



## The Scientific Graph Programming Paradigms of Systems from Modules to the Application Areas

By E. M. Lavrischeva

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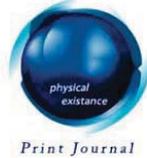
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E. M. Lavrischeva

*Annotation-* The mathematical basics of graph paradigm programming of applied systems (AS) are presented. The vertices of graph are been the functional modules of the systems and the arcs define the connections between them. The graph is represented by an adjacency and reach ability matrix. A number of graph' program structures and their representation by mathematical operations (unions, connections, differences, etc.) are shown. Given the characteristics of graph structures, complexes, units, and systems created from the modules of the graph. The method of modelling the system on the graph of modules, which describe in the programming languages (LP) and the advanced operations of association (link, assembling, make, building, config etc.). The standard of configuration (2012) Assembly of heterogeneous software elements in AS of different fields of knowledge is made. A brief description of modern and future programming paradigms for formal theoretical creation of systems from intelligent and service-components of the Internet is given. The modules and AS are protected and quality assessment. There are giving the new direction of modern paradigms programming in the near future.

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## I. INTRODUCE. THE GRAPH THEORY AND PARADIGMS OF PROGRAMS

Programming theory is a mathematical science, the object of study of which is the mathematical abstraction of the functions of programs with a certain logical and information structure, focused on computer execution. With the advent of the LP began to develop new methods of analysis of algorithms of AS problems, the graph theory for the representation the structure AS by separate programs elements, displaying them in the vertices of the graph to create a complex structure of AS (programs, aggregate, large program, system, etc.). Programs elements of missile defense were first called modules, programs, then objects, components, services, etc. For the formal specification of these elements were formed the corresponding *programming paradigms*, allowing from the point of view of the theory and graphs to describe the problems of different AS (medicine, biology, chemistry, genetics, etc.).

## II. GRAPH THEORY OF PROGRAMS FROM MODULES

The basis for the creation of systems of modules was the method of assembling the graph (70-80 years of the last century) heterogeneous modules in specialized

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software packages (Lipaev V. V.) and in the system APROP of ES OS (IBM-360) [1, 2]. Formed Assembly programming [3-5], which "provided the building is already existing individual pieces of software (such reuses) in the complex structure" [6]. The interface of the modules was described initially in a special description language link, and then in equivalent operations: make BSD, Java (1996); config SPAROL, building, assembling Grid (2002), etc. [7-12]. And after 90-x there were standard languages of the description of these operations of IDL, API, WSDL and the standard statement of config of the IEEE 828-2012 standard (Configuration Management) for receiving a configuration file of any application system from ready modules, objects, components, services and other resources.

A module is a formally described program element that displays certain AS function that has the property of completeness and connectivity with other elements according to the data specified in the interface part of the description. From a mathematical point of view, a module is a mapping of a set of initial data  $X$  to a set of output  $Y$  in the form  $M: X \rightarrow Y$ .

A number of restrictions and conditions are imposed on  $X$ ,  $Y$  and  $M$  to make the module an independent program element among other types of program objects [1-3].

Types of connections between modules via input and output parameters are as follows:

- 1) linking of control:  $CP = K_1 + K_2$ , where  $K_1$  is the coefficient of the calling mechanism;  $K_2$  is the coefficient of transition from the environment of the calling module to the environment of the called;
- 2) Linking of data:  $CI = \sum_{i=1}^n K_i F(x_i)$ , where  $K_i$  - the weight coefficient iron of the parameter;  $F(x_i)$  - the element function for the parameter  $x_i$ .

Coefficients  $K_{id} = 1$  - for simple variables and  $K_{id} > 1$  - for complex variables (array, record, etc.).  $F(x_i) = 1$  if  $x_i$  - a simple variable and  $F(x_i) > 1$  if complex.

The program, modular structure is given by the graph  $G = (X, E)$ , where  $X$  - a finite set of vertices;  $E$  - a finite subset of the direct product of  $X$  z on the set of relations on the arcs of the graph. The program structure represents a pair  $S = (T, \chi)$ , where  $T$  - a model of a program, modular structure;  $\chi$  - a characteristic function given on the set of vertices  $X$  of the graph  $G$ .

The value of the characteristic function  $\chi$  is defined as:

$X(x) = 1$  if the module with vertex  $x \in X$  is included in the modular system;

$X(x) = 0$  if the module with vertex  $x \in X$  is not included in the modular system and is not accessed from other modules.

**Definition 1:** Two models of program structures  $T_1 = (G_1, Y_1, F_1)$  and  $T_2 = (G_2, Y_2, F_2)$  are identical if  $G_1 = G_2$ ,  $Y_1 = Y_2$ ,  $F_1 = F_2$ . The  $T_1$  model is isomorphic to the  $T_2$  model if  $G_1 = G_2$  between sets  $Y_1$  and  $Y_2$  exists an isomorphism  $\phi$ , and for any  $x \in X$   $F_2(x) = \phi(F_1(x))$ .

**Definition 2:** Two program structure  $S_1 = (T_1, \chi_1)$  and  $S_2 = (T_2, \chi_2)$  are identical if  $T_1 = T_2$ ,  $\chi_1 = \chi_2$  and the structures  $S_1$  and  $S_2$  are isomorphic, then  $T_1$  is isomorphic to  $T_2$  and  $\chi_1 = \chi_2$ .

The concept of isomorphism of program structures and their models is used in the specification of the abstraction level at which operations on these structures are defined. For isomorphic graph objects, operations will be interpreted in the same way without orientation to a specific composition of program elements, provided that such operations are defined over pairs  $(G, \chi)$ . The software module is described in the LP and has an interface section in which external and internal parameters are set for data exchange between related modules through interface (Call/RMI) operations, etc.

*The interface* defines the connection of heterogeneous software modules according to the data and the way they are displayed by programming systems with the LP. Its main functions are: data transfer between program elements (modules), data conversion to the equivalent form and transition from the environment and platform of the called module to the caller and back. Functions of conversion of different, non-equivalent data types is carried out with the help of a previously developed library of 64 primitive functions for heterogeneous data types of LP in the APROP system [1-5] and included in the common system environments of the OS (IBM, MS, Oberon, UNIX, etc.).

In practice, the assembly method of software modules is performed by operations (link, make, assembling, config. weaver) special programs [1] OS libraries (OS ES, IBM, MS.Net, etc.), a builder of complex applications in OS RV for SM computers, complication modules for ERM "Elbrus" are used. In these operations and interface modules and data type conversion library [1, 2].

Next, we consider the mathematical theory of graphs of software modular structures and mathematical operations (union, projection, difference, etc.) implementation of ways of linking the graph modules and the semantics of the data transformation by the vertices of the graph. Software modules are described in modern LP and with help of the new paradigms programming.

#### a) Definition of a modular structure graph

To represent modular structures, we use the mathematical apparatus of graph theory, in which the graph  $G$  is treated as a pair of objects  $G = (X, E)$ , where  $X$  - a finite set of vertices, and  $E$  is a finite subset of the direct product of  $X \times X \times Z$  - arcs of the graph, corresponding to a finite vertex (Fig. 1).

