid boundaries, a sporadic manifestation of a steep / abrupt / practically abrupt phenomenon occurs (one of the options due to the lack of experimental data) changes in the moduli of deformation $\overset{\prime}{B},\overset{\prime}{G},\overset{\prime}{R},\overset{\prime}{N},\overset{\prime}{R}_{\Lambda}$, $\overset{\prime}{N}_{\Lambda}$, expressed in the form of turbulent fluctuation. In connection with the above, the postulate on the dominant similarity of the specified effect to the phenomenon of plastic deformation or brittle fracture in solid continuous media was advanced in [1] (see also further the paragraph following relations (10a) and marked with a dot • on the left). However, unlike the mechanism for describing a turbulent transition, considered as a possible option, in [1] with respect to the critical level of the main values of the deviator of the transposed strain velocity gradient tensor $\dot{\mathbf{S}}_{d}$, at this current stage of research, with permanent refinement and development of the present theory, it seems natural to propose a different, generalized criterion for collapse transitions in Cmediums, based on the property of memory about the pre-actual values of e.m.p. and written in the form of the following equality (10), obtained on the basis of the installations described in A.9.

The indicated development of the theory assumes: the nomination of the epistemological causal property of *reciprocity* of the left and right sides of the fundamental equations (I) - (IV) (see below), the establishment of an integral memory about the prehistory of particle deformation of the medium, the introduction of a absolute *binary* ($L \land E$) totality system of the counting and viscous torsion of the continuum moles in relation to its absolute system as well as at to momentarylocal trajectory bench-mark for given e.p.m.

with force elongation / shortening and rotation of their fibers / current tubes [7], consideration of the problems of *near-wall interaction* [3], *semi-analytically* established action factors [7, 14], etc.

A. 9. First of all we would bring in necessary clarifications for separate dependences in the relations (6), (A), (B), (C) written down in *E*-system of counting of the right column table.

For fixed time moment $t + \partial \mathbf{r}$ we would consider dyad $\nabla_{\mathbf{x}} \vec{a}_d = \left(\frac{\partial a_{dj}}{\partial \mathbf{x}_i}\right)$ on 4D scales of time and space $\mathbf{x} \in \mathbf{v}$ ep.m. Vector \vec{a}_d is equal to difference $\vec{a}_d = \vec{a} - \vec{a}_c$, where vectors $\vec{a}, \vec{a}_c, \vec{a}_d$ are pseudo-accelerations $\partial \vec{v} / \partial t$, $\partial \vec{v}_c / \partial t$, $\partial \vec{v}_d / \partial t$ of the full velocity \vec{v} , forward motion \vec{v}_c and *full distortion* \vec{v}_d prototypes of the marked *e.p.m.* respectively. We think that focuses of these particles $c_{L-s.p}$ for data interval/quantum of time $\partial \mathbf{T}$ "passed" over some fixed points $c_{E-s.}$ elementary volume \mathbf{v}_E by *E-system*, accepted, in turn, in the capacity of centers (also focuses) $c_{L-s.m}$ of the marked *e.p.m.* (particles)but in previous, on quantum smaller, moment of time, that is t (see Fig. 3).



Fig. 3: Conditional "image" of the *e.p.m.* passage across registration elementary volume \mathbf{v}_E of the *E-space*. On the time interval $[t, t + \partial \mathbf{T}]$ the marked *e.m.p.* with center $\mathbf{c}_{L-s.m}$ is substituted by its nearest prototype of future with center $\mathbf{c}_{L-s.p}$ in time $t \in [t, t + \partial \mathbf{T}]$.

The first part of the word *pseudo*-acceleration underlines fundamental difference of a classical notion about acceleration, as referred to unit mass measure of isolated body force of a inertia at action thereupon of the outside loading from appears above relations of differential proper velocities for two nearest *e.p.m.*, i.e. prototypes \leftarrow types, on vanishingly small distance from point **c** at to temporal equivalent $\partial t = \partial \mathbf{T}$ of this deviation. Later on distinctive abbreviation *pseudo*- for foregoing vectors in *E-system* analysisis omitted, and word acceleration is put in quotes like before, and for all partial differentials to make use symbol ∂ .

For furthest it is important following circumstances.

1. At each fixed moment of time and for any point $\vec{x} \in \overline{v}$ of the volume of individually *e.p.m.* velocities

of it transit transfer \vec{v}_c have equal meaning, but in general depending from time and, consequently, from *current* coordinate of it focus *c* in space.

2. Later under terms "distortion/deformation" we imply deformations in the value, form and elastic/viscid turning of some element of the medium, in absolute system of the couting $(L \lor E)$

As a result for stated above dyad we deduce (see also (B))

$$\vec{\nabla}_{\bar{\mathbf{x}}}\vec{a}_d = \vec{\nabla}_{\bar{\mathbf{x}}}\vec{a} - \vec{\nabla}_{\bar{\mathbf{x}}}\vec{a}_c = \vec{\nabla}_{\bar{\mathbf{x}}}\vec{a} \,. \tag{9a}$$

Present factor will be inserted and into vector/tensor operations. Thus, appearing further tensors of the convection carry \mathbf{U}_c , \mathbf{U}_c , \mathbf{U}_c , a for every fixed

of the time moment and on *e.p.m.* scales are regarded as *tensor constants*.

Now we shall propose and discuss the criterion of the collapse-passage based on function of long memory accumulation about deformations of *e.p.m.*, it follows representative itself *a priori* considerable degree of probability.

Memory about before the actual states velocity \vec{v}_d and proper deformation \vec{u}_d in rigid 3*D* space may be established by following integrals (in particular case of the start from *state of rest*, see also (6) and (B))

$$\vec{v}_d = \int_0^t \vec{a}_d \partial \boldsymbol{\tau}, \qquad \vec{u}_d = \int_0^t (\int_0^{\leftarrow t} \vec{a}_d \partial \boldsymbol{\tau}) \partial \boldsymbol{\tau} \qquad (9b)$$

where arrow between symbols of the integrals in brackets means simultaneity of the their both increments of inner and outer integrals.

On Fig. 4 is exemplified simplest, but visual example of the "memory effects" at discretely-linear change of the "acceleration" \vec{a}_d .



Fig. 4: Didactic instance of the "memory effects" forming about e.p.m. deformation.

However expressions (9b) don't permit, without appearance "superfluous" unknowns subject objectively to elimination, to express change of deformations \vec{u}_d during time across vector $\vec{a} = \partial \vec{v} / \partial t$ escaping "acceleration" \vec{a}_c of the transit transfer *prototype* by marked e.p.m. over fixed point **c**.

Thus we shall put forward following lower modification of the field of deformation $\vec{a}_d^{\bullet}, \vec{v}_d^{\bullet}, \vec{u}_d^{\bullet}$ (and with distinctive from previous notation as a point by the capacity of a superliner index).