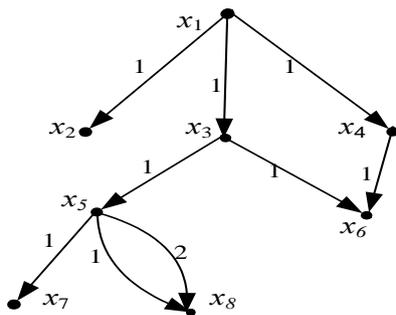


Fig. 1: Graph of program from modules

The set of arcs of the graph have the form:  $E = \{(x_1, x_2, 1), (x_1, x_3, 1), (x_5, x_8, 1), (x_5, x_8, 2)\}$  [1-7]. Based on this definition, we can say that the graph  $G$  is a multi-graph, since its two vertices can be connected by several arcs. To distinguish these arcs introduced their numbering positive integers - 1, 2. (Fig.1) and vertices of the graph  $x_1$ ,

$x_2, \dots, x_8$  form a set of  $X$ . From the module corresponding to the vertex  $x_5$ , there are two calling operators to the modules, with vertices  $x_7, x_8$ .

**Definition 3:** A program aggregate is a pair  $S = (T, \chi)$ , where  $T$  - a model of the program modular structure of the aggregate;  $\chi$  - a characteristic function defined on the set of vertices  $X$  of the graph of the modular structure  $G$ . The value of the  $\chi$  function is defined as follows:

- $\chi(x) = 1$  if the module corresponding to the vertex  $x \in X$ , - included in the unit;
- $\chi(x) = 0$  if the module corresponding to the vertex  $x \in X$ , - not included in the software unit, but it is accessed from other modules previously included.

**Definition 4:** The model of the program structure of the program unit is an object described by the triple  $T = (G, Y, F)$ , where  $G = (X, E)$  - a directed graph of a modular structure;

$Y$  is a set of modules included in the program aggregate;  
 $F$  is a correspondence function that puts an element of the set  $y$  at each vertex  $X$  of the graph.

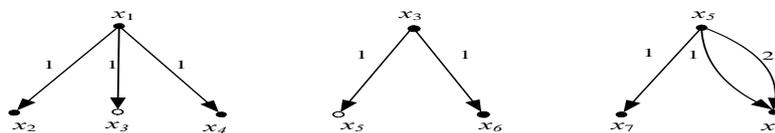
Function  $F$  maps  $X$  to  $Y$ , (1)  

$$F: X \rightarrow Y.$$

In General, an element from  $Y$  can correspond to several vertices from the set  $X$  (which is typical for the dynamic structure of the aggregate) [5, 15, and 20].  
 The graph of software aggregates has the following properties:

- 1) Graph  $G$  has one or more connectivity elements, each of which represents an acyclic graph, i.e. does not contain oriented cycles;
- 2) In each graph  $G$  is allocated a single vertex, which is called the root and is characterized by the fact that there are no arcs included in it and the corresponding module of the software unit is performed first;
- 3) Cycles are allowed only for the case when some vertex has a recursive reference to itself. Typically, this feature is implemented by the compiler with the corresponding *LP* and this type of communication is not considered by the intermodule interface. Therefore, such arcs are not included in the graph. The exception to the consideration of other types of cycles is due to the fact that some modules will have to remember the history of their calls in order to return control correctly, which contradicts the properties of the modules;
- 4) An empty graph  $G_0$  corresponds to an empty program structure.

Next, the graph  $G$  will be used to illustrate mathematical operations on modular structures. For Fig.2. three types of subgraphs are shown and their description is given.



*Fig. 2:* The graphs of modules structures

A sub graph - a fragment of a software aggregate  $G^s = (X^s, E^s)$  for whose functions one of two conditions is satisfied:

$C(S) = 1$ , if  $\chi(x) = 1$  for any  $x$  of  $X$ ;

$C(S) = 0$ , if there is  $x$  such that  $\chi(x) = 0$ ;

$R(S^s) = 0$ , if the modular structure is part of a higher-level structure and  $R(S) = 1$  if the software assembly is ready to run.

Given these combinations  $C$  and  $R$ , the subgraph can be: open ( $C = 0, R = 0$ ); closed at the top ( $C = 0, R = 1$ ); closed at the bottom ( $C = 1, R = 0$ ).

The graph of the module ( $m$ ) is represented as:  $G^m = (X^m, E^m)$ . It contains a single vertex  $x \in X^m$  for which  $\chi(x_j) = 1$ . This vertex is the root. An arc of the form  $(x_j, x_e, k)$  means calling the module to the corresponding vertex  $x_j$ , i.e. to the module with the vertex  $x_j$ . The dark circle on the+ graph corresponds to the vertex for which  $\chi(x) = 1$ ; light -  $\chi(x) = 0$ .

Program graph  $G^p = (X^p, E^p)$  which is performed  $C(S^p) = 1; R(S^p) = 1$ . An example of a graph of such a program modular structure is shown in Fig. 1.

The graph of the complex  $G^c = (X^c, E^c)$  consists of  $n$  connectivity components ( $n > 1$ ), each of which is a graph and includes:  $G^c = G_1^p \cup G_2^p \cup \dots \cup G_n^p$ , where  $X^c = X_1^p \cup X_2^p \cup \dots \cup X_n^p$  и  $E^c = E_1^p \cup E_2^p \cup \dots \cup E_n^p$ .

These definitions of the graph of the program module, program and complex are used for the process of assembling the modules. These concepts may differ from similar ones, which are considered in other contexts of the work.

*b) Matrix representation of graphs from program elements of module type*

To determine the main operations on software structures, we use the mathematical apparatus of the matrix representation of graphs in the form of an adjacency and reachability matrix. That is, the graph is represented by the matrix  $M = m(i, j)$  of adjacency and is proved by the reach ability matrix [5, 11-13]. The element of the matrix  $m_{ij}$  determines the number of call operators with index  $i$ , to the module with index  $j$ .

In addition to the adjacency matrix (calls), the characteristic vector  $V_i = \chi(x_i)$  for  $i$ -elements is used. For a modular structure graph (Fig. 1) characteristic vector and adjacency matrix have the form:

$$V = \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} \quad M = \begin{pmatrix} 0 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix} \quad (2)$$

We analyze adjacency matrices and characteristic vectors for subgraphs and graphs of modular structures corresponding to different types – program, complex, aggregate, etc. For subgraphs (Fig.2) vectors and matrices have the form:

$$V_3^s = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \quad M_3^s = \begin{pmatrix} 0 & 1 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}; \quad V_1^s = \begin{pmatrix} 1 \\ 1 \\ 0 \\ 0 \end{pmatrix},$$



$$M_1^s = \begin{pmatrix} 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}; \quad V_5^s = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \quad M_5^s = \begin{pmatrix} 0 & 1 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad (3)$$

For the program graph (Fig. 1) the characteristic vector and the matrix of calls coincide with  $V$  and  $M$ , respectively, and determine the form (2), in which all elements of  $V$  are equal to one. In the case of the complex, the characteristic vector and the call matrix have the following form:

$$V^c = \begin{pmatrix} V_1^p \\ V_2^p \\ \dots \\ V_n^p \end{pmatrix}, \quad M^c = \begin{pmatrix} M_1^p & 0 & \dots & 0 \\ 0 & M_2^p & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & M_n^p \end{pmatrix} \quad (4)$$

Here  $V_i^p$  and  $M_i^p$  ( $i = \overline{1, n}$ ) denote the characteristic vector and the adjacency matrix for the graph of the  $i$ -th program included in the graph of the complex. In the future, the matrix representation is used when performing mathematical operations on software structures.

### c) The relation of the reach ability graph of program structures

Let  $G = (X, E)$  - a graph of a program of modular structure;  $x_i, x_j$  - vertices belonging to  $X$ . If there is an oriented chain from  $x_i$  to  $x_j$  in the graph  $G$ , then the vertex  $x_j$  is reachable from the vertex  $x_i$ . The following statement is true: if the vertex  $x_j$  is reachable from  $x_l$  - и  $x_j, x_l$  - from  $x_i$ , then  $x_l$  is reachable from  $x_i$ . The proof of this fact is obvious.