Stated modification permits for rather dense 4D set of grid points to formulate criterion of the collapse passage, i.e. metamorphosis, qualitatively changing character of a medium motion when accumulated during time deformation in some *3D E-space* point or into its totality of proper limiting level.

The stated implies that at corresponding stage of calculation dynamics is considered within the resolvent particularization of development of physical processes in the field of certain *k*-th increment of *FWS*, set by specific algorithm of numerical implementation of corresponding initial boundary value.

We shall represent in the a.m. system modification of the "acceleration" deformations \vec{a}_d^{\bullet} as it middling integral meaning by surface **s** of volume **v**, conceding in each fixing moment of time with volume of the actual *e.p.m.* at additional referring of the present functions to typical linear scale *l*. Then using known relations of the tensor analysis we obtain following the set of equality

$$\vec{\bar{a}}_{d}^{\bullet} = \frac{1}{k} \int_{\mathbf{s}} (\vec{a}_{d})_{n} \partial \mathbf{s} = \frac{1}{k} \int_{\mathbf{s}} (\vec{n} \cdot \mathbf{a}_{d}) \partial \mathbf{s} = \frac{1}{k} \int_{\mathbf{v}} \vec{\nabla}_{\bar{\mathbf{x}}} \cdot \mathbf{a}_{d} \partial \mathbf{v} \mathbf{s}$$

$$\vec{\bar{a}}_{d}^{\bullet} = \frac{1}{k} \int_{\mathbf{v}} (\vec{\nabla}_{\bar{\mathbf{x}}} \cdot \mathbf{a} - \vec{\nabla}_{\bar{\mathbf{x}}} \cdot \mathbf{a}_{c}) \partial \mathbf{v} = \frac{1}{k} \int_{\mathbf{v}} \vec{\nabla}_{\bar{\mathbf{x}}} \cdot \mathbf{a} \partial \mathbf{v}, \quad \vec{\bar{a}}_{d}^{\bullet} = \vec{a}_{d}^{\bullet} / \mathbf{1} .$$
(9c)

Here underlined item fall out.

In view of supposed continuity of functions, trifle spatial scales of *e.p.m.* and at convenient choice I = v/s (symbolical division in multitude theory) with admissible error, but with preference in simplicity, we shall find (on condition of use sign of the strong equality)

$$\vec{\overline{a}}_{d}^{\bullet} = Div \,\mathbf{a} = \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{a} , Dim \,\vec{\overline{a}}_{d}^{\bullet} = c^{-2}.$$
(9d)

where $Div \wedge Dim$ is short for "divergence" and "dimension" respectively.

In (9c, 9d) \vec{n} is singleness exterior normal to surface **s**; $\mathbf{a} = (a_{ij}), \mathbf{a}_c = (a_{c,ij}), \mathbf{a}_d = (a_{d,ij}) - tensors of the "accelerations" of velocities <math>\vec{v}, \vec{v}_c, \vec{v}_d e.p.m.$ and their full deformations; Similarly over divergence of the tensors of velocities \vec{v} and transferences **U** is written vectors $\vec{v}_d^{}, \vec{u}_d^{}$.

By integrating (9d) by t single (short memory) and twice (long memory) in view of expressed previously consideration with respect to expressions (9b) we shall establish

 $\overline{\overline{u}}_{d} \stackrel{\bullet}{=} \overline{\nabla}_{\overline{\mathbf{x}}} \cdot \mathbf{U}_{d} = \overline{\nabla}_{\overline{\mathbf{x}}} \cdot \mathbf{U} = \int_{0}^{t} (\int_{0}^{\leftarrow t} \overline{\nabla}_{\overline{\mathbf{x}}} \cdot \mathbf{a} \partial \tau) \partial \tau$

Second integral in (9e) can be interpreted in the capacity of modification of relative and averaged to **s** deformation of volume, form and turning of *e.p.m.* with centers are passing through point **c** at preservation memory about before the actual strained states of its particles of medium. Function of $\overline{\vec{u}_d}^{\bullet}$ depends to time only from components of tensor "accelerations" of surface distribution the desired vectors of velocity, i.e. specific momentum $(\vec{v})_n \in \mathbf{s} \Leftrightarrow \vec{n} \cdot (v_{ii})$.

In terms of adjusting supposition contained in following item marked from the left by points •, ••, •••, we shall accept that there is such limiting meaning $\left|\overline{\vec{u}_d}\right| = \overline{\vec{u}_d}^{\bullet}$ at which appears collapse passage with sharp the drop of modules resistance by the motion of the *e.p.m.*. Therefore, we shall propose following dimensionless criterion

$$I^* = \overline{u}_d^{\bullet} \Big|^* = \Big| \vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{U} \Big|^*, \quad Dim \ I^* = \emptyset, \quad \mathbf{U} = \left(u_{ij} \right), \quad i \wedge j = \overline{1,3} . \tag{10}$$

To bring more clarity to the subject under process underlined, that criterion (10), appearing also in relations (C) of the table, reduced to generally dimensionless form and defines critical level of resulting deformation of prototypes of marled e.p.m. passing through certain node (focus) point of rigid 3*D* space. The proper vector of the deformation is defined by scalar product of Hamilton operator $\vec{\nabla}_{\vec{x}}$ (in *E-system*) and sum of tensors $\mathbf{U} = \mathbf{U}_c + \mathbf{U}_d$ by forward motion of noted *e.p.m.*, each as unit \mathbf{U}_c and full deformations by its of the particles \mathbf{U}_d . Moreover by the preceding

remark relatively of the equalities (9a) vector $\vec{\nabla}_{\vec{x}} \cdot \mathbf{U}_c = 0$.

We shall indicate still yet, that in principle it is not inconceivable: alternative forming of the criterion passage on base first equality in expressions (9e) independently or in combination with criterion (10) in dimensionless form with referring the vector \vec{v}_d^{\bullet} to spectral velocity $v_{s.}$, established by limiting *FWN* certain *k*-th increment of *FWS*, as per the mesh of numerical solution. Namely

$$\vec{\bar{v}}_{d}^{\bullet} = \omega_{s.}^{-1} (\vec{\nabla}_{\vec{\mathbf{x}}} \cdot \mathbf{U}), \quad \mathbf{U} = (v_{ij}), \quad \omega_{s.} = \mathfrak{B}_{s.} v_{s.} = \mathbf{I}^{-1} v_{s.}, \quad i \wedge j = \overline{1,3} \quad ,$$

$$I^{*} = (b_{u} \overline{u}_{d}^{\bullet} + b_{v} \overline{v}_{d}^{\bullet})^{*}, \quad (10a)$$

where b_{μ} , b_{ν} are weight coefficients, $b_{\mu} + b_{\nu} = 1$.

It should be noted following. The process return to until critical conditions are reversible for fluid mediums but as a rule irreversible for solid. We shall adduce some quality proofs / positive evidences in behalf of the present criterions.

 Reason from basics representations about material unity natural structure every concrete medium, satisfaction by it to fundamental laws of a thermomechanics, together with total character *direction* electromagnetic molecular and atomic interaction in present medium independently, however, from actual the kind of it *state of aggregation* of matter, represents permissible advancement postulate about *the dominant similarity* of phenomena of critical transition of modes of its movement disregarding the categories of these states [1].

- Numerous, long since, dubbed experiments for solids, by example, on one-axis tension prismatic samples either from constructive materials or brittle bodies, show that at deformation \vec{u}_d proper to conditional limits of fluidity or of the extreme principal of the shear strain is taking place jump decrease of the modulus of volume elasticity and shear but in the latter case we have fragile destruction. Present fact can be treated as breakdown of increase intensity of the attraction property for intermolecular connections on its mediums. Then with this in mind contents of the previous item we assume a priori and in fact heuristically opinion about certain correspondence of the collapse-passage in C-mediums situated in various state of aggregation.
- ••• We shall omit enough laborious for concise description details of metamorphosis accompanying condition of the development of transitional processes in considered mediums we restrict only ascertaining of following.

Structure relations (9e) and criterion (10) in its application to F-mediums permits qualitative, at least, explain face established also in distant years, but by careful the experiments, influence to origin of turbulence (in F-medium) heterogeneity by the enter stream at smooth solid boundaries but also apparently and view of a transitional process at a steady state. By consequence of the present circumstances is change of the critical Reynolds number in highly wide range of meaning $Re_{cr} \in [2 \cdot 10^3 \div 5 \cdot 10^4]$ and possibly more (see, for example [4, 8 – 13] and etc.).

We shall indicate also, that relations (9c) - (9e), (10), (10a) involves *full* tensors displacement **U**, their velocity **U** and "acceleration" **a**, but not their deviators, i.e. is taken into consideration and "spherical" part of *e.p.m.* volume deformation. Clearly, that only specifically posed physical experiments will be able to bring clarity in present dilemma.

Besides, it remains open question, particularly important for *solid*, about equivalence (without take of sign) processes of a *tension* and *pressing* of medium filaments as approach it's to critical meaning. At last the following investigation will bring out the need and way of the collapse-functions entering into heat physical coefficients of the expressions for *T*, q_{cd} , q_r etc.

It is obvious to the possibility or the need, at properly proof, entering into the compositions functions (the left parts of equations (II), (IV)) the terms of additional force and moment effects of actions to e.p.m. containing components of the vectors of local torsion turn $\vec{\Lambda}$, its velocity $\vec{\Lambda}$ and "accelerations" $\vec{\Lambda}e.p.m.$ as a single but deformable whole, expressed in forms of antisymmetric tensors $\mathbf{\Lambda} = (\mathbf{\Lambda}_{ij})$ similarly by members with components A_{ij} (see in table relations (6), (A)).Let us remark that parameters c_i and $æ_i$ entering into expression for moment of inertia $\mathbf{J} = c_i \mathbf{J}^0$, need special analysis. So the greatest meaning of the parameters $\mathbf{æ}_{I}$ is defined by established of PP linear scale in accordance to the greatest admissible of Knudsen's number Kn_{sup} . That statement maybe apparently the most important for the solid C-mediums.

Thus it function Λ in law (IV) should be consider as fourth (by enumeration) fundamental substance with possibility close the system of basic equations of C- mediums'thermomechanics.

The subsequent development concerned above the question as and problem of the realization of algorithm for irregular distribution of the unknowns substances \mathcal{LE} -conversions into fixed regular net of *E*space(see later operation (12)) is assumed to state in one of the following publications of author.

In conclusion, we believe we need to extract and explain two stated below and radically necessary important circumstances missing in work [14].

*Property of a *concerted action* of the left and right parts of equations (I)-(IV) imply the following.

Suppose, as before, designation fis identifier one from the desired substances of a matter –field, so that $\mathbf{f} = \left\{ \rho \lor \varepsilon \lor \upsilon_i \lor \dot{\Lambda}_i, i = \overline{1,3} \right\}$ of everywhere dense set of points of some closed 3D *Eulerian* space $\overline{\mathbf{V}}$. In this domain $\overline{\mathbf{V}}$ we shall give a *regular*, bounded and *countable* set of the points $\mathbf{\vec{x}}_{rg}$. In each fixed moment of the time t = t we have the same set of *labeled point* $\mathbf{\vec{x}}(t)$, (coinciding with $\mathbf{\vec{x}}_{rg}$, i.e. $\mathbf{\vec{x}}(t) = \mathbf{\vec{x}}_{rg}$) and values in them of all causal factors of the *action* to **f** in accordance to the left parts of the equations (I) – (IV).

At change time in stated above scale for PP on quantum $\partial \tau$ we will have

$$\vec{x}(t+\partial\tau) = \vec{x}_{rr} + \vec{v}(\tau)\partial\tau = \vec{x}_{ir} \Big|_{t+\partial\tau\tau}, \ t \le \tau \le (t+\partial\tau)$$
⁽¹¹⁾

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where $\vec{\mathbf{x}}_{ir}$ – are the coordinates trajectory *irregular* points of their preceding regular set $\vec{\mathbf{x}}_{rg}$ but with functions **f** meanings

$$\mathbf{f} = \mathbf{f}(\vec{x}(t+\partial\tau), t+\partial\tau) = \mathbf{f}(\vec{\mathbf{x}}_{ir})|_{t+\partial\tau}$$

Now let us call by symbol \mathcal{LE} operator/algorithm of return with renovation of a topological transfer, with inevitable and stipulated previously of physically objective *defect*, of functions **f** defined on set $\vec{\mathbf{x}}_{ir}$ as according to (11), from this set to set of formers fixed points $\vec{\mathbf{x}}_{rg}$. In this way is go return to regular net $\vec{\mathbf{x}}_{rg}$ with renewal **f** in common case. As a result the new (non-stationary state of the medium) values of this

functions fare determined on regular *Eulerian* 3D grid
$$\mathbf{\tilde{x}}_{r\sigma}$$
 at time $t + \delta \tau$ by equality

$$\mathcal{LE}\left\{\mathbf{f}(\vec{x}(t+\partial\tau),t+\partial\tau)\right\} = \mathbf{f}\left(\vec{\mathbf{x}}_{rg}\right)\Big|_{t+\partial\tau}$$
(12)

It is clear too that on basis of the conversional (12) are revived too *corresponding* functions of the *action* in left parts of the equations (I) – (IV) apart from its components which are not dependent directly from indicated earlier functions **f** (e.g. \vec{q}_r , possible \vec{F}).

When reaching, beginning with $t = t^0 = t^0$, of steady movement in volume \overline{V} we will evidently get

$$\mathcal{LE}\left\{\mathbf{f}(\vec{x}_{ir},t^0)\right\} = \mathcal{LE}\left\{\mathbf{f}\left(\vec{x}_{ir},t^0 + m \partial \tau\right)\right\} = \mathbf{f}(\vec{\mathbf{x}}_{rg})\Big|_{t^0} , m=1,2,...$$

where $\vec{x}_{ir}(t^0) = \vec{x}(t^0 + m\partial \tau) = \vec{x}_{ir}|_{t^0 + m\partial \tau}$.