Consider a binary relation on the set  $X$  that determines the reach ability of one vertex of a graph to another. We introduce the notation  $x_i \rightarrow x_j$  - reach ability of the vertex  $x_j$  from  $x_i$ . The relation is transitive. Denote by  $D(x_i)$  the set of vertices of graph  $G$  reachable from  $x_i$ . Then the equality

$$\overline{x_i} = \{x_i\} \cup D(x_i) \quad (5)$$

of determines the transitive closure of  $x_i$  in relation to the achievability of tops. We prove the following theorems.

*Theorem 1.* For the selected element of connectivity of the graph of the program structure, any vertex is reachable from the root corresponding to the given vertex of the graph. i.e. the equality ( $x_i$  - root vertex)

$$\overline{x_i} = \{x_i\} \cup D(x_i) = X. \quad (6)$$

*Evidence.* Suppose the vertex  $x_i$  ( $x_i \in X$ ) is unattainable from  $x_i$ , Then  $x_i \notin \overline{x_i}$  and the set  $X' = X \setminus \overline{x_i}$  - not empty. Since the selected component of the graph is connected, there is a vertex  $x_j \in \overline{x_i}$  and a chain  $H(x_i, x_j)$ , leading from  $x_i$  to  $x_j$ . Based on the acyclicity of the graph  $G$ , in  $X'$  there should be a simple chain  $H(x_i, x_j)$ , where the vertex  $x_i$  does not include arcs (this chain can be empty if  $X'$  consists only of  $x_j$ ). Consider the chain  $H(x_i, x_j) = H(x_i, x_i) \cup H(x_i, x_j)$ . This means that the module  $x_i$  is reachable from vertices  $x_i$  and  $x_j$  and both vertices contain no incoming arcs. This

contradicts the definition of a graph of a modular structure with a single root vertex. The theorem is proved.

Thus, the results of theorem1 reinforce the requirement that there are no oriented cycles in the graph of the program structure.

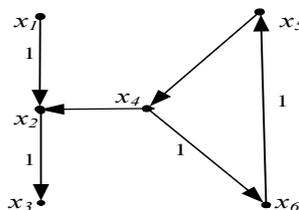


Fig. 3: A graph that contains directed cycle

The results of this theorem are important to substantiate the requirement of the absence of oriented cycles in the graph of the program structure with respect to the notion of reachability. Consider the graph shown in Fig. 3. From this figure it is clear that the graph contains a directed cycle and modules corresponding to vertices  $x_4, x_5, x_6$  will never be executed.

Thus, the results of theorem1 reinforce the requirement that there are no oriented cycles in the graph of the program structure.

$$\mathbf{A} = \begin{pmatrix}
 x_1 & x_2 & x_3 & x_4 & x_5 & x_6 & x_7 & x_8 \\
 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\
 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
 \end{pmatrix} \tag{7}$$

We analyze the matrix representation of the reach ability relation for the graph of the program structure Fig. 1 with the reach ability matrix  $A$ , which has the form (7). Coefficient  $a_{ij} = 1$  if the module corresponding to the index  $j$  is reachable from the module corresponding to the index  $i$  the Following results are based on the following theorem from graph theory.

*Theorem 2:* The coefficient  $m_{ij}$  of the  $l$ -th degree of the adjacency matrix  $M^l$  determines the number of different routes containing  $l$  arcs and connecting vertex  $x_i$  to the vertex of the  $x_j$ -oriented graph. The proof of this theorem is given in [20]. Consider the following three consequences of this theorem.

*Corollary 1.1:* Matrix  $\overline{M} = \sum_{i=1}^n M^i$ , where  $M$  is the adjacency matrix of a directed graph with  $n$  vertices coincides up to the numerical values of the coefficients with the reachability matrix  $A$ .

*Evidence.* In a directed graph containing  $n$  vertices, the maximum path length without repeating arcs cannot exceed  $n$ . Therefore, the sequence of degrees of the adjacency matrix  $M^i$ , where  $i = 1, 2, \dots, n$  determines the number of all possible paths in the graph

with the number of arcs  $\leq p$ . Let the coefficient  $\overline{m_{ij}}$  of the matrix  $M$  be different from zero. This means that there is a degree of matrix  $M^i$  in which the corresponding coefficient  $\overline{m_{ij}}$  is also nonzero. Therefore, there is a path from vertex  $x_i$  to  $x_j$ , i.e. vertex  $x_j$  is reachable from  $x_i$ . This consequence determines the connection of the matrix of calls of the graph of the modular structure  $M$ , coinciding with the reachability matrix  $A$ , and determines the algorithm for constructing the latter.

*Corollary 1.2.* Let there be a coefficient  $m_{ii} > 0$  for some  $i$  in the sequence of degrees of the adjacency matrix  $M^i$ . Then there is a cycle in the original graph.

*Evidence.* Let  $m_{ii} > 0$  for some  $i$ . Therefore  $x_i$  reachable from  $x_i$ , i.e. there is a cycle. According to the theorem, this cycle has  $i$  arcs (generally repeated).

*Corollary 1.3.* Let the  $n$ -th degree of the adjacency matrix of the  $M^n$  of the acyclic graph coincide with the zero matrix (all coefficients are zero).

*Evidence.* If the graph is acyclic, then the simplest path cannot have more than  $n - 1$  arcs.

If  $M^n$  has a coefficient other than zero, then there must be a path consisting of  $n$  arcs. And this way can only be oriented cycle. Therefore, all coefficients of  $M^n$  for an acyclic graph are zero. This consequence provides a necessary and sufficient condition for the absence of cycles in the graph of a modular structure.

For acyclic graphs, the reachability ratio is equivalent to a partially strict order. The transitivity of the reachability ratio was considered above. Anti-symmetry follows from the absence of oriented cycles: if the vertex  $x_j$  is reachable from  $x_i$ , then the opposite is not true.

We introduce the notation  $x_i \not\prec x_j$  if vertex  $x_j$  is reachable from vertex  $x_i$ .

Let  $G = (X, E)$  be an acyclic graph corresponding to some program structure.

Consider the decreasing chain of elements of a partially ordered set  $X$ :  $x_{i1} > x_{i2} > \dots > x_{in} \dots$ , where “ $>$ ” denotes the reachability ratio.

Since  $X$  is finite, the chain breaks. The vertex  $x_{in}$  has no outgoing arcs, i.e. the element  $x_{in}$  is minimal (it corresponds to a module that does not contain access to other modules). The maximum element in the set  $X$  is the root vertex.

#### d) Mathematical operations on the graph elements

Mathematical operations ( $\cup, \cap, /, +, -, P, C, R$ ) on graphs are performed at the level of abstractions of elements of program structures that lead to changes in graph elements and characteristic functions of systems:  $S = (G, \chi)$  [20].

Let  $S_1 = (G_1, \chi_1)$  and  $S_2 = (G_2, \chi_2)$  be two graphs of program structures  $G_1 = (X_1, E_1)$  and  $G_2 = (X_2, E_2)$  respectively.

We introduce the following notations:

$D(x)$  – the set of vertices reachable from the vertex  $x$ ;

$D^*(x)$  – the set of vertices from which vertex  $x$  is reachable.