Special case of \mathcal{LE} transformation is elated to movements of continuous medium in the static closed range calculation volume filled with it $\overline{V} = V \cup S$ with fixed boundary S when in each consequent time unit labeled e.p.m. crossingtransparent sections of the boundary S entering or exiting region \overline{V} are allowed for.

Stated the operating sequence is conceptual represented model of the numerical discretization of a mathematically strict limiting condition of the *consistency* of equations (I)-(IV) left and right sides which are expressed by equation

$$\lim_{\substack{\Delta t \to 0 \\ \Delta \mathbf{\bar{x}} \to 0}} \mathbf{A} \ ct_k(t - \Delta t, \mathbf{\bar{x}} - \Delta \mathbf{\bar{x}}) = \lim_{\Delta t \to 0} \frac{\mathbf{M} \ on_k(t + \Delta t, \mathbf{\bar{x}}(t + \Delta t)) - \mathbf{M} \ on_k(t, \mathbf{\bar{x}}(t))}{\Delta t}, \ k = \overline{1, 4}, \quad (12a)$$

where $A ct_{k}$ - are totalities of the equations (I)-(IV) left sides as casual factors, and $M on_{k}$ are proper monads: $ln\rho$, $\rho\vec{v}$, $\rho\epsilon$, $J\vec{\Lambda}$, - as effect factors in right parts of its equations. Let us remark that structure of the equality (12a) in a certain relation is similar to the first left (ascending) and right (descending) differences in differential calculus theory and finite differences methods.

Didactic scheme of the base substances Mon_k renovated return in knots of 3D regular net $\vec{\mathbf{x}}_{rg}$ from irregular net $\vec{\mathbf{x}}(t_{v+1}) = \vec{\mathbf{x}}_{ir}|_{t_{v+1}}$ for time quantum in from of a plane cut to volume \mathbf{V} fragment is illustrated by Fig.5. In explanations to Fig.5 and further in text are employed indicators t_v , t_{v+1} , $\partial \tau = t_{v+1} - t_v$ for *L*-system (and the same but by fat print for *E*-system). Here as and before $\partial \tau$ is quantum of time; index v is marked moment of time for beginning of quantum with number v and (v+1) is marked termination of it quantum and beginning for quantum with number (v+1), v = 1, 2...; meaning $t_{v=1} = 0^+$ is initial time moment.



Boundary under-domain influence

Fig. 5: Scheme of the base substances renovative return on regular net in a plane cut. Here sign × are knots of the regular net; $\vec{\mathbf{x}}_{rg}$ is one from its knots; sign \otimes are positions of the marked *e.p.m.* (particles); $\vec{\mathbf{x}}_m(t_{v+1}) = \vec{\mathbf{x}}_{ir.m}|_{t_{v+1}}$ at the end t_{v+1} of current v-th time quantum $[t_v, t_{v+1}]$ as counting set of trajectory points $m \in \{m_s\}$ in under-domain of *influence* \vec{r}_{sup} on meaning of M on $_k$ in knot $\vec{\mathbf{x}}_{rg}$.

At numerical solutions of the equations (I)-(IV) return with renovation transfer (12) under evident *discrepancy* connected with continuity hypothesis *defect* and with *discretesation* of the assumed continuous dependences maybe realized by various ways requiring of the following analysis and experimental investigation.

The variants of \mathcal{LE} computing transformation over the whole visibility will be different by formalism of weight functions W_m . Here index*m* marks the numbers of irregular /belonging to trajectory medium points, i.e. e.p.m. focuses from its regular set net knots $\vec{\mathbf{x}}_{rg.m}$ at $t = t_v$ (beginning of data time quantum). Data particles for quantum $\partial \tau$ moved to own distances $(\vec{\mathbf{x}}_{ir.m}|_{t_{v+1}} - \vec{\mathbf{x}}_{rg.m}|_{t_v})$ and in moment t_{v+1} with meaning of the monads $M \text{ on }_k(t_{v+1}, \vec{x}_m(t_{v+1}))$ proved to be fixed in under-domain of its influence (by norm r_{sup}) upon values of the its monads at $t = t_{v+1}$ in separately chosen and deveined r_{sup} knots $\vec{\mathbf{x}}_{rg}$ as forerunner indicated earlier under-domain.

Of course above influence is absolute function from distribution of distances r_m between $\vec{x}_m(t_{v+1}) = \vec{x}_{ir,m} \Big|_{t_{v+1}}$ and data knot \vec{x}_{rg} .

In sight may also statement of much more *perfect* but, highly *laborious* algorithm with attraction of the action functions ACt_k not only at the *beginning* of a current the time quantum $\partial \tau$ but also (we shall say) in it *end*.

It's expedient put in the two alternative of the transformation function \mathbf{f}_{ir} (some from *M on* _k) to \mathbf{f}_{rg} , i.e. on regular net. We have the following

$$\begin{cases} \mathbf{f}_{rg} = \sum_{m=1}^{m_s} \mathbf{f}_{ir.m} W_m, \ \sum_{m}^{m_s} W_m = 1, \ W_m \ge 0, \ t = t_{v+1} \ \Rightarrow \ \mathcal{LE} \left\{ _ \right\} = \sum_{m=1}^{m_s} __{ir.m} W_m; \\ \text{first variant:} \\ W_m = \frac{(1 - \overline{r}_m^{\ \alpha})}{\sum_{m=1}^{m_s} (1 - \overline{r}_m^{\ \alpha})} ; \\ \text{second variant:} \\ W_m = \frac{\overline{r}_m^{\ -\beta}}{\sum_{m=1}^{m_s} \overline{r}_m^{\ -\beta}} \\ (\mathbf{v}_{pp}^{-1/3} / r_{sup} = \overline{r}_{inf}) < (\overline{r}_m = r_m / r_{sup} = \left| \mathbf{\bar{x}}_{rg} - \mathbf{\bar{x}}_{ir.m} \right| / r_{sup}) < 1; \\ \text{if } r_j \le \mathbf{v}_{pp}^{-1/3} \text{ and } j \in \{m_s\}, \text{ that } \mathbf{f}_{rg} = \sum_{i=1}^{j_s} \mathbf{f}_{ir.j} / j_s, \ j = 1, 2, \dots j_s, \end{cases}$$

where r_{sup} and m_s is linear norm and common number of points $\mathbf{\tilde{x}}_{ir.m}\Big|_{t_{v+1}}$ in defined (by consensus) underdomain of influence $\mathbf{f}_{ir.m}(\mathbf{t}_{v+1}, \mathbf{\tilde{x}}_{ir.m})$ on $\mathbf{f}_{rg}\Big|_{\mathbf{t}_{v+1}}$; j_s is amount distances of r_j ; \mathbf{v}_{pp} - numerically stipulated volume of physical/material point PP. Parameters α and β can to depend from $\overline{r}_m \in [\overline{r}_{inf}, 1]$ as well as in strict sense from the kind of unknown substances *M* on _k and required the additional analysis.