The same symbols are used for the same vertices included in the graphs  $G_1$  and  $G_2$ . The main operations on the program structures are discussed below

Merge (join) operation 
$$S = S_1 \cup S_2 \quad (9)$$

is intended to form a graph of the structure of the complex and is formally defined as follows  $S_1$  and  $S_2$  – any program structures that satisfy the definitions of claim 1:

$$G = G_1 \oplus G_2, \quad X = X_1 \oplus X_2, \quad E_1 \oplus E_2, \tag{10}$$

where the symbol denotes a direct sum provided:

$$\begin{aligned} \chi(x) &= \chi_1(x), \text{ if } \chi \in X_1. \\ \chi(x) &= \chi_2(x), \text{ if } \chi \in X_2. \end{aligned}$$

The same vertices included in  $G_1$  and  $G_2$  are represented by different objects in the operations of combining program structures. The characteristic vector and adjacency matrix of the program structure  $S$  are defined as follows:

$$V_{1,2} = \begin{pmatrix} V_1 \\ V_2 \end{pmatrix}, \quad M_{1,2} = \begin{pmatrix} M_1 & 0 \\ 0 & M_2 \end{pmatrix}, \tag{11}$$

where  $V_{1,2}$  and  $M_{1,2}$  are characteristic vectors and adjacency matrices of modular structures  $S_1$  and  $S_2$  respectively. This operation is associative, but not commutative – the order of the operands determines the order of the components of the complex.

It should be noted that if the operands  $S_1$  and  $S_2$  satisfy the conditions for defining program structures, the result  $S$  will also satisfy the same requirements. The join operation increases the number of connected graph elements. In addition, the column structures may themselves have multiple items of connectedness. For the rest of the operation counts of the operands and result are the only element of connection.

*The connection operation.* We denote by  $x_i$  and  $x_j$  the root vertices of graphs  $G_1$  and  $G_2$  of program structures  $S_1$  and  $S_2$ , respectively. This operation

$$S = S_1 + S_2, \tag{12}$$

which is executed if these structures meet the following conditions:

set  $X' = X_1 \cap X_2$  not empty;  
vertex  $x_j \in X'$  and  $\chi(x_j) = 0$ ;

$$D^*(x) \cap D(x) = \emptyset \text{ for every } x \in X', \text{ where } D^*(x) \in X_1 \text{ и } D(x) \in X_2;$$

$$G = G_1 \cup G_2, \quad X = X_1 \cup X_2, \quad E = E_1 \cup E_2, \tag{13}$$

The characteristic function  $\chi$  is satisfied under the condition:

$$\begin{aligned} \chi(x) &= \chi_1(x), \text{ if } x \in X_1 \setminus X'; \\ \chi(x) &= \max(\chi_1(x), \chi_2(x)) > 0 \text{ if } x \in X', \\ \chi(x) &= \chi_2(x), \text{ if } x \in X_2 \setminus X'. \end{aligned}$$

First condition means that there are common vertices in graphs  $G_1$  and  $G_2$ . According to the second condition, the root vertex  $G_2$  belongs to the common part and for  $S_1$  the object corresponding to  $x_j$  is not included in the program structure yet.

The third condition prohibits the existence of cycles in the result graph. Indeed, if there is  $x_n \in D^*(x) \cap D(x)$ , then  $x_n > x$  and  $x > x_n$ , then this means the existence of a cycle.

If  $S_1$  and  $S_2$  satisfy the above conditions, the connection operation is partial.

Let us determine whether the result of the connection operation belongs to the class of program structures. Since  $X'$  is not empty, the graph  $G$  has one connected component. The root vertex of the graph  $G$  is  $x_i$ . The graph  $G$  itself has no oriented cycles, i.e. is acyclic.

Thus,  $S$  belongs to the class of program structures under consideration.

This connection operation is not commutative and is generally not associative. To show that this operation is not associative, consider the result  $S = (S_1 + S_2) + S_3$ , where the root vertices of graphs  $G_2$  and  $G_3$  are part of the vertices of graph  $G_1$  and  $X_2 \cap X_3 \neq \emptyset$ .

Then the result of the  $S_2 + S_3$  join operation is undefined.

*The operation of projection.* Let  $S_1 = (G_1, \chi_1)$  be a program structure and  $x_i \in X_1$ . The operation of projection of this structure to the top of the graph  $S_1$  is denoted as  $S = P_{rx_i}(S_1)$  and is defined as

$$G(X, E), \quad X = \bar{x}_i, \quad E = \{(x_i, x_j, K) \mid x_i, x_j \in X\}, \quad (14)$$

for the characteristic function is  $\chi(x) = \chi_1(x)$ , if  $x \in X$ . The projection operation defines the program structure  $S_1$  in the structure  $S$ . let's check the belonging of the structure  $S$  to the class of the considered program structures. If the graph of the structure  $S_1$  is connected acyclically, then the same properties will be possessed by the graph  $G$ . There is a single root vertex  $x_i$  in the graph  $G$ . Thus, the program structure  $S$  belongs to the class under consideration.

*The difference operation* for program structures is defined as follows. Let  $S_1 = (G_1, \chi_1)$  be a program structure and  $x_i \in X_1$ . The difference operation is performed on this structure and its projection to the vertex  $x_i$  of the corresponding graph ( $x_i$  is not the cortical vertex of the graph  $G_1$ ). Formally, the difference operation of the program structure has the form:

$$S = S_1 - P_{rx_i}(S_1), \quad (15)$$

and defined as follows

$$G = (X, E), \quad X = (X_1 \setminus \bar{x}_i) \cup X'$$

$$\Gamma = \{(x_i, x_i, K) \mid x_i, x_i \in X\}, \quad (16)$$

where the set  $X'$  consists of such elements for which

$$X' = \{x'_j \mid (x_j \in X_1 \setminus \bar{x}_i) \& (x'_j \in \bar{x}_i) \& (x_j, x'_j, K) \in E\} \quad (17)$$

Here, the characteristic function  $\chi$  is defined as:

$$\chi(x) = \chi_1(x), \text{ если } x \in X_1 \setminus \bar{x}_i;$$

$$\chi(x) = 0, \text{ если } x \in X'.$$

The set  $X$  includes vertices that are not included in the set  $\bar{x}_i$ , and those vertices  $\bar{x}_i$  that include arcs from vertex  $X_1 \setminus \bar{x}_i$  (sets  $X'$ ). The characteristic function for elements  $x' \in X'$  is zero. The difference operation is the inverse of the join operation, i.e. the equality is performed:

$$S - p_{rx_i}(S) + p_{rx_i}(S) = S. \quad (18)$$

Let us check that  $S$ , defined in (15), belongs to the class of program structures. If the graph is  $G$ , connected and acyclic, then the graph  $G_I$  will have the same properties. The root vertex  $G$  is the same as the root vertex  $G_I$ . Thus,  $S$  satisfies the conditions for determining the program structure given in paragraph 1.

Let  $S^*$  be the set of program structures given by the direct product  $G^* \times \chi^*$ , where  $G^*$  and  $\chi^*$  are the set of graphs and the set of characteristic functions. Denote by  $\Omega = \{U, \cap, /, +, -\}$  - set of mathematical operations on program structures and  $P, C$  and  $R$  - predicates of:

$$\Omega = \{U, \cap, /, +, -, P, C, R\}. \tag{19}$$

Thus, an algebraic system  $\Sigma = (S, \Omega)$  over a set of program structures and operations on them (union, connection, differences and projections) is defined.

e) *Characteristics of simple and complex graph structures*

Among the variety of program structures there are three main ones – a simple, complex structure with a call of modules from the external environment and a dynamic structure. The main purpose of various structures is the most optimal use of the main memory during the execution of the unit [15-20].