In special case of the meaning β =2 it takes place correspondence with proper laws Newton and Coulomb.

By essential lack of the noted variants (12b) is uncertainty in meaning of parameters $\alpha \land \beta$.Leaving at yet aside of a classical methods of the parabolic, harmonic and some other approximations of it difficult may be reduced as follows.

The small neighborhood of central knot $\vec{\mathbf{x}}_{rg}$ we shall envelop by not large 3D domain $\delta \mathbf{v}$ (see Fig. 5) and for it domain at $t=t_{v+1}$ we claim that

$$\mathcal{LE}\left\{\mathbf{f}_{ir.m}, \overline{r}_{m}(\mathbf{\vec{x}})\right\} - \mathbf{f}(\mathbf{\vec{x}}) = 0, \ m \in \left\{m_{s}\right\}, \ \mathbf{\vec{x}} \in \delta \mathbf{v}.$$
(12c)

For reasons of $\delta \mathbf{v}$ trifle we should accept parameter α (or β) depending from $\vec{r}_m(\vec{\mathbf{x}})$ linearly. Necessary registration points of it index we select from

positively approbatory diapason of it variation in volume $\delta \mathbf{v}$. Then for realization of (12c) relation and therefore establishment of $\mathbf{f}_{rg}(\mathbf{\ddot{x}}=\mathbf{\ddot{x}}_{rg})$ the numerical values maybe used one from the most productive for data problem *weighted discrepancy methods*. In addition is assumed attraction of suitable sampling and examination functions with \mathbf{W}_m rate setting at integration on $\delta \mathbf{v}$ in relation to knot $\mathbf{\ddot{x}}_{rg}$.

Letting now degree $\alpha \lor \beta$ varying in depending from $\overline{r}_m(\mathbf{\vec{x}})$ for example to linear law and with choice of it law degree necessary meaning from range [1/2, 2] to fulfil of the dependence (12c)we shall apply one in suitably (by selection of sampling and examination functions) of *weighted discrepancy methods* with final act $\mathbf{\vec{x}} = \mathbf{\vec{x}}_{rg}$. In addition most likely with rate setting of $W_m \mid_{\mathbf{\vec{x}} = \mathbf{\vec{x}}_{rg}}$ at integration on $\delta \mathbf{v}$ by it knot, e.i. $\mathbf{\vec{x}} = \mathbf{\vec{x}}_{rg}$.

As a whole evidently that purpose of parameter $\alpha \lor \beta$ must largely to show the best correlation with well the known precise experimental results.

** Please note the following. Equation of a internal energy (increment) ε (III) completely coincides which differential form of writing of the more total law about balance of full energy (per unit time) of particles of moving continuous medium in the labeled volume of *Eulerian* space

$$\rho(\vec{F}\cdot\vec{v}) + \vec{\nabla}_{\bar{\mathbf{x}}}\cdot(\mathbf{\Pi}\cdot\vec{v}) + ((\vec{\nabla}_{\bar{\mathbf{x}}}\vec{u}_d)^* \times \mathbf{\Pi})\cdot\dot{\vec{\Lambda}} + \vec{\nabla}_{\bar{\mathbf{x}}}\cdot(\mathbf{M}^{(a)}\cdot\dot{\vec{\Lambda}}) + \rho q_{cd} + \rho q_r = \frac{d}{dt}\rho\left(\frac{v^2}{2} + \varepsilon\right) \tag{III'}$$

if velocity of change of a kinetic energy of a medium macromotion satisfies the equation

$$\rho \vec{F} \cdot \vec{v} + (\vec{\nabla}_{\vec{x}} \cdot \Pi) \cdot \vec{v} = \frac{d}{dt} \rho \frac{v^2}{2}, \qquad (III'')$$

in which the left and right parts of this equation are written, as stated previously, in various systems of counting:

The last demands additional analysis which is tied with question: whether the second term in expression (III") at left describes the second volume work of an exterior surface forces in *E*-system, i.e. at coordinates (\vec{x}, t) ?

The term $\vec{\nabla}_{\vec{x}} \cdot (\mathbf{\Pi} \cdot \vec{v})$ in (III') describes volume action of a work per unit time of exterior surface forces, one part of which goes into change of a kinetic energy of macroscopic motion $v^2/_2$ of partices media. It motion is expressed of *phenomenological* by second term to left in equation (III'), and the other part defined in equation (III) of the first term at left is spent on increment (in algebraic sense) of internal energy.

Let us remark, that by analogue of expression (III") in traditional model of thermomechanics C-mediums is equation which succeeds from relation (II_T) by means of the scalar product of it *both* parts on vector velocity \vec{v} , it is inderstood, only in *E*-system of counting [5].

Anyhow it's beyond question possibility of the inclusion in fundamental system (I)-(IV) equation (III') instead of (III).

III. SUPPLEMENTS

Let us consider some particular simple models used for description of the fluid dynamics as examples of application of the proposed formalism with regarded that given conception contains group of the additional physical coefficients requiring of its determination. In considered examples $L\Lambda E$ -systems of counting in essence fully are agreed upon.

a) Main Balance Relations of the Dynamics of Ideal Gas for Barotropic Processes with Moderately Inhomogeneous Flow

In addition we accepts that thermomechanics is symmetrical and steady mass, processes are stationaries and to be considered along of the flow lines. Conditions stipulated in the title of this subsection and followings imply that operator $\frac{d}{dt} = \vec{v} \cdot \vec{\nabla}_{\vec{x}} \ni d\vec{x} = d\vec{x}$, tensor

 $\Pi = \mathbf{P}_s = p \cdot \mathbf{I}, \dot{G} = 0, \dot{B} \approx \ddot{B} \approx 0$ and in fact we proceed to the notions of quasi-equilibrium thermodynamics.

Further subscript at operator $\vec{\nabla}$ is lowered.

As known, the equation of energy balance per unit time for a continuous medium in full writing and for a given case (see too (III')) is as follows:

$$\rho \frac{d}{dt} \left(\varepsilon + \frac{v^2}{2} \right) = \rho \vec{F} \cdot \vec{v} + \vec{\nabla} \cdot \left(\mathbf{P}_s \cdot \vec{v} \right) + \rho q, q = q_{cd} + q_r$$
(13)

This equation reduces to balance relation (III) upon subtraction of an equation of energy balance for macroscopic motion, which is obtained by scalar multiplication of both parts of relation (II) by velocity \vec{v} .

Setting $\rho = \rho(p)$ and using Eqs. (III),(2) (see Table)at $\kappa = 1$ and (13) in the theoretical model under consideration and taking into account that the initial pressure is equal to the algebraic sum of lower limits of integration in expression (2), we obtain the following equations for the class of barotropic flows.

$$\frac{d}{dt}(\varepsilon + \frac{v^2}{2}) = -\vec{v} \cdot \vec{\nabla}\Pi - \frac{1}{\rho}\vec{\nabla} \cdot (p\vec{v}) + q, \quad \frac{1}{\rho}\vec{\nabla} \cdot (p\vec{v}) = \vec{v} \cdot \frac{\vec{\nabla}p}{\rho} + \frac{p}{\rho}\vec{\nabla} \cdot \vec{v}$$
(14)

$$\vec{v} \cdot \frac{\vec{\nabla}p}{\rho} = \vec{v} \cdot \vec{\nabla} \,\mathcal{P}(p(\rho, T(\rho))), \quad \frac{p}{\rho} \vec{\nabla} \cdot \vec{v} = -\frac{p}{\rho^2} \frac{d\rho}{dt} \tag{14a}$$

$$\frac{d}{dt}\varepsilon = \frac{1}{\rho}\mathbf{P}_{s}\cdot\dot{\mathbf{S}} + q = -\frac{p}{\rho}\vec{\nabla}\cdot\vec{v} + q \quad \mathbf{\mathcal{F}} \quad \frac{d}{dt}\frac{v^{2}}{2} = -\vec{v}\cdot\vec{\nabla}\Pi - \vec{v}\cdot\vec{\nabla}\mathcal{P}$$
(14b)

which naturally yield the well-known generalization of the Bernoulli equation for steady-state regime of motion along the flow lines:

$$\frac{v^2}{2} + \mathcal{P} + \Pi = const_{\mathsf{P}} , \quad \mathcal{P} = \int \frac{dp}{\rho}, \quad (15)$$

where Π is the potential of mass forces, \mathcal{P} is the pressure function that is assumed to depends on ρ and T, and T is assumed to be a function of ρ .

For the ideal gas we obtain the following relations (here and below, subscripts T and ρ at partial derivatives are omitted):

$$dp = \frac{\partial p}{\partial \rho} d\rho + \frac{\partial p}{\partial T} dT = \frac{B}{\rho} d\rho + \frac{B_{\rho}}{T} dT. \quad (16)$$

The latter sum is actually a complete differential of pressure, provided that $B/\rho = RT \text{and} B_{\rho}/T = R\rho$, where R = const. Therefore, $B_{\rho} = B$ and, if these moduli are equal to pressure p (i.e., to isothermal value of the bulk elastic modulus), we arrive at a formula that coincides with the Clapeyron equation, while the differential of pressure p can be expressed as

$$dp = R \, d(\rho T). \tag{17}$$

In application to polytrophic processes, which constitute a broad subclass of barotropic processes, the relation $dp = n(\frac{p}{\rho})d\rho$ is valid provided that $T = (\frac{T_0}{\rho_0^{n-1}})\rho^{n-1}$ in relation (16). In this case, $B_n = n$ is a bulk elastic modulus in the given dynamic

np is a bulk elastic modulus in the given dynamic process.

In the case of adiabatic flows, i.e., for q = 0, it follows from Eqs. (14) – (14b) and (16) that

$$d\varepsilon = RT\rho^{-1}d\rho = d\hat{i} - d\frac{p}{\rho} = d\hat{i} - \frac{dp}{\rho} + \frac{p}{\rho}\rho^{-1}d\rho = d\hat{i} - d\mathcal{P} + RT\rho^{-1}d\rho$$

where \hat{i} is enthalpy. Therefore, $d\hat{i} = d\mathcal{P}$ and Eq.(15) can be written in the following quasi-equivalent form.

$$\frac{v^2}{2} + \hat{i} + \Pi = const_{\hat{i}},$$
(18)

so that energy balance trinomial (18) differs from (15) by a constant. Then, using Mayer's formula $R = c_p - c_v$, we obtain

$$d\varepsilon = c_{v}dT = RT\rho^{-1}d\rho \quad \boldsymbol{\vartheta} \quad d\ln T = (k-1)d\ln\rho \quad \boldsymbol{\vartheta} \quad \frac{T}{T_{0}} = \left(\frac{\rho}{\rho_{0}}\right)^{k-1}, k = \frac{c_{p}}{c_{v}}.$$

Using these relations and the Clapeyron equation, we eventually arrive at the classical Poisson's adiabatic equation, $p/p^k = const$. In the presence of external heat supply, $dq = Td\hat{e}$, where $d\hat{e}$ is increment of an entropy, we readily obtain the well-known formula

$$d\hat{e} = c_v d \ln \frac{p}{\rho^k}, \qquad (19)$$

which shows that for $d \ln (p/\rho^k) = 0$ in Eq. (19) (i.e., for dq = 0), the adiabatic flows of ideal gases are isentropic.

Thus, the formalism developed in this work, when applied to a particular case of gas flow (which is widely used in solving many practical problems) isfully consistent with the corresponding field of gasdynamics.

b) Steady-State Laminar Flow of a Fluid in a Cylindrical Round Tube with Smooth Walls at T = const

Conditions stipulated in the title of this subsection imply that we can set

$$v_z = v_z(z, r), v_{\varphi} = 0, \dot{B} \approx \ddot{B} \approx G \approx \ddot{G} \approx 0, B = B(z), \rho^{-1}\dot{G} = \rho^{-1}\mu = \upsilon = const.$$

Besides, restriction accepted in example S.1 also are maintained but at $\dot{G} \neq 0$.

In this case, it is natural to use a cylindrical coordinate system (r, φ , z), where z is measured along the tube axis as indicated on Fig.6a. Assuming in addition that the radial component v_r of velocity \vec{v} is negligibly small, the pressure and density will depend only on the axial coordinate: $z \ni p = p(z), \rho = \rho(z)$. This assumption poses rather strict limitations on the algorithm of solution of this problem.

In the given particular case, the equations of continuity (I) and momentum balance (II) reduce to the following relations

$$M(r) = \rho(z)v_z(r,z) \; \mathbf{\mathcal{F}} \; v_z = \frac{\rho_0}{\rho(z)}v(r), \quad (20)$$

$$\mu(\frac{\partial^2 v_z}{\partial r^2} + \frac{1}{r}\frac{\partial v_z}{\partial r} + \frac{\partial^2 v_z}{\partial z^2}) - \rho v_z \frac{\partial v_z}{\partial z} = B \frac{1}{\rho}\frac{d\rho}{dz}, \quad (21)$$

Where *M* is the mass flow rate $[kg/(m^2 s)]$ that depends

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only on *r*, ρ_0 is the density in the input cross section where the fluid flow enters the tube. It follows from Eq.(20) that v_z is described by an expression with separable variables.