*Simple structure.* An aggregate with a simple structure is created in the process of building modules based on the operations of link calls. The amount of main memory occupied by an aggregate with a simple structure is constant and equal to the sum of the volumes of individual modules:  $V_s = \sum_{i=1}^n v_i$ , where  $v_i$  is the amount of memory occupied by the  $i$ -th module. The corresponding graph of a modular structure is always connected.

*Complex structure.* Assembly of complex structures with dynamic invocation of modules in the shared memory is created in the Assembly process of the modules. In such an aggregate, the connections between the modules are not so rigid and their sequence is determined by the modules included in the chain. The modules are loaded into the main memory at the time of processing. When finished, the memory is freed and used to load another module. As in the case of a simple structure, the graph of a complex program structure is also connected (Fig.4) and is reflected in the adjacency matrix (2).

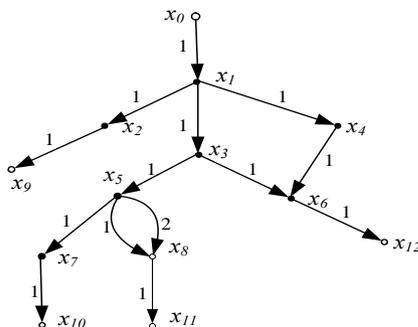


Fig. 4: Modification graph of program structure

The amount of main memory required depends on the number and composition of modules and the maximum amount of memory is equal to the sum of individual modules:

$$V_0^{\max} = V_s = \sum_{i=1}^n v_i.$$

The minimum amount of memory required when performing the aggregate is calculated by Floyd's algorithm, which determines the shortest path in the graph, in which each arc corresponds to a weight coefficient, called the arc length. The following transformations are performed to apply the Floyd algorithm.

- 1) Let's add new vertices and arcs to the graph. The vertices are  $x_0, x_{n+1}, \dots, x_{n+m}$ , where  $m$  is the number of end vertices. New arcs include  $(x_0, x_1, 1), (x_1, x_{n+1}, 1), \dots, (x_m, x_{n+m}, 1)$ . In them  $x_1$  corresponds to the main module and all  $x_i$  – to the end vertices. After performing operations, the graph of the modular structure (Fig. 1) is given to the graph on Fig. 5 with vertices  $x_0, x_9, x_{10}, x_{11}, x_{12}$ . Its vertices correspond to the weight coefficients:

$$v_0 = v_9 = v_{10} = v_{11} = v_{12} = 0$$

- 2) Each arc of the form  $(x_i, x_j, k)$  is assigned a coefficient  $v_{ij} = \frac{v_i + v_j}{2}$ .

Consider all routes leading from  $x_0$  to one of the other additional vertices. The length of the shortest route path is calculated as follows:

$$l_{0,n+p} = v_{01} + \dots + v_{rp,n+p} = \frac{v_0 + v_1}{2} + \dots + \frac{v_{2p} + v_{n+p}}{2} = \frac{v_0}{2} + v_1 + \dots + v_{rp} + \frac{v_{n+p}}{2} = v_1 + \dots + v_{rp}.$$

This length  $l_{0,n+p}$  will be equal to the sum of the memory modules for path  $x_1, \dots, x_{rp}$ .

Thus, applying Floyd's algorithm to the graph in Fig. 2, we solve the problem of calculating the amount of memory for the maximum chain.

- 3) We replace the adjacency matrix with the path matrix. For each  $m_{ij} > 0$ , the corresponding location will be  $v_{ij}$ . The values  $m_{ij} = \emptyset$  are replaced by  $-\infty$ . The program implementing Floyd's algorithm has the following form (it is assumed that the path matrix is described as a two-dimensional matrix  $(n \times n)$ : this length  $l_{0,n+p}$  will be equal to the sum of the memory modules for path  $x_1, \dots, x_{rp}$ .

for  $k = 1$  to  $n$  do

for  $i = 1$  to  $n$  do

for  $j = 1$  to  $n$  do

if  $M[i, j] < M[i, k] + M[k, j]$  then

$M[i, j] := M[i, k] + M[k, j]$ .

As a result of this algorithm, a matrix of maximum paths will be constructed. The maximum of  $l_{0,n+p}$  will determine the minimum amount of  $l_{0,n+p}$  memory for the memory-overlapping aggregate.

The most complex structure for the values  $V_0^{\min} \leq V_0 \leq V_0^{\max}$  can be constructed by following the algorithms proposed in [2-6]. The qualitative dependence of  $V_0$  on the number of dynamic sites is shown in Fig.5. Here  $n$  is the number of modules in the unit. Despite the different kind of curves, they have a common pattern – any  $V_0$  is enclosed between the values of  $v_0^{\max}$  и  $v_0^{\min}$ .

*Dynamic structure.* The mechanism of dynamic links between modules is different from the call mechanism. Dynamic objects are loaded into the main memory when they are accessed. By analogy, we call the volume loaded with a single treatment of a dynamic element, has its own program structure, for which the adjacency matrix is composed. If the same modules are found in different dynamic structures, they are different objects.

The original graph is used for illustration (Fig.1). Let the module corresponding to the vertex  $x_1$ , be dynamically called from the module corresponding to the vertex  $x_3$ . The resulting modified graph is shown in Fig. 6. A dashed arrow indicates a dynamic call. The module corresponding to the vertex  $x_6$ , occurs twice.

We construct an adjacency matrix for this aggregate. Each dynamic element will have its own *CALL* . To distinguish a dynamic call, the corresponding matrix elements will contain negative numbers whose absolute values specify the number of dynamic calls between the data of the module pair [20].

The adjacency matrix will look like:

$$M = \begin{pmatrix} x_1 & x_2 & x_4 & x_6 & x_3 & x_5 & x_6 & x_7 & x_8 \\ 0 & 1 & 1 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix} \tag{20}$$

We investigate the qualitative dependence of the amount of the number of dynamic segments (Fig.5. and 6). With one component in the software unit of a simple structure we have  $V_d^1 = V_s$ . If each dynamic component consists of one module, then the modified Floyd algorithm finds the maximum path and  $V_d^n = V_0^{min}$ .

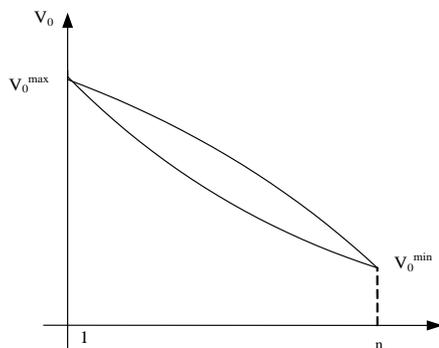


Fig. 5: Graphics of qualitative dependence  $V_a$  from the number of sub graphs

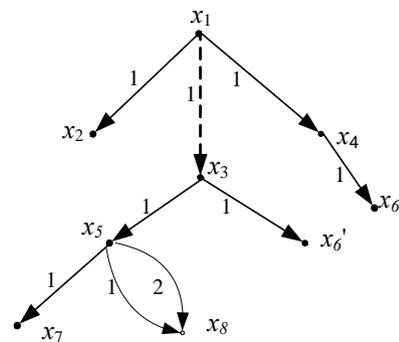


Fig. 6: Graph programs structure with dynamic Calls

For intermediate values, the dependence is more complex. On fig.7 presents two curves (1, 2), and n is the number of modules in the program unit.

Curve 1 defines a relationship in which different segments do not have the same modules. Curve 2 describes the dependence for the case when different segments have the same modules. For them, the required memory increases due to the duplication of

such modules. However, dependence 2 is typical for the case when there are no identical modules in dynamic structures and they are written in high-level *LP*. These modules are handled by utility tools – memory management, I/O, emergency handling, etc.