Analysis shows that, for the low-gradient (layered) flow under consideration, the last term in parentheses on the left-hand side of Eq. (21)can be ignored and, for the existence of a single solution, it is necessary to set the values of pressure p_0 , p_1 in cross

sections 0–0 and 1–1 (fluid in- and outflow, respectively) and function $\rho(z)$ and to transform relation (21) into an ordinary differential equation with constant coefficients for the unknown function v(r).

Omitting the description of simple transformations and passing to dimensionless variables, we eventually obtain from Eqs. (20) and (21) (see also Fig. 6a) the following relations:

$$\frac{d^2\overline{v}}{d\overline{r}^2} + \frac{1}{\overline{r}}\frac{d\overline{v}}{d\overline{r}} + R_1(\overline{z})\overline{v}^2 = R_2(\overline{z}), \ R_1 = \frac{r_0^2 v_0}{l\upsilon}\frac{1}{\overline{\rho}^2}\frac{d\overline{\rho}}{d\overline{z}}, \ R_2 = -\frac{4}{\ln\overline{\rho_1}}\frac{1}{\overline{\rho}}\frac{d\overline{\rho}}{d\overline{z}},$$

$$\overline{v} = \frac{v}{v_0}, \ v_0 = -\frac{r_0^2}{4\rho_0 v} \frac{\Delta p}{l}, \ \Delta p = p_1 - p_0,$$

$$\overline{r} = \frac{r}{r_0}, \ \overline{z} = \frac{z}{l}, \ \overline{\rho} = \frac{\rho}{\rho_0}, \ \rho_1 = \exp(\Delta p/B),$$

where the characteristic velocity v_0 corresponds to the maximum value on the paraboloid profile of velocity according to the model of incompressible fluid.

Restricting the consideration to a linear approximation for the fluid density

 $\overline{\rho} = 1 + \Delta \overline{\rho} \ \overline{z}, \Delta \overline{\rho} = \overline{\rho}_1 - 1$, multiplying both parts of Eq. (22) by *dz*, and integrating over $\overline{z} \in [0,1]$, we eventually obtain the following ordinary nonlinear differential equation:

$$\frac{d^2\overline{v}}{d\overline{r}^2} + \frac{1}{\overline{r}}\frac{d\overline{v}}{d\overline{r}} + \overline{R}\overline{v}^2 = -4, \quad \overline{R} = -\frac{r_0^4}{4\upsilon^2\rho_0 l^2} \quad \frac{\Delta\overline{\rho}_1}{\overline{\rho}}, \quad \overline{v}_z = \overline{\rho}^{-1}\overline{v}.$$
(23)

v

Evidently, in the model of incompressible fluid $\overline{\rho}_1 = 1 \wedge \Delta \overline{\rho}_1 = 0$ **A** $\overline{R} = 0$ and a solution of Eq.(23)

corresponds to the classical *Poiseuille* velocity profile $\overline{v}_{z} = \overline{v} = 1 - \overline{r}^{2}$, representing a paraboloid of rotation.



Fig. 6: Fragment of the tube and dimensionless of velocity $\overline{v}(\overline{r})$ epures

Numerical solutions of Eq. (23) for liquids showed that, in the interval of pressure changes Δp corresponding to Re values in the field of laminar flow regimes, the effect of compressibility described by the term $\overline{R} \ \overline{v}^2$ is negligibly small. An analogous conclusion is valid for isothermal layered flows under conditions of normal and rarefied gases. As it was expected, the effect of compressibility, manifested by a significant

difference of the velocity $\overline{\nu}_z$ from its *Poiseuille* profile, is observed only for strongly rarefied gases. Fig.6b (solid curve) shows of the dimensionless *Poiseuille* velocity profile. Dashed curve shows the results of calculation using Eq. (23) for the following parameters: $r_0 = 5 \cdot 10^{-3}$ m, l = 1 m, B = 60550 Pa, $\rho_0 = 0.8$ kg/m³, $\upsilon = 1.5 \cdot 10^{-5}$ $^{5}m^2/s$, $\Delta p = 230$ Pa, Re = $4 \cdot 10^4$ and $\overline{R} = -0.76$. In this case $\overline{z} = 1$ and velocity is displayed to it meaning on the 2019

(22)

tube axis. As can be seen, differences between the two velocity $\overline{\nu}\,$ distributions are relatively small, although the Re value adopted in calculations corresponds in fact to a turbulent flow regime.

c) One-Dimensional Stationary Isothermal Efflux of the Ideal Liquid via a Nondivergent Nozzle

With a view to obtaining only a qualitative picture, let us consider a simple model with modulus *B*set to be constant (in particular, let fluid to be water with $B = 2.25 \cdot 10^3$ MPa). Fig. 7a shows a model scheme used in calculations. Spacer 1 separates two reservoirs (the left-hand one being of large volume), so

$$\mathsf{P} = B \int \frac{d \ln \rho}{\rho} \quad \boldsymbol{\Im} \quad \frac{v^2}{2} - \frac{B}{\rho_1} = -\frac{B}{\rho_0}$$

or with allowance for a physical result

$$v^{2} - \frac{2B}{M}v + \frac{2B}{\rho_{0}} = 0$$
 \Im $v = \frac{B}{M} - \sqrt{\frac{B^{2}}{M^{2}} - \frac{2B}{\rho_{0}}}$, (24b)

Where *M* is the mass flow rate. For $\rho_0 = const$ and decreasing density ρ_1 (and, hence, pressure ρ_1 , since $p_1 - p_0 = B \ln \frac{\rho_1}{\rho_0}$) from ρ_0 to $\rho_1^* = \frac{\rho_0}{2}$, the flow velocity in the right-hand reservoir reaches a critical value of $v^* = \sqrt{\frac{2B}{\rho_0}} = \sqrt{\frac{B}{\rho_1^*}}$ with the well-known that liquid can flow from left to right only via a hole with hermetically mounted nozzle 2, provided that $\rho_1 < \rho_0$. The density ρ_0 and pressure ρ_0 in some inlet cross section 0-O(sufficiently far from the left input edge of the nozzle) represent the "retardation" parameters ($v_0 = 0$). Cross sections *i-i* and 1-1 correspond to the right-hand boundary of the initial region with constant steady-state flow velocity v and the nozzle output section, respectively.

With neglect of mass forces, assuming small radial dimensions of the nozzle, Eq. (15) yields

$$\boldsymbol{\vartheta} \quad v = \sqrt{2B(\rho_1^{-1} - \rho_0^{-1})}.$$
 (24a)

phenomenon of efflux blocking. For water under conditions close to normal with $\rho_1^* = 10^3$ kg/m³ and $p_1^* = 10^5$ Pa, the flow considered from the abstract point of view (i.e., without a change in the physical state of medium and its flowability properties) will proceed purely theoretically for $\rho_0 = 2 \cdot 10^3$ kg/m³and $\rho_0 \approx 1560$ MPa at the efflux with a sound velocity of $v^* = 1500$ m/s.





Fig. 7: Qualitative estimation of compressibility effect on velocity of fluid outflow from hydraulic nozzle

Fig. 7b shows the plot of flow velocity *v* versus $\Delta p = p_0 - p_1$ (in the interval of practically significant variation of this parameter) in steady-state regimes in cross section 1-1, calculated using the proposed model with allowance for compressibility (solid curve), which almost coincides with the velocity profile according to the model of incompressible liquid. The dashed curve shows the excess velocity $\Delta vaccording$ to the latter model (plotted on a greater scale), while the dash-dot curve represents the corresponding excess density

$$\Delta \rho = \rho_0 - \rho_1$$

Fig. 7c shows the analogous plots of velocity *v* for the models of compressible (solid curve) and incompressible (dashed curve) liquids in the vicinity of a hypothetical zone of efflux blocking. As can be seen, a significant difference of velocity *v* for the two theoretical models under comparison is only observed at very large pressure differences Δp , which are difficult or even impossible to achieve in practice. These results exhibit positive correlation with a conclusion made in the preceding subsection **S.2** concerning a negligibly small influence of the compressibility of fluids on the dynamic

process in steady-state layered flows. However, it is hardly possible that this conclusion can also be expanded to turbulent flows, which are principally threedimensional and non-stationary and (according to both theoretical and experimental data [5]) have derivatives with respect to (\vec{x}, t) that exceed by many orders of magnitude the values taking place in laminar regimes of fluid motion.

IV. Conclusion

- 1. The foundations of the non sacramental theory of continuous mediums thermomechanics have been developed.
- 2. We obtained new phenomenological closed system of equations with unknown functions are the fundamental substances of the matter-field: the specific mass ρ , the momentum \vec{v} , the increase of internal energy ε , the velocity $\vec{\Lambda}$ of the torsion motion direct turn of the marked *e.p.m.* for unit of time, determining the inertial moment at it appearance in the course of viscous turnings of the real C-mediums elementary particles.

 A large group of physical coefficients / parameters / indicators with qualitatively different weighting contributions to balance equations for yielding deformation C-mediums and being in various of aggregate conditions requires its experienced predefinition, and essentially - the initial establishment. Therefore, it can be assumed that the article is oriented on the future and at professionals, theoreticians and experimentalists which are working creatively in the field of research strongly perturbed dynamics of continuous media in nature and artifact of various purposes.

Notations *

 \dot{F} - vector by volume forces;

 $\mathbf{\hat{S}}_{d}$ - deviators of the symmetric transposed tensors for gradients: deformations $\mathbf{S}\left(\frac{d\vec{u}_{d}}{d\vec{\mathbf{x}}}\right)^{T}$, their velocities

 $\dot{\mathbf{S}}\left(\frac{d\vec{v}_d}{d\mathbf{\tilde{x}}}\right)^*$ and *pseudo*-accelerations (or simple "accelerations") $\ddot{\mathbf{S}}\left(\frac{d\vec{a}_d}{d\mathbf{\tilde{x}}}\right)^*$;

 $\stackrel{i}{B}$, $\stackrel{i}{G}$, $\stackrel{i}{R}$ and $\stackrel{i}{N}$ – modules of deformations of volume and shears ($i = \emptyset$), its velocity ($i = \bullet$), "acceleration" ($i = \bullet \bullet$) from strain tensors \mathbf{P}_s , \mathbf{P}_d , $\mathbf{P}^{(a)}$ and moment of strain $\mathbf{M}^{(a)}$ accordingly;

I, 1 - the unit tensor and the Heaviside step function;

 ξ – for F-mediums is distance by strong interaction with wall, or with boundary surface of two-phases jets mixing;

 I_x - index of a binary interacting (see also [8]);

 c_v - specific heat at constant volume;

 J, c_J , \mathfrak{B}_J – moment of inertia; coefficient of correction and the weighted mean wave number characterizing the local spatial topology of the marked *e.p.m.* by normal to direction of $\vec{\Lambda}$;

 $\vec{\Lambda}$ –vector of turn of the marked *e.p.m.* for unit of time and related to one radian;

 $\mathbf{\hat{\Lambda}}, \mathbf{\hat{N}}_{\Lambda}, \mathbf{\hat{R}}_{\Lambda}, J^{0}$ -antisymmetric tensors of the turn $\mathbf{\Lambda}e.p.m.$ as a single but deformable whole, its velocity $\mathbf{\hat{\Lambda}}$ and "acceleration" $\mathbf{\ddot{\Lambda}}$; further: physical coefficients of these acts influence and the *distinctive* moment of inertia accordingly;

 $ec{q}_{\mathit{cd}}$, $ec{q}_{\mathit{r}}$ - vectors of conductive and radiation heat transfer;

 \vec{u}_d , \vec{v}_d , \vec{a}_d -vectors of deformation, it velocity and "acceleration" from removal and rotation shears in *E*-system counting; second word-to-word index 0 marks the initial conditions;

 \vec{w} , \vec{w}_d - additional vectors that simplify the formulas; \vec{w}_c - the proper referring to forward motion of *e.p.m.*;

 λ - heat conductivity coefficient; μ - dynamic viscosity coefficient;

 μ_{β} , μ_{b} , μ_{g} – integrator factors;

I - criterion in relations (C) meets to increment of wave specters with modulus of the wave number ϖ_s ;

 $\vec{u}_d^{\bullet}, \vec{u}_d^{\bullet}$ - modifications of the vector of deformation and its modulus related to linear scale $I = \varpi_s^{-1}$;

 $\mathbf{U} = [\mathbf{u}_{ij}] \mathbf{U} = [\mathbf{v}_{ij}] \mathbf{a} = [\mathbf{a}_{ij}], i \wedge j = \overline{1,3}$ - tensors of the removal, in quantum of time, it velocity, "acceleration";

si, eo, et., ubi, ad, edo, utlex, vel, solid media, liber/iunetus turbulences-from Lat. designations: "if", "then", "and", "where", "when", "since", "usually", "or", "solid medium", "free/constrained turbulence respectively";

•, ••, \times – scalar, biscalar, vector products;

 $\vec{\nabla}_{\vec{x}}$ – operator of Hamilton in *E*-system of counting;

 \land,\lor,\cup,\ni,\in , \varnothing – logical "and", "or", "union", "so", "belongs", "empty set".

e.p.m., FWS, FWN - elementary particle of medium, frequency-wave spectrums / numbers of its e.p.m..

^{* -} mainly not explained into text.

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Fig. 1: Schematic representations of $L \wedge E$ - systems: a, b- separate; c - combined



Fig. 2: The instantaneous position of the labeled/marked particles of the medium. Actual particle - darkened volume; distortions: shear - bar loop, torsion - bar-dotted momentary axis to the vector of the torsion velocity $\vec{\Lambda}$ of inertial turning of marked e.p.m. for the unit of time, in one radian and point c is center of inertia / mass. Designations $i_{A,k}$, $k = \overline{1,3}$ are the trajectory three-orthogonal *bench-mark* for the given e.p.m.