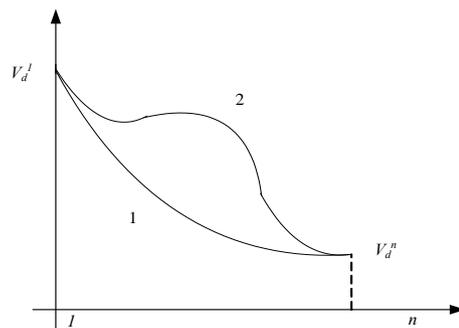


Fig. 7: Graphic dependence  $V_a$  from the number of dynamic elements

Due to the duplication of modules there is an increase in the main memory of the *OS*. Thus, curve 1 is characteristic of software aggregates of graphs in the form of a tree, which ensures that there are no identical modules in the graph. Despite the lack of dynamic structure in terms of memory savings, there is a significant advantage – independence from editing links. Each dynamic object can be modified, and editing relationships in the *OS* is not required.

### III. ASSEMBLING NODULES OF GRAPH G TO PROGRAMS

Let the graph  $G$  be represented by the set of modules  $X = \{x_1, x_2, \dots, x_m\}$ , as described in *LP*, and located at the vertices of the graph. The modules are assembled into a software unit. In this case, each pair of modules  $x_i, x_j$  ( $i, j$  – languages from the set of *LP*) are connected by the relation of call on the basis of which the module of communication  $x'_{ij}$  is formed. In General, for simple program structures, the aggregate contains link communication (call) operators and forward and reverse transformations of data types passed from the calling module (in  $i$ -language) to the calling module (in  $j$ -language) and back [23].

*LP* allows you to describe the information part - passport modules with a description of the transmitted data [8-14] and operations call modules. Taking into account the passports of the modules, the software structure of the unit is built (program - *Prog*, complex - *Comp*, package - *Pac*). The passport describes the special language WSDL containing: - a subset of the operations associate link elements of the graph in the language  $L'$  that contains a description of the parameters from the list of actual and formal parameters of the invocation; - mathematical operations on the graph and operations of binding modules in a complex structure (*Prog*, *Comp*, *Agr*, *Pac* and so on).

The operator modules link (make, config, assembling, etc. since 1994) takes the form:

Link <aggregate type> <aggregate name> (<main module name>, <additional list of module names>) <execution mode>, when constructing specific program structures, the vertices of the graph – modules can be marked with special symbols  $\rho$ , denoting:

$\rho = \Lambda$  – formation of a fragment with the name of the module;

$\rho = *$  – the beginning of the dynamic fragment with the vertex marked by this symbol;

$\rho = +$  the module in the graph  $G$  is marked as the main program of the complex;

$\rho = /$  – means enabling debugging or testing of the unit.

Ref

23. Ekaterina M.Lavrishcheva. Assembling Paradigms of Programming in Software Engineering.- 2016, 9, p.296-317, <http://www.scrip.org/journal/jsea>, <http://dx.do.org/10.4236/jsea.96021>.

Using these designations, the graph  $G$  will take the form shown in figure 8 and has a representation:  $E = \{(x_5, x_7, 1), (x_5, x_8, 1), (x_5, x_8, 2)\}$ .

The aggregate is given a unique name corresponding to the generated root module. For the graph  $\Gamma = \{(x_4, x_6, 1)\}$  a fragment of operators providing a dynamic call will be formed in the communication module  $x'_{46}$ . For a pair of modules specified in Fig.8 vertices  $x_4, x_6$ , the structure of the corresponding part of the unit, including the communication module, is shown in Fig. 9. Similarly links of heterogeneous modules and other types of calls are implemented.

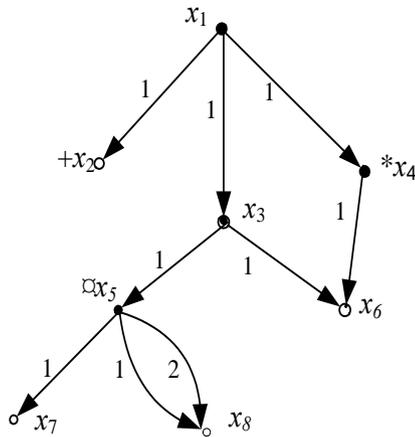


Fig. 8: Graph of software unit with control marks on the graph

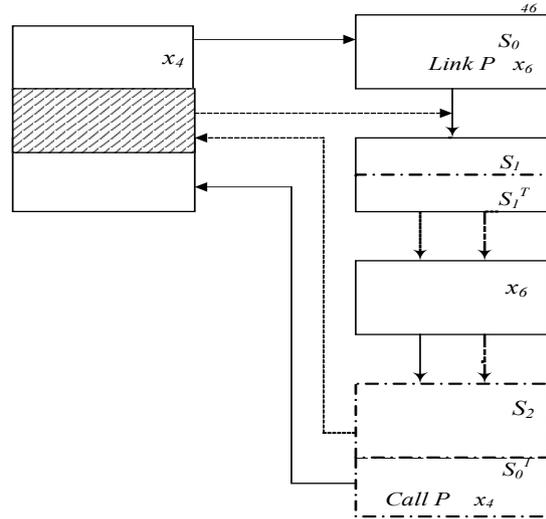


Fig. 9: Graph of modular structure with dynamic call [1]

Thus, for a pair of modules  $x_i, x_j$ , a module of connection  $x_{ij}$  of the form:

$$x'_{ij} = S_0 * (S_1 \times S_1^T) * (S_2 \times S_2^T) * S_0^I,$$

where  $S_0$  is a fragment of the aggregate that defines the environment of  $x_j$  module functioning;

$S_1$  – a fragment of the aggregate, including a sequence of calls to functions from the set  $\{P, C, S\}$ , each of which performs the necessary conversion of the actual parameters when referring to the  $x_j$ -module;

$S_2$  – a system with a fragment of operators for the inverse transformation of data types transmitted from  $x_j$  to  $x_i$  after its execution;

$S_0^I$  – a piece of software structures with operators epilogue for the vertex  $x_i$ , for the restoration of the environment.

For the described program structures, set the link operations to build the individual programs in Fig.8:

Link Prog  $P_1(x_1, x_2)$ ;

Link Prog  $P_2(x_1, x_3)(x_3, x_6)$ ;

Link Comp  $P_3((x_1, x_3)(x_3, x_5/x'_{58}) + (x_5, x_7))$ ; (20)

Link Prog  $P_4 (x_1, x_4), (x_4, x_6)$ ;

Link Comp  $(P_1 \cup P_2 \cup P_3 \cup P_4)$ .

Programs of the complex (aggregate) are given unique names  $(P_1, P_2, P_3, P_4)$  corresponding to the root names of the modules in the chains of the graph.

Thus, the process of constructing the program structure on the graph includes:

1. Enter the module description in the  $LP (L^{\wedge})$  and perform syntax checking.
2. Select the required modules and interfaces from the repositories and place them in the graph.
3. Translation of the unit modules in the  $LP$ .
4. Generation of communication modules for each interconnected pair of graph modules.
5. Assembly of the elements of the graph in the finished structure, linking modules in the operating system (IBM, MS, Oberon, Unix и др.) [1-5].
6. Test the system on data sets and assess the reliability of the unit.

After the modules are built, the name of the software Assembly is entered into the boot library. If you create a fragment that is later included in another aggregate, its name must match the name of the main module. In connection with the transition to the Internet environment to work with various software and system services in the configuration assembly of such tools provides security, data protection and quality assessment of ready-made modules, service resources and web systems in Internet.

*a) Ready-made software elements configurate to the system*

Under *the configuration of the system* is understood the structure of some of its version, including software elements, combined with each other by link operations with parameters that specify the options for the functioning of the system [1, 2, 16-22]. Version or variant of system configuration according to the IEEE Standard 828-2012 (Configuration) includes:

- configuration basis – BC (Configuration Baseline);
- configuration items (Configuration Item);
- program elements (modules, components, services, etc.) included in the graph;

Configuration Management is to monitor the modification of configuration parameters and components of the system, as well as to conduct system monitoring, accounting and auditing of the system, maintaining the integrity and its performance. According to the standard, the configuration includes the following tasks:

1. Configuration identification.
2. Configuration Control.
3. Configuration Status Accounting.
4. Configuration audit.
5. Trace configuration changes during system maintenance and operation;
6. Verification of the configuration components and testing of the system.

A configuration build uses a system model and a set of out-of-the-box components that accumulate in the operating environment repositories or libraries, and selects their operating environment Configurator (for example, in <http://7dragons.ru/ru>). The Configurator assembles the components according to their interfaces and generates a system configuration file.

The Configurator assembly of components and reuses with operation config, which is equivalent to the operations link (20) for figure 8, taking into account their interfaces. The *config* statement generates a program variant or system configuration file of Comp.

#### IV. THE MODERN AND FUTURE PARADIGMS PROGRAMMING

The theory of system programming is represented by numerous paradigms - mathematical, object-component, ontological, technical, service, aspect, etc. They replace on the *LP* and realized by different paradigms [15-17, 23-25], some of this paradigms are presented below.

##### a) Mathematical programming paradigms

Theory of graphs for design software modular structures with mathematical operations (union, projection, difference, etc.) implementation of linking the graph modules (objects) and the semantics of the transformation of data transmitted by the vertices of the graph *G*.

##### Object-component methods - OCM

OCM are the mathematical design of systems from ready-made resources (objects, components, services, etc.) to OM (Object Model). It is the formal method which transform the elements *OM* to a component model or a service model [15, 26].

*Graph objects* is designed on four levels:

*Generalizing* for determining *SD* base notions without considering of their essences and properties;

*Structuring* for ordering objects in the *OM* taking into account relationships between them;

*Characterization* for forming concepts of objects on the base of them properties and descriptions;

*Behavioral level* for descriptions of conduct depending on events (such as time).

That is, vertices of the graph *G* are objects of two types:  $O = (O_0, O_1, O_2, O_n)$  with the object relations hold  $\forall i (i > 0) \Rightarrow (O_i \in O_0)$  and interface objects *I* (Fig.10).

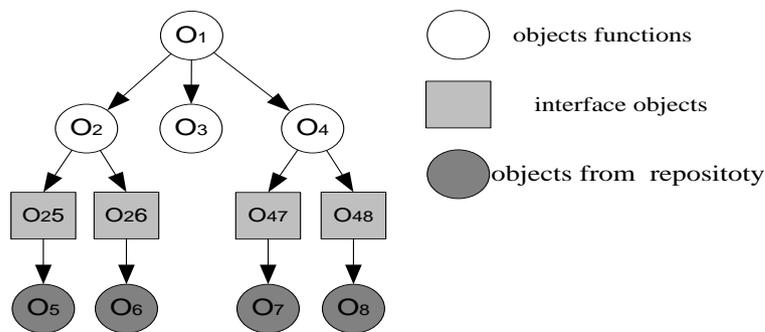


Figure 10: Object-interface graph *G*

At the vertices of a graph *G* contains the functional objects  $O_1, O_2, O_3, O_4, O_5, O_6, O_7, O_8$  and interface objects —  $O'_{25}, O'_{26}, O'_{47}, O'_{48}$ , which are placed in the repository of system, and arcs correspond to relationships between all kinds of objects. The parameters of the external characteristics of the interface objects are passed between objects through specified interfaces and are designated in language IDL *in* (input interface), *out* (output) and *inout* (intermediate). Based on the graph *G* we can construct a program  $P_0 - P_5$  using mathematical operation  $\cup$  Assembly link:

- 1)  $P_0 = (P_1 \cup P_2 \cup P_3 \cup P_4 \cup P_5)$ .
- 2)  $P_1 = O_2 \cup O_5$ ,  $link P_1 = In O'_5 (O_2 \cup O_5)$ ;
- 3)  $P_2 = O_2 \cup O_6$ ,  $link P_2 = In O'_6 (O_2 \cup O_6)$ ;
- 4)  $P_3$ ;
- 5)  $P_4 = O_4 \cup O_7$ ,  $link P_4 = In O'_7 (O_4 \cup O_7)$ ;
- 6)  $P_5 = O_4 \cup O_8$ ,  $link P_5 = In O'_8 (O_4 \cup O_8)$ ;

The set of objects and interfaces of the graph is reflected by general or individual properties and descriptions of the object model. Verification of properties of objects is provided by the specific operations (classification, specialization, aggregation, etc.) [15, 20, 29].

*Component paradigm.* The basis of this paradigm - OCM graph in which vertexes are the components of the CRP (reuses), interfaces and arcs specify the subject classification and the relationship between the vertices. Components are described by the formalisms of the triangle of Frege [15]:

- sign – identifier of the real function entity;
- denotation – the designation of this entity;
- concept – a set of properties defined by logical connections and must be true. Operations of OCM and component algebra represented on the website <http://7dragons.ru/ru> (in the VS environment.MS IBMSphere, Java, Linux, Intel etc.) [20].

*Service-component paradigm.* System and service-components - web resources implement intellectual knowledge of specialists about applied fields in the Internet environment [22 - 26]. Each implements some function and communicates with the technological interface to interact with other services through protocols and provide Assembly and solution of applications of different nature. The means of describing the application systems include:

- XML for description and construction of SSA components;
- WSDL to describe web services and their interfaces;
- SOAP to determine the formats of requests to the web services;
- UDDI for integration of services and their storage in libraries;
- building configuration (config) of the service resources in some high-quality and secure systems.

*The theory of graphs* develop in the school of A.P. Ershov (V.I. Kasyanov, V.E. Itkin, A. A. Evstigneev et al.) for programming Systems [13]. The graph theory has been actively developing in the Russian Academy of Sciences (I.B.Burdonov, A.S. Kosachev, V. V. Kulyamin [19]. The theory of conformity for systems with blocking and destruction for the schematic organization of memory in Linux.

*Methods of production of factories* (Product Line/Product Family) programs and Appfab and certificate them of the quality are discussed [23].

*Application of the ontology* language OWL ([www.semanticweb.com](http://www.semanticweb.com)), resource language (RDF) and intelligent agents of ISO 15926 standard for networking.

*Ontology of Life Cycle* and *Computational geometry* is a part of computer graphics and algebra. Used in the practice of computing and control machines, numerical control etc. is also used in robotics (motion planning and pattern recognition tasks), geographic information systems (geometric search, route planning), design chips, etc.[25-30].

Ref

19. Burdonov I. B., Kosachev A. S., Kulyamin V. V. Theory for systems with locks and destructions.-Moscow, 2008.- 411p.

*Cloud technologies* (PaaS, SaaS) are related to the Internet and are used to create adaptive applications that interact through agents of web pages.

*Device configuring Big Data Processing Devices* (Big Data) in Smart Data Internet 4.0.

b) *Intellectualization of systems*

The intelligent system implements creative tasks, the knowledge of which is stored in its memory. It includes — knowledge base, output mechanism and intelligent interface. The main tasks of artificial intelligence: symbolic modeling of thought processes, work with natural languages, presentation and use of knowledge, - machine learning, biological modeling of artificial intelligence, robotics [30].

c) *Application technical programming*

*Event management paradigm* based on the processing of external events (event-driven programming) in the Window environment. Features of the event paradigm are the use of testing methods based on operational (scenario) profiles of programs [20, 25, and 28].

*Coordinated and parallel programming* provides a division of the computational process into several subtasks (processes) for TRAN's computers and supercomputers, the results of which are sent via communication channels. Languages for parallel programming - PVM, LAM. CHMP and MPI (Message Passing Interface) interface descriptions and OpenMP. The POSIX standard provides messaging between programs in YAP C, C+ and Fortran.

*Programming on classes and on a prototype in OOP.* The principles of the OOP are: inheritance – the mechanism of establishing relations "descendant-ancestor" (the ability to generate one class from another with the preservation of all the properties and methods of the class-ancestor); encapsulation (the hiding of class implementation); abstraction (description of interaction only in terms of messages/events in the subject area); polymorphism (the possibility of replacing the interaction of objects of one object with another object with a similar structure). Many modern languages are specially created for programming on classes, for example, Smalltalk, C++, Java, Python, PHP, Object Pascal (Delphi), VB.NET, Xbase++, etc.

*Programming by prototype.* Creating a new object is done by one of two methods: cloning an existing object, or by creating an object from scratch. Reuse (inheritance) is made by cloning an existing instance of the object —a prototype Clone, a sample. An example of a prototype language is the Self language and it is the basis of such programming languages as JavaScript, Squeak, Cecil, Newton Script, Io, MOO, REBOL, Keno and etc.

*The Agile methodology* is focused on the close collaboration of a team of developers and users. It is based on a waterfall model lifecycle incremental and rapid response to changing demands on PP. The team works according to the schedule and financing of the project.

*eXtreme Programming (XP)* implements the principle of "collective code ownership". It any member of the group can change not only your code but also code another programmer. Each module is supplied with the Autonomous test (unit test) for regression testing of modules. Tests written by the programmers and they have the right to write tests for any module. Thus, most of the errors are corrected at the stage of encoding, or when you view the code, or by dynamic testing.

Ref

30. Lavrischeva E.M. Scientific Basis of System Programming.- Journal of Software Engineering and Applications (JSEA), Vol. 11 No. 8 of August issue, 2018.-N 11.- p.408-434, ISSN online 1945-3124, ISSN Print 1945-3116. <http://www.scirp.org/journal/jsea>

*SCRUM* is agile methodology project management firm Advanced Development Methods, Inc., used in organizations (Fuji-Xerox, Canon, Honda, NEC, Epson, Brother, 3M, Xerox and Hewlett - Packard etc.) are based on an iterative lifecycle model with well-defined development process, including requirements analysis, design, programming, testing (<http://agile.csc.ncsu.edu>).

*DSDM* (Dynamic Systems Development Method) for rapid development of RAD (Rapid Application).

d) *Ensuring the quality of AS, Web systems*

According to the ISO / IEC 12207 standard, the software LC standard regulates the planning, quality management and cost estimation for the creation of the system. In these processes, lifecycle analyses quality assurance; verification and validation (V&V) resources and evaluating the degree of achievement of individual quality indicators; test of the finished system; data collection about the failures, defects etc. and failures; assessment of the reliability on the respective reliability models based on the results of testing [33, 35, 36].

The ISO/IEC 9000 (1-4) Quality model defines characteristics  $q_1$  —  $q_6$ :  $q_1$  (functionality),  $q_2$  (reliability),  $q_3$  (usability),  $q_4$  (efficiency),  $q_5$  (maintainability),  $q_6$ (portability).

Each  $q_i$  characteristic is calculated according to special formulas and metrics of the standard. Reliability is evaluated according to the errors, defects and failures in the SOFTWARE obtained during the testing process and according to the corresponding reliability models (evaluation, measurement, etc.). Data on all quality indicators  $q_1$  —  $q_6$  are evaluated by the formula:

$$q_i = \sum_{j=1}^6 a_{ij} m_{ij} w_{ij}$$

where  $a_{ij}$ -attributes of each quality indicator ( $i = 1..6$ );  $m_i$  - metrics of each quality attribute;  $w_i$  - weight of each attribute of the system quality indicator. The obtained values for the indicators of the quality model are included in the product quality certificate. Options for assessing the quality of configured systems are given on the website <http://7dragons.ru/ru>.

e) *Perspective directions for the development of the Internet*

Promising areas of development for the Internet1 include [28]:

The information objects (IO) that specifies the digital projection of real or abstract objects that use Semantic Web Ontology interoperability interfaces. IO through Web services began more than 10 years ago. Interaction semantics IO is based on RDF and OWL language of ISO 15926 Internet 3.0.

The next step of the development of the Internet is Web 4.0, which allows network participants to communicate, using intelligent agents. A new stage in the development of enterprise solutions-cloud (PaaS, SaaS) who spliced with Internet space and used to create Adaptive applications. Cloud services interact through the Web page by using agents.

*Internet of Things* Smart IoT to support competitive APPS using: distributed microservices; Hypercat Mobile; GSM-R traffic control. Industrial Internet develops concepts - “smart energy”, “smart transportation”, “smart appliances”, “smart industry”, “smart homes and cities”, etc. Internet stuff (Internet of Things, Smart IoT) indicates the Smart support competing APPS using distributed micro services such as

Hyper cat (mobile communications); industrial Internet (Industrial), covering the new automation - transportation, appliances, industry, and another.

f) *Computer nanotechnology*

Today computer nanotechnology is actually already working with the smallest elements, "atoms" similar to the thickness of the thread (transistors, chips, crystals, etc.). For example, a video card from 3.5 million particles on single crystal, multi-touch maps for retinal embedded in the eyeglasses, etc.

In the future, ready-made software elements will be developed in the direction of nanotechnology by "reducing" to look even smaller particles with predetermined functionality. Automation of communication, synthesis of such particles will give a new small element, which will be used like a chip in a small device for use in medicine, genetics, physics, etc.[28].

## V. CONCLUSION

In the early stages of the emergence of the method of assembling large programs and complexes of spent modules in the LP used the theoretical apparatus of graphs to create modular program structures. Graph theory allows to establish the shortest path of program elements and prove the correctness of binding graph modules using adjacency matrices, reach ability and mathematical operations (association, connection, difference, etc.) in complex program structures (complex, aggregate, system, etc.). Initially, the method of Assembly on the basis of graph theory was widely implemented in the complex systems (Juza, Ruza, Prometheus) under the leadership of Lipaev V.V. [1-5], and was supported by A. P. Ershov in the IPI SO Academy of Sciences SSSR and his researcher and scientist, who formulated the theoretical aspects of the application of graph theory in programming [6-14]. Since 2013, graph theory has been used in the modeling of complex systems of objects, components, services, etc. (OCM) [15] and has been used in the world practice in the transition to the Internet environment [22, 23]. The paper describes the features of modeling systems using graph theory and mathematical operations on elements of software structures. The new Assembly operations – *config* of the IEEE Standard 828-2012 (Configuration) are implemented in different environments of Internet. Elements of the graph set transition labels to obtain reactions at the time of exposure to test sets, proof of completeness of testing systems of AS and the measurement of quality ready AS.

Programming paradigms on the graph and ontology of mathematical modeling of applied problems for vital areas of society (medicine, biology, physics, mathematics, economics, etc.) will become the main tools of smart machines and AS of the 21st century [15, 24-31].

